

Roadmap for Molecular Benchmarks in Nonadiabatic Dynamics

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ABSTRACT: Simulating the coupled electronic and nuclear response of a molecule to light excitation requires the application of nonadiabatic molecular dynamics. However, when faced with a specific photophysical or photochemical problem, selecting the most suitable theoretical approach from the wide array of available techniques is not a trivial task. The challenge is further complicated by the lack of systematic method comparisons and rigorous testing on realistic molecular systems. This absence of comprehensive molecular benchmarks remains a major obstacle to advances within the field of nonadiabatic molecular dynamics. A CECAM workshop, *Standardizing Nonadiabatic Dynamics: Towards Common Benchmarks*, was held in May 2024 to address this issue. This Perspective highlights the key challenges identified during the workshop in defining molecular benchmarks for nonadiabatic dynamics. Specifically, this work outlines some preliminary observations on essential components needed for simulations and proposes a roadmap aiming to establish, as an ultimate goal, a community-driven, standardized molecular benchmark set.

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I. INTRODUCTION

Modeling the dynamical behavior of a molecular system upon photoexcitation is a formidable theoretical and computational challenge. This is due to the involved coupled electron-nuclear dynamics, the so-called nonadiabatic effects, that necessitate treatment beyond the Born-Oppenheimer approximation.¹⁻⁸ As a result, the development of methods for simulating nonadiabatic molecular dynamics (NAMD) remains a key area of focus,⁹⁻²¹ with research groups in theoretical chemistry and chemical physics having been particularly active in improving and testing simulation methods for several decades.

The field of NAMD has benefited from advances in experimental techniques capable of imaging the coupled electron-nuclear dynamics of molecules upon light absorption. The development of ultrashort laser pulses and subsequent experiments in femtochemistry²² revealed direct measurements of dynamical processes in molecules,²³⁻³¹ which have helped validating and guiding advances in NAMD methodologies. However, the field of NAMD has also been fueled by significant progress in the development of efficient algorithms and software³²⁻⁴⁷ able to solve the coupled dynamics of electrons and nuclei. Thanks to all of these developments, strong collaborations between experiments and theory, for example in the context of gas-phase time-resolved spectroscopy,⁴⁸⁻⁵⁷ have emerged for studying the excited-state dynamics of many systems, and have sparked community efforts aiming to challenge the predictive power of various NAMD methods.⁵⁸ Despite these significant steps toward unraveling the ultrafast photodynamics of numerous molecular systems, the field of NAMD still faces considerable challenges, as the following sections will discuss. At the same time, the reliability and trustworthiness of theoretical predictions often remain difficult to assess.

As a result, the community of developers and users of NAMD has recently pointed out the critical need for established and standardized benchmarks to advance the field. By *benchmark* here, we mean well-chosen systems that can be used to compare and test computational methods, along with a community-accepted robust procedure to be followed whenever newly developed methods and approximations in NAMD are tested. Benchmarks in NAMD are

needed to improve methodologies, ensure reproducibility, estimate the reliability of the predictions, and enable theoretical developments to keep pace with experimental techniques. Further, we believe that benchmarking existing methodologies and codes will ultimately assist users and newcomers to NAMD in identifying the most suitable technique for addressing specific problems.

Benchmarking has long been a cornerstone of computational chemistry, for instance of electronic structure theory,^{59–63} and computational sciences in general.^{64,65} While such efforts serve as inspiring examples, NAMD presents unique challenges due to its inherent complexity. The outcome of an NAMD simulation relies on the calculation of observables with intricate time and energy dependencies, which are often associated with a wide range of physical and chemical phenomena. The high dimensionality of realistic molecular systems makes it impossible to simulate their quantum dynamics exactly. As a result, using approximations to the time-dependent molecular Schrödinger equation is necessary, which has driven the development of numerous NAMD methods over the past 40 years.

So far, mostly low-dimensional models of nonadiabatic processes have served as benchmark sets for NAMD.^{66–72} These models have often been engineered to challenge specific aspects of the NAMD formalism and offer the great advantage that they typically have numerically exact results to compare with. The famous Tully models, proposed in 1990 to evaluate the accuracy of the trajectory surface hopping method,⁶⁶ are still nowadays widely used by the NAMD community. This set of three one-dimensional model systems was specifically designed to investigate prototypical nonadiabatic processes, including single and multiple nonadiabatic crossings. However, the overarching goal of NAMD methods is to describe the photodynamics of a molecule in its full dimensionality. Thus, benchmarking NAMD on realistic photochemical processes is necessary to provide justification for their suitability in the simulations of the molecular systems of interest. In addition, while some approximations are thoroughly tested and understood for low-dimensional problems, their performance in higher dimensions is not necessarily known. In this respect, multidimensional model potentials are also important for benchmarking, and are often used by the community especially to compare fully-quantized and mixed quantum-classical approaches.^{68,73–76}

Constructing multidimensional potential energy surfaces (PESs) can rapidly become a

very difficult task. The situation becomes even more complex for large molecular systems (hundreds of atoms) involving dozens of coupled excited states, where energies, gradients, and nonadiabatic couplings must all be considered. In these cases, strategies to reduce computational costs, such as dynamically limiting the number of excited states or nonadiabatic couplings to be calculated, become indispensable.⁷⁷

The challenge of constructing multidimensional PESs is often circumvented by performing excited-state dynamics based on on-the-fly electronic structure calculations. Therefore, the concept of benchmarks needs to be adapted to on-the-fly NAMD, as was recently done with the “molecular Tully models”, composed of ethylene, 4-*N,N'*-dimethylaminobenzonitrile (DMABN), and fulvene.⁷⁸ This benchmark set has been adopted by the community, and already several NAMD methods have been tested on one or more of these systems.^{79–86} While useful, the molecular Tully models have shortcomings, such as the limited set of properties that have been used for comparisons, the fact that initial conditions were oriented towards trajectory-based methods, and the fact that only commercial software has been used for the underlying electronic structure, preventing broader accessibility and reproducibility. Even leaving the electronic-structure problem aside, it is evident that developing generalized and reliable benchmark sets for NAMD comes as a stringent challenge and currently hampers further developments in the field.

A CECAM workshop,⁸⁷ entitled *Standardizing nonadiabatic dynamics: towards common benchmarks*, took place in Paris in May 2024 with the central goal of stimulating the NAMD community towards developing a common benchmark set by (i) agreeing on the main ingredients required to test all families of NAMD techniques, of which we will provide examples in Section II, and (ii) selecting potential molecular systems for further tests. This Perspective summarizes the main conclusions reached during the CECAM workshop, aiming to inform the broader scientific community and encourage future benchmark efforts. More specifically, this Perspective serves as an opportunity to elaborate on key questions that emerged from the workshop regarding what makes a proper benchmark in NAMD.

Discussions made it clear that, given the complexity of NAMD simulations, initial attempts to propose realistic molecular benchmarks should begin with simple systems, namely small or medium-sized molecules in the gas phase. Even with such a limited focus, numerous open

questions still arose during the discussions in the workshop.

- What constitutes an adequate reference for a benchmark in NAMD? An experiment or an accurate simulation?
- How do we decide which observables should be prioritized when establishing the reliability of a given method?
- How can NAMD methods based on fundamentally different theoretical frameworks be compared, such as those based on wavefunctions and those based on trajectories?
- How can different electronic-state representations and the intricacies of electronic-structure methods be handled?
- How can we even ensure that different NAMD techniques are initialized in the same way for a given benchmark system?
- How can we ensure that statistical convergence of computational results is achieved?

In addition to offering a structure for this Perspective article, the questions above highlight key topics that require dedicated attention to ensure the definition of proper and generalized benchmark systems in nonadiabatic dynamics. Accordingly, Section II A proposes some prototypical phenomena and related families of molecular systems that were considered appropriate for benchmarking. Section II B is dedicated to the different families of NAMD methods, aiming to identify the most representative theoretical approaches that can be used for a systematic comparison. Section II C provides a brief overview of the issues related to various electronic-structure methods for obtaining electronic energies and other electronic properties. In Section II D, we discuss the problem of the initial conditions for NAMD and how to ensure an equivalent initialization of the dynamics across different theoretical methodologies. Section II E identifies suitable physical observables and properties that can be directly calculated in an NAMD simulation and used in the context of benchmarking. In Section II F, we examine the role of experimental measurements and their suitability as a reference for NAMD. Finally, Section III summarizes the key insights that emerged from the CECAM

workshop and outlines practical strategies for the community to advance the initiative of establishing robust benchmark systems for NAMD. We discuss how members of the community with diverse expertise can organize, share data, and collaborate effectively while also briefly exploring the future prospects for benchmarking. In this sense, this Perspective acts as a *roadmap* for future developments in NAMD.

II. TOWARDS MOLECULAR BENCHMARKS: GENERAL CONSIDERATIONS

A. Selected photophysical and photochemical phenomena for benchmarking

This Section describes photophysical and photochemical processes that could be used to assess the performance of different NAMD methods. In the following, we propose to select a few specific light-triggered phenomena, with the aim of achieving two main goals: narrowing down the choice of current benchmark systems, and providing some clear points of comparison between the results of different NAMD calculations (see also Section II E). The chosen phenomena should cover diverse aspects of photodynamics, highlighting the role of both nuclear and electronic effects. They should be generally well understood to avoid controversies related to the interpretation of the results. Additionally, we choose to privilege unimolecular processes in order to avoid unnecessary complexities in the early stage of building a benchmark strategy. With these elements in mind, the following four types of processes, which are briefly described below and illustrated in Figure 1, were preselected as interesting test systems.

- Photoisomerization (ISO): $ABC + h\nu \rightarrow CAB$
- Photodissociation (DIS): $AB + h\nu \rightarrow A + B$
- Nonreactive radiationless relaxation (NRR): ${}^1A + h\nu \rightarrow {}^1A^* [\rightarrow {}^3A^*] \rightarrow {}^1A$
- Excited-state intramolecular proton transfer (ESIPT): $AH \cdots B + h\nu \rightarrow A \cdots HB$.

We note, however, that this list of phenomena is by no means exhaustive and future benchmark efforts will extend this selection to include, for instance, systems with high densities of

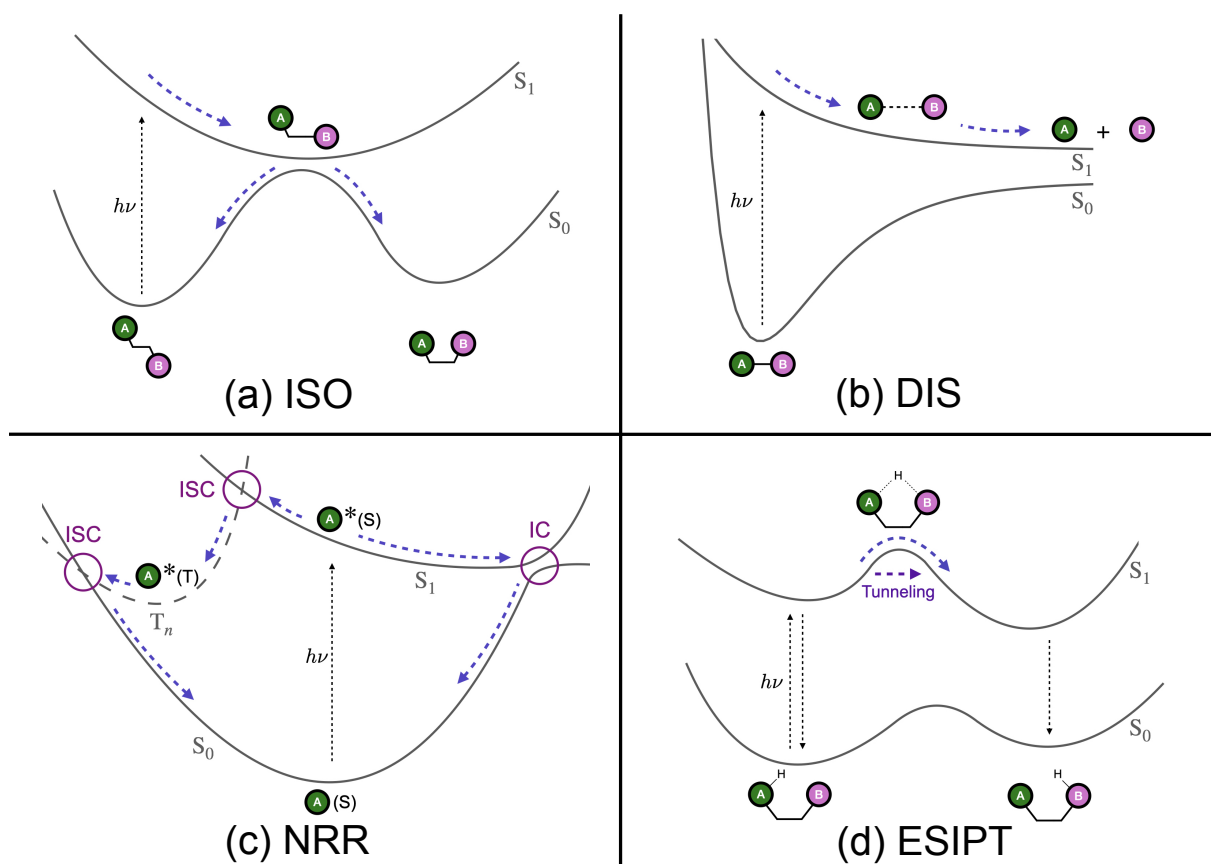


FIG. 1: Schematic representation of the four phenomena of interest for the benchmarking of NAMD methods: (a) Photoisomerization, i.e. an isomerization induced by photoexcitation; (b) Photodissociation, i.e. bond-breaking activated by absorption of light; (c) Nonreactive radiationless relaxation, i.e. transition between electronic states initiated by photoabsorption, potentially involving different spin multiplicities, without resulting in different photoproducts; and (d) Excited-state intramolecular proton transfer, occurring upon photoexcitation, typically involving hydrogen-bonded donor and acceptor groups. The curves labeled with S and T represent singlet and triplet potential energy curves, respectively, and the asterisk indicates an excited state of a species. The blue dashed arrows show nuclear motion along a molecular coordinate.

electronic states, initialized in a coherent superposition of states, systems undergoing photoinduced electron transfer, or excited-state energy transfer or charge migration, or complex dynamical processes such as molecular collisions.

The above phenomena are some of the most common photoinduced processes in molecules

(see textbooks on molecular photophysics and/or photochemistry^{2,88–91}) and are representative of many of the current applications of NAMD methods. A search through the Semantic Scholar Academic Graph⁹² indeed reveals that, when using the keywords “nonadiabatic dynamics”, at least 50% of research articles on molecular systems published in the last 10 years discuss one of the four phenomena outlined above. Each of these phenomena presents a different challenge from a theoretical perspective: complex interplay between electronic character and nuclear motion (DIS), potential involvement of tunneling effects (ESIPT), molecular rearrangement (ISO), or complex transfer of electronic population (NRR). In the following, we discuss a few selected examples (i.e., not an exhaustive list) that demonstrate the importance of such light-induced processes.

One of the most paradigmatic examples of ISO is the *cis* → *trans* isomerization of retinal induced by photon absorption in mammalian eyes.^{93,94} Azobenzenes, stilbenes, and spiropyrans are also prominent classes of compounds subject to photoisomerization, which have widespread applications in molecular switches, photopharmacology, and smart materials.^{95–105} As shown in Figure 1a, photoisomerization¹⁰⁶ begins with light absorption, which weakens an originally locked bond (for example, by promoting an electron from a π to a π^* molecular orbital in a π bond). This weakening of the originally locked bond allows the molecule to rearrange easily, often by rotation around a (pseudo-)single bond. In many photoisomerization processes, such as those involving retinal, azobenzene, and stilbene, the first excited state possesses a minimum located very close to the S_0/S_1 conical intersection (see Figure 1a). This minimum often corresponds to a geometry where the isomerization dihedral angle is close to 90–110°. Upon reaching this region of configuration space, the molecule can either proceed with a full photoisomerization or return to the original isomer, typically through a nonradiative decay involving a conical intersection and additional nuclear motion.¹⁰⁶

In the field of femtochemistry, DIS was one of the first studied processes,^{22,107} and is schematically represented in Figure 1b. In the series of pioneering experiments by Zewail, the study of the photodissociation of iodocyanide (ICN)¹⁰⁸ preceded that of sodium iodide (NaI),¹⁰⁹ which was already studied in the earliest experiments of Polanyi.¹¹⁰ Wavepacket dynamics simulations have supported these experiments from the beginning^{69,111–115} and NaI, as well as similar alkali halides, has been extensively used as a simple one-dimensional test

case for quantum dynamics methods since.^{116–118} DIS has also been proposed as a key mechanism driving the buildup of chemical complexity in interstellar environments. Small organic species present in large interstellar dust clouds are constantly bombarded by various kinds of radiation, including UV light.¹¹⁹ Absorption of such photons by, for example, methanol (significantly abundant in interstellar environments), phenol or pyrrole readily leads to chemical bond breaking via dissociative excited states (S_1 in Figure 1b).^{120–122} The resulting reactive radical intermediates can then kick-start a chain reaction, whereby larger molecules are eventually formed.¹²³

NRR involves the complex nonradiative electronic population decay that can be observed between states of the same spin multiplicity (internal conversions) or between states with different spin multiplicity (intersystem crossings), see Figure 1c. Beyond common single crossings between excited states within the singlet manifold,¹²⁴ typical examples of complex internal conversions that do not involve large amplitude nuclear motions are decays induced by repeated crossings of regions of strong nonadiabaticity¹²⁵ or reflections⁷⁸, three-state conical intersections¹²⁶ or extended degeneracies between electronic states.¹²⁷ Intersystem crossings are driven by spin-orbit coupling, and are, thus, most often associated with transition metal complexes.¹²⁸ Nonetheless, they are also common in organic molecules^{129–133}, particularly in carbonyl compounds, when sulfur- or selenium-substituted,^{134–137} and in nitroaromatic compounds.^{138,139} The rate at which triplet states are (de)populated is of great interest in the context of functional chromophores, used, for example, in optoelectronics.^{140–142} It should be noted that since spin-orbit coupling is generally relatively weak, the timescale necessary for observing significant intersystem crossing can range from few hundreds of femtoseconds to hundreds of nanoseconds.^{140,143–146} In addition, the performance of simulations of intersystem crossing may depend on the strength of spin-orbit coupling, especially since it is also now established, experimentally and theoretically, that intersystem crossing can compete on similar time-scales as internal conversion, at least in geometrically unconstrained molecules with high density of states and overlapping spin manifolds.^{147–149} Although several NAMD approaches have been formulated to describe intersystem crossing,^{134,146,150–160} simulations over long timescales still remain challenging.

ESIPT reactions may occur in complex biological systems and are exploited for the devel-

opment of sensors and sunscreens, among others.^{161–164} For the purpose of our benchmark, ESIPT processes taking place on ultrafast timescales are of particular interest as they are generally simpler to simulate with most NAMD methods.¹⁶⁵ Molecules exhibiting ESIPT typically contain donor and acceptor units linked by an intramolecular hydrogen bond, allowing the proton to easily migrate upon photoexcitation.^{166,167} The mechanism of this migration can occur via two distinct pathways, illustrated in Figure 1d. The small barrier is overcome thermally, after which the proton undergoes a “ballistic” type motion between the donor and the acceptor; alternatively, tunneling through the potential barrier is also possible. The proper description of tunneling requires the treatment of at least some nuclear degrees of freedom (e.g., protons) at the quantum level,^{168–170} which may constitute a challenge for NAMD methods relying on classical-like trajectories.

In summary, the phenomena highlighted in this section, i.e., ISO, DIS, NRR and ESIPT, are representative of a large variety of processes found in photophysical and photochemical applications, from the study of the interstellar medium to optoelectronics. Simulating the underlying photodynamics requires that NAMD methods are able to capture challenging features, as mentioned above. Therefore, determining the capability of NAMD methods to describe accurately these highlighted phenomena will provide valuable insights into their strengths.

B. Computational methods for NAMD

Many different NAMD methodologies have been developed over the years,⁶ and in the interest of treating a comprehensive set of molecular benchmarks, the techniques developed and applied within the NAMD community should be broadly represented. Here, we briefly summarize some of these approaches related to molecular dynamics and (photo)chemical reactions, with a schematic overview being given in Figure 2.

Early efforts in the field can perhaps be traced back to the development of real-space grid-based solvers for the time-dependent Schrödinger equation, such as the discrete variable representation (DVR) approach,^{171,172} or sparse-grid approaches.^{40,173} Going beyond the DVR picture whilst maintaining the concept of a fixed underlying basis, the multicon-

figurational time-dependent Hartree (MCTDH) family of methods^{174,175} comprises a powerful range of exact numerical wavefunction solvers, including the original and multilayer (ML-MCTDH) formulations,^{176,177} which are available for fermions, bosons, and mixtures of the two.¹⁷⁸ There are also approaches within this framework to treat density operators (ρ -MCTDH).^{179–182} While fundamentally different at first sight, the time-dependent density matrix renormalization group (TD-DMRG)^{183,184} and tree tensor network state (TTNS) extensions thereof actually are another way to solve the ML-MCTDH equations of motions.^{185,186}

A challenge for applying these approaches to high-dimensional systems is that the global electronic PESs and related couplings as well as local operators are required to be in a separable form, either sum-of-products (for MCTDH) or a tree, multilayer representation (for ML-MCTDH), as a prerequisite.^{187,188} Alternatively, additional time-dependent sparse-grid approximations can be used together with MCTDH methods.^{189,190} Furthermore, the surfaces and couplings should preferentially be in a diabatic representation to avoid numerical issues arising from singularities at conical intersections in the adiabatic representation.

Relaxing the constraint of having a fixed basis has led to dynamical wavepacket methods such as full multiple spawning (FMS)¹⁹¹ and ab initio multiple spawning approaches (AIMS),^{11,192} as well as the recent variants of AIMS that have been developed to include external fields,¹⁹³ spin-orbit coupling,¹⁵⁰ and to optimize the computational efficiency.^{194,195} In this family of methods, nuclear trajectory-basis functions represented by frozen Gaussians evolve classically on adiabatic PESs. In addition, there is the closely related range of techniques stemming from multiconfigurational ansätze, such as the coupled-coherent states approach (CCS),¹⁹⁶ the multiconfigurational Ehrenfest method (MCE),¹⁹⁷ and the ab initio multiple-cloning algorithm (AIMC),¹⁹⁸ that in general use different PESs than the adiabatic ones to evolve the trajectory-basis functions.

Using a fully variational framework with Gaussian wavepackets leads to the variational Gaussian-based approaches, namely the variational multiconfigurational Gaussian (vMCG) formulation and Gaussian-based MCTDH (G-MCTDH).^{199–201} More recently, direct-dynamics extensions of vMCG (DD-vMCG) have been developed enabling implementations with on-the-fly electronic structures,²⁰² forgoing the need to precompute a global PES.

While the above trajectory-guided methods have been developed to directly tackle the

time-dependent molecular Schrödinger equation, quantum-classical methods simplify the coupled electron-nuclear quantum problem by decomposing it into a quantum electronic system coupled to a classical-like nuclear system. Quantum-classical approaches can capture some of the quantum aspects of nuclear dynamics by using an ensemble of trajectories to represent the nuclear density, and they are extremely appealing due to their tractable computational cost.

Surface-hopping methods, in their original formulation^{66,203,204} and further developments^{153,205–211} have become an important class of algorithms for simulating mixed quantum-classical dynamics. Of these, the fewest switches surface hopping (FSSH) approach of Tully⁶⁶ is perhaps the most popular choice in current practice. Alternative hopping formalisms have been introduced and gained popularity to circumvent the direct calculation of nonadiabatic or overlap couplings, such as Landau-Zener surface hopping (LZSH) or Zhu-Nakamura theory.^{205,212–214} Decoherence corrections (dFSSH), which are intended to cure the overcoherence problem with FSSH and ensure consistent numerical propagation of classical and quantum populations by enforcing population alignment during decoherence events,^{15,215} have been developed from numerous different approaches,^{216–221} as well as alternative hopping algorithms.^{212,222–225} While surface-hopping methods are a popular choice in applications, there remain many open questions in terms of conceptual grounds¹⁵ and formulation of an optimal algorithm, particularly, pertaining to how velocity rescaling and frustrated hop protocols are implemented,^{226,227} or concerning the treatment of trivial crossings.^{228,229} As such, a range of alternative surface-hopping approaches have also been developed, including approximate methods based on the exact factorization of the full molecular wavefunction,^{230,231} which can involve coupled^{223,232–234} or auxiliary^{235–238} trajectories (SH-XF). Other FSSH-based variants that offer improved accuracy have also been developed^{221,225,238–242}. For example, while the standard implementations of surface-hopping methods conserve the energy of each classical nuclear trajectory in the ensemble, it has been pointed out that energy should be conserved over the trajectory ensemble as a whole, as quantum-trajectory surface-hopping methods do,^{241,242} which eliminates the need for velocity rescaling and special treatments for forbidden hops. Surface hopping has also been generalized beyond internal conversion^{153,243,244} and beyond the usual quantum-electron/classical-nuclei partitions.²⁴⁵

Recently, using the semiclassical mapping formalism, a mapping approach to surface hopping (MASH) has also been introduced.^{246–248}

Mean-field type approaches are another major category of trajectory-based dynamics methods. While Ehrenfest dynamics²⁴⁹ belongs to the family of quantum-classical methods and is perhaps the most well-known method of this type, a number of notable improvements have been developed. Quantum-Ehrenfest (Qu-Eh) combines the idea of evolution on an average potential with quantum dynamics and has been related to a particular formulation of vMCG.²⁵⁰ The ab initio multiple cloning (AIMC) has been proposed as an alternative to address the coherence issues inherent in Ehrenfest trajectories, naturally incorporating decoherence through *cloning* events.^{198,251} A valuable improvement of semiclassical Ehrenfest was the inclusion of coherence and decoherence effects in the coherent switching decay of mixing (CSDM) method.^{252–254} One important branch of these developments stems from the semiclassical initial value representation.^{255–259} The quantum-classical Liouville equation^{260,261} has also been used to derive mean-field²⁶² and improved mean-field algorithms using full^{263,264} and partial linearization techniques^{265,266}, introducing the groups of linearized semiclassical methods (LSC) and partially linearized methods (PLDM). A closely related range of techniques have been developed using a path integral formulation²⁶⁷, which also permits full²⁶⁸ and partial linearization²⁶⁹ approximations. More recently, fully linearized,^{270–274} and partially-linearized^{275,276} approaches based on the mapping formalism (linearized spin mapping, LSM) have been put forward,²⁷⁷ which have also proven to offer improved accuracy over the Ehrenfest limit. More generally, it is worth noting that mapping Hamiltonian approaches, such as the Meyer-Miller model, provide an effective framework for investigating nonadiabatic dynamics by transforming discrete quantum states into continuous physical variables.^{277–284} In this way, electronic and nuclear degrees of freedom can be treated on an equal footing in the phase space.^{263,285,286} The exact factorization of the full molecular wavefunction can also be used as a starting point to derive coupled-trajectory mixed quantum-classical (CT-MQC) dynamics,^{287–290} such that decoherence effects naturally emerge as correction terms to the mean-field Ehrenfest equations. Additional variants of mean-field Ehrenfest have been developed to include external fields and simulate transient absorption spectroscopy.^{291,292}

In the density matrix representation, a further range of numerically exact approaches

have been developed to solve the electron-nuclear problem. Real-time path integral methods such as the quasi-adiabatic path integral (QuAPI) methods,^{293,294} and recent extensions such as the quantum-classical path integral approach²⁹⁵ and the small matrix path integral approach,²⁹⁶ use the Feynman path integral method to propagate quantum degrees of freedom. Nonequilibrium Green's functions (NEGF),^{297–299} often applied to mesoscopic systems and transport problems, can also be of interest to study proton tunneling reactions.³⁰⁰

Other related quantum dynamics methods, which employ either a density-matrix or a wavefunction formalism, are also worth mentioning here, such as nuclear-electronic orbital (NEO) methods,^{170,301,302} the hierarchical equations of motion (HEOM) method,^{303,304} TTNS approximations^{305,306} and tensor-network-based time-evolving block-decimation techniques (TEBD), among others.^{307,308}

A careful comparison between quantum dynamics and trajectory-based NAMD should address the potential for zero-point energy (ZPE) leakage in the latter, especially in long-time-scale processes such as intersystem crossings. Recently developed Hessian-free ZPE correction methods provide a promising solution to improve the consistency of simulations across these approaches.^{309,310}

Recent, provably efficient quantum-computer (QC) algorithms for NAMD simulations present additional opportunities for benchmarking. QC NAMD algorithms use the exponentially large Hilbert space of the QC to represent the Hilbert space of the nuclei and electrons of molecules. This representation allows them to prepare states, simulate dynamics, and measure observables using time and memory polynomial in system size. QC algorithms have been developed for both analog quantum simulators and fully programmable digital quantum computers. Most of the analog approaches are simulations of vibronic-coupling models,^{311–314} and have been implemented on quantum hardware to simulate dynamics around conical intersections,³¹² charge transfer,³¹³ and photoinduced dynamics in molecules such as pyrazine.³¹⁴ Digital algorithms require large-scale, fault-tolerant quantum computers, but they could simulate the time-dependent Schrödinger equation of all nuclei and electrons on a grid exactly, up to a known and controllable error.^{315–319} Other digital algorithms for near-term QCs use variational principles, but lack provable error bounds.^{320,321} QC approaches both require new benchmarks to allow fair comparisons with heuristic classical methods and deliver

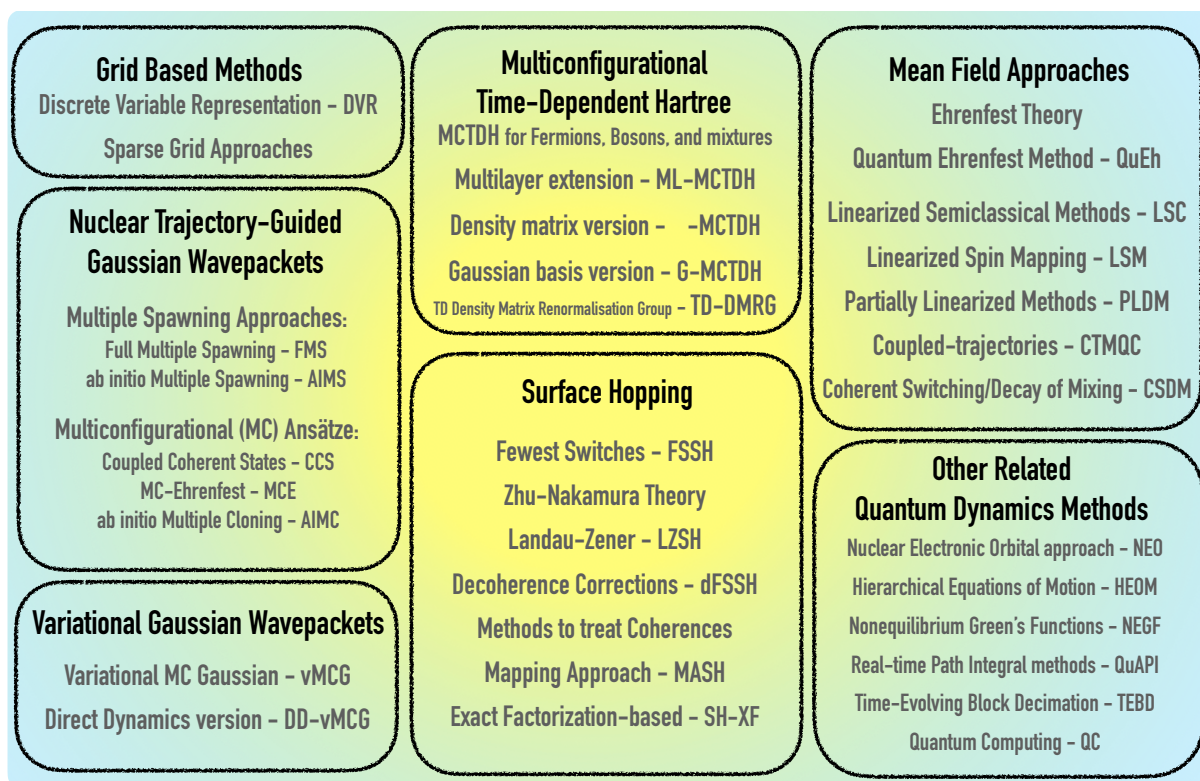


FIG. 2: Selected techniques from the range of NAMD methods that are relevant to establishing molecular benchmarks.

new tools for error-analysis which will allow developers of classical-computer algorithms to more accurately bound the errors of their simulations.

Figure 2 provides an overview of the classes of methods presented in this section. However, NAMD is a rapidly evolving field, with a wide variety of methods being constantly developed and improved, thus, it is challenging to provide an exhaustive list of all the methodologies and variations that have been introduced. Our goal is to offer an overview of the most common and widely used approaches. We also recognize that some methods on the list have primarily been used with low-dimensional model systems so far, but in principle, they could be adapted for realistic molecular systems. Figure 2 also gives an additional categorization of the methods by organizing them in “categories” highlighted by the boxes.

C. Electronic structure and representation of potential energy surfaces

The ingredient of an NAMD simulation that arguably plays a critical role on its outcome is the underlying electronic structure method, i.e., the level of theory at which the electronic energies, gradients, and couplings between electronic states are calculated – as highlighted in numerous studies.^{148,322–326} The impact of the electronic structure on the result of NAMD remains, however, challenging to predict. While very different PESs calculated from two different electronic-structure methods often lead to different excited-state dynamics,³²⁷ examples in the literature show that this correlation does not always hold: vastly different PESs can lead to similar dynamics, and similar PESs can lead to different results in NAMD.^{325,328–330} In any case, it is critical to ensure that the electronic-structure quantities for any benchmark system are obtained consistently to fairly compare the outcome of the NAMD simulations.

For the current standard practice of benchmarking on low-dimensional analytical models, ensuring consistency in electronic structure between different NAMD methods is a minor issue. A model Hamiltonian usually provides analytical expressions for energies and (diabatic) couplings, and perhaps even for gradients and for nonadiabatic couplings, making it simpler to ensure that different NAMD simulations are performed using the same electronic information.³³¹

In more realistic scenarios, NAMD is often carried out with electronic structure calculated on the fly (also called direct-dynamics) using trajectory-basis functions or quantum-classical techniques. This terminology means that any electronic-structure quantity for the dynamics is calculated locally, i.e., at the current nuclear configuration at that time step, rather than being precomputed or predefined over the full configuration space. In these cases, resolving the electronic structure problem becomes a critical step before establishing benchmark systems. To meaningfully compare different NAMD methodologies and softwares, it is essential to define the level of electronic-structure theory, ensuring that the underlying electronic-structure quantities remain consistent for all NAMD methods being compared.

An ideal electronic structure method should fulfill several criteria: 1) provide electronic energies, nuclear gradients, and any required couplings (e.g., nonadiabatic couplings, spin-orbit couplings, transition dipole moments), 2) describe all electronic states involved in the

dynamics with equal accuracy across the entire configuration space encountered during the dynamics, 3) be numerically robust, 4) capture the potential multiconfigurational character of electronic wavefunctions, and finally, 5) be computationally affordable.^{11,332}

Multiconfigurational methods³³³ like multiconfigurational self-consistent field (MCSCF), (state-averaged) complete active space self-consistent field (CASSCF), or complete active space configuration interaction (CASCI) are computationally expensive but include static correlation, often providing a qualitative correct picture of the PES. These methods allow the user to select the active space orbitals (occupied and unoccupied) that dominate the excited-state characters of the molecule of interest.³³⁴ Making an informed choice of active space, that is, making it as compact as possible while still remaining sufficiently stable throughout the dynamics, can offer a good compromise between cost and accuracy. However, in many cases a CASSCF or CASCI approach may not be accurate enough, due to the lack of dynamical correlation. This can be incorporated through the application of perturbation theory (e.g. via multi-state or single-state CASPT2)³³⁵ or with multireference methods (e.g. MRCIS or MRCISD).³³³ Such methods bring an improved description of the PESs, in particular when excited electronic states of different characters interact, but also increase substantially the cost of the calculation.³³⁵ Alternatively, scaled CASSCF methods (e.g. α -CASSCF,^{336,337}) introduce empirical corrections to state-averaged CASSCF, improving the description of PESs while maintaining computational efficiency, and have been successfully applied to study photochemical ring-opening and isomerization reactions.^{48,337,338} If structural rearrangements during the dynamics drive the molecule to regions of the PESs far from the Franck-Condon region, a single computationally-affordable active space might not provide enough flexibility to describe the photoproducts with the same accuracy as the initial molecule often leading to instabilities in the electronic structure. As a computationally efficient alternative, floating occupation molecular orbital complete active space configuration interaction (FOMO-CASCI)³³⁹ was also employed in combination with NAMD.³⁴⁰

For large molecular systems, linear-response (LR) time-dependent (TD) density functional theory (DFT) is a practical alternative due to its excellent balance between cost and accuracy. However, LR-TDDFT often suffers from limitations due to its approximations necessary for practical applications.³⁴¹ One of them is its reliance on the *adiabatic approximation*, which

hinders describing conical intersections with the electronic ground state, electronic states with double-excitation character, and charge-transfer transitions and Rydberg transitions; range-separated hybrids may help with these last two problems.^{342–352} These shortcomings may hamper the applicability of LR-TDDFT in NAMD simulations for systems exhibiting such features. In general, for any application to a molecular system, the choice of an adequate density functional may be challenging and requires careful benchmarking.^{353–355} Spin-flip variants of these methods exist,^{356,357} which can address some of these issues but often introduce spin contamination, except for spin-adapted spin-flip methods.^{358–361} Some of the aforementioned limitations of LR-TDDFT can be overcome using the ensemble-DFT-based approach which combines multireference methods within a density functional theory framework.³⁶² In a related approach, the mixed-reference spin-flip TDDFT (MRSF-TDDFT) technique³⁶³ has been proposed recently. At variance with LR-TDDFT, MRSF-TDDFT was shown to predict the correct topology of conical intersections with the ground state and to describe excited states with significant double excitation character^{364,365}. Hole–hole Tamm–Dancoff approximated (hh-TDA) density functional theory³⁶⁶ constitutes another variant of LR-TDDFT adequately describing conical intersections and combined with NAMD.³⁶⁷ Relatedly, particle-particle RPA can describe double excitations well,³⁶⁸ and, along with their oscillator strengths, related to their couplings, so can dressed frequency-dependent TDDFT.^{369,370}

We note that, in addition to conventional LR-TDDFT, real-time TDDFT (RT-TDDFT)³⁴¹ has also been used. In RT-TDDFT the electron density is propagated by integrating the time-dependent Kohn–Sham equations. RT-TDDFT (or more broadly, real-time electronic structure methods)³⁷¹ can be naturally coupled with Ehrenfest dynamics³⁷² to propagate nuclei classically with forces derived from a weighted average of all electronic states. However, in this approach there is no need for the explicit determination of individual electronic states and their couplings.

The algebraic diagrammatic correction to second order, ADC(2), is a wavefunction-based single-reference method that has been exploited for NAMD.^{373,374} This method, in its original implementation, possesses some limitations – it cannot describe conical intersections with the ground electronic state³²² and suffers from a systematic flaw for carbonyl-containing molecules.³⁷⁵ However, its overall accuracy and efficiency in describing excited PESs and

their coupling regions,³⁵⁰ as well as its reliability, makes it a key contender for the NAMD of medium-sized molecular systems. ADC methods are closely related to coupled cluster (CC) methods,³⁷⁶ which were historically not a popular choice for NAMD due to their intrinsic instabilities.^{374,377} However, recent CC implementations managed to resolve some of these problems, and have opened the door for CC-based NAMD simulations.^{378,379}

Semi-empirical multireference methods based on multiconfigurational configuration interaction wavefunctions built from FOMO-CI,^{38,224,380,381} particularly those reparameterized based on high level calculations, or the multi-reference configuration interaction based on the orthogonalization-corrected model Hamiltonian (MRCI/OMx),^{38,382} may offer an affordable alternative for describing conical intersections and complex electronic densities. If reparameterization has already been performed for the molecule of interest, these methods can be a suitable choice for benchmarking. They offer electronic structure quantities at a low cost, enabling long propagation times and large numbers of trajectories to be evolved.^{232,325,383–386}

The use of a given electronic-structure method to benchmark on-the-fly NAMD techniques is challenging, even if all the input parameters (and initial orbitals) are provided. Ideally, the same quantum-chemical code should be used to ensure a one-to-one comparison, as minor implementation details, such as convergence criteria or algorithmic differences, can impact the final results. To promote accessibility and broader participation of community members, benchmarks should preferably employ freely available or open-source quantum-chemical codes that are widely used within the NAMD community (e.g., OpenMolcas,³⁸⁷ Bagel,³⁸⁸ Orca,³⁸⁹ NWChem³⁹⁰, GAMESS³⁹¹, MNDO,³⁹² MOPAC-PI³⁷ or PySCF³⁹³). For many quantum-chemical methods, ensuring consistency between two calculations is relatively straightforward if one uses the same version of a given quantum-chemical code and the same input parameters. The case is harder for multireference and multiconfigurational methods, for which it is crucial to ensure that the very same initial molecular orbitals are included in the active space. This can be achieved by making sure that the starting orbitals are provided as a wavefunction file.

Grid-based methods for quantum dynamics require integrals to be performed over the entire nuclear configuration space. On-the-fly dynamics is hard to perform for such methods (even though recent forays in this direction have been made^{394,395}), therefore they often rely

on precomputed electronic structure quantities to fit or build analytical models. A very common approach for obtaining high-dimensional model potentials is to parameterize the PESs with vibronic coupling (VC) models, where the simplest form is the linear VC (LVC).³⁹⁶ An LVC model proposes to build a harmonic expansion of the diabatic states around the Franck-Condon region, using information from electronic-structure calculations, along with the linear coupling among these diabatic states. While VC models can accurately capture the ultrafast decay in NAMD, in their simplest LVC form, they are limited by their underlying harmonic approximation for describing the PESs and can only be applied to relatively rigid systems. Despite these shortcomings and when used on suitable systems, the LVC approach has recently gained popularity as a cost-efficient mean for comparing different trajectory-based approaches with accurate quantum dynamics results in high-dimensional systems.^{75,79,80,128,227,397,398} Here it is worth noting that recent advances in artificial intelligence and machine learning have significantly enhanced the accessibility of high-dimensional and anharmonic analytical potentials, reducing the computational cost of electronic structure and improving the fitting procedures,³⁹⁹ thus pushing NAMD simulations to longer time scales.^{400–402} In this context, benchmarking efforts will become even more critical in the future, particularly as machine learning based interatomic potentials (MLPs) evolve into widely adopted tools for NAMD. Well-defined benchmarks will be crucial not only for testing traditional electronic structure methods but also for providing a structured framework to assess how well MLPs reproduce reference electronic structure results within the same NAMD framework. Moreover, stable and reliable MLPs have the potential to revolutionize how NAMD methods are evaluated by enabling rapid and extensive testing, and facilitating the efficient exploration of the parameter space in existing NAMD techniques.

Finally, the use of fitted, analytical potentials versus on-the-fly dynamics for benchmarking needs to be addressed further. There is a clear and obvious advantage in developing models based on analytical potentials, as they directly allow quantum dynamics simulations to be performed and (near) numerically-exact solutions to be used as a reference. However, most common applications of NAMD focus on molecules for which a parametrization in full dimensionality is often inaccessible and that are therefore more easily described by on-the-fly simulations. Hence, NAMD benchmarks should be best conducted based on both

approaches: fitted/analytical potentials and on-the-fly dynamics. One should stress that in general, a NAMD simulation carried out on precomputed, fitted potentials in reduced dimensionality cannot be compared with NAMD conducted with direct dynamics in full dimensionality (see for instance a quantum dynamics study on a 2D model of retinal,⁶⁸ followed by fully-dimensional direct dynamics⁴⁰³ and experimental evidence⁴⁰⁴ demonstrating the necessity of additional degrees of freedom). This is because the configuration space that can be explored is predefined in a precomputed model, constraining the dynamics to a certain region of the nuclear configuration space. It might be useful, however, to conduct simulations on model potentials using on-the-fly NAMD simulation methodologies to provide a strict comparison of their performance against accurate grid-based methods.

A plausible solution to such an issue is to fit directly a global PES into analytical separable (sum of products or tree) form. In this way, it could be used by the whole range of NAMD techniques. From a purely algorithmic perspective, one can distinguish two classes of such fitting procedures: (i) those based on machine learning (ML) or neural networks (NN) and (ii) those relying on a functional ansatz related to tensor decomposition algorithms.

The first category includes methods based on machine learning or neural networks, such as single-layered Neural Networks with specific activation functions⁴⁰⁵ and Gaussian Process Regression with separable multidimensional kernels.⁴⁰⁶ The second category involves methods exploiting PES smoothness under separable form constraints, including Smolyak interpolation scheme with non-direct product basis⁴⁰⁷ and the Finite Basis Representation (FBR) family of PES representations.^{408–410} FBR models can be optimized from scattered reference data and have been applied to various physico/chemical processes, including vibrational problems (6D/9D),^{408,409} reactive scattering processes (13D/15D/72D),^{409,411} and nonadiabatic dynamical problems (12D).

D. Initial conditions for the dynamics

Any NAMD simulation requires a definition of the initial state of the molecule before being excited by light or before the dynamics is started. Therefore, a critical aspect to discuss is the nature of this initial molecular state for the molecule of interest, be that the ground state

of the molecule or the state directly generated by the photoexcitation process.⁴¹²

Following the time-dependent perturbation theory to first order for a system with two electronic states,⁴ one can show that the first-order contribution to the molecular state immediately after excitation by an infinitely short pulse (a δ -pulse) is simply the initial ground-state nuclear wavefunction (multiplied by the transition dipole moment between the ground and the excited electronic state). In other words, if the molecule is excited by a very short pulse, a commonly accepted approximation is to simply project the ground-state nuclear wavefunction onto the desired excited electronic state.⁴¹³ This approximation, often referred to as the sudden, or vertical, excitation, dramatically simplifies the preparation of initial conditions for NAMD, as it neglects the time duration of the excitation process (e.g. an experimental laser pulse) and the precise nature of the molecular state formed upon photoexcitation.

Within this sudden excitation, the initialization of a quantum dynamics simulation only requires the nuclear wavefunction associated with the ground electronic state for the system of interest, often taken as the ground vibrational state for all modes considered. This nuclear wavefunction can be obtained by imaginary-time propagation or, for potential energy surfaces invoking a harmonic approximation, simply from a Gaussian nuclear wavefunction. Similarly, the most commonly employed strategy for trajectory-based methods consists first of sampling an approximate ground-state distribution. The harmonic Wigner distribution, constructed from the molecular equilibrium geometry and its harmonic normal modes, is often used to sample representative initial conditions (nuclear momenta and positions).^{10,412} Once the initial ground-state nuclear wavefunction (quantum dynamics methods) or ground-state nuclear momenta + positions (trajectory-based methods) are acquired, they can be projected onto the desired excited electronic state to begin the NAMD.

While the protocol described above is the most commonly employed strategy to initialize a NAMD simulation, it relies on a series of approximations,⁴¹⁴ namely that (i) the molecule is in its electronic and vibrational ground state before photoexcitation and (ii) that the laser pulse employed is infinitely short (or at least short enough for its bandwidth to overlap with all necessary vibrational states in the excited electronic state for a projection of the ground-state nuclear wavefunction), meaning that a perfect nuclear wavepacket is generated in the excited electronic state(s) of interest. We note that the initialization of quantum

dynamics simulations also often relies on the Condon approximation, that is, the transition dipole moment does not depend significantly on the nuclear geometries under the initial wavepacket. Nevertheless, care must be taken since cases of strong violation of Condon approximation have been reported.⁴¹⁵

For floppy molecules with multiple dihedral angles and low rotational barriers, harmonic Wigner distributions are not suitable for sampling initial conditions. Improvements in the generation of the ground-state probability density can be obtained for trajectory-based methods by using *ab initio* molecular dynamics (AIMD). Initial positions and momenta can be obtained from long, equilibrated ground-state molecular dynamics simulations, providing a more accurate representation of the nuclear phase space. Incorporating zero-point energy (ZPE) in the dynamics requires the use of a quantum thermostat (QT),^{416–418} as a regular 300K AIMD would lead to molecular distributions that are too narrow in comparison to their ZPE equivalent.⁴¹⁹ QT-AIMD can overcome some limitations of the harmonic Wigner sampling, in particular for flexible molecules with low-frequency (anharmonic) vibrational modes. Using the harmonic Wigner sampling for molecules with photoactive low-energy modes can lead to severe artifacts in the ensuing excited-state dynamics – an issue fixed with the QT-AIMD.⁴²⁰

Moving beyond the sudden excitation requires a more careful inclusion of the external electric field in the simulation, aiming for more robust comparisons with experiments. Most methods for NAMD have been extended to incorporate photoexcitation triggered by an explicit laser pulse (e.g., Refs. 47,153,291,292,421–423). This strategy, though, does appear to stretch the approximations of methods like surface hopping for longer laser pulses,^{193,424,425} and modifications of surface hopping based on Floquet theory were presented in the literature.^{426,427} Different works have discussed photoexcitation beyond laser pulses, including incoherent sunlight^{413,428,429} or a periodic drive,⁴³⁰ in NAMD. Building the effect of a laser pulse within the initial conditions was also suggested.^{118,431,432} Furthermore, upon initial photoexcitation by a laser pulse, a group of electronic states may be excited and the subsequent dynamics can differ depending on whether the system evolves from a superposition of states (pure) or a mixed ensemble.⁴³³

Another issue that needs to be addressed in the context of benchmarking different families of methods for NAMD is the representation of the electronic states. In conventional

trajectory-based methods, the nuclear dynamics is usually performed by invoking electronic properties in the adiabatic representation. On the other hand, quantum dynamics methods often rely on the – more convenient – diabatic representation to avoid encountering singularities of the nonadiabatic couplings at conical intersections. Therefore, in the initialization of a quantum dynamics simulation, the ground-state nuclear wavefunction needs to be projected onto a given diabatic electronic state. For a proper assessment of trajectory-based methods against quantum dynamics results, the initial electronic diabatic state needs to be translated appropriately into an adiabatic state or a linear combination of adiabatic states when the trajectory-based simulation is performed with methods employing the adiabatic representation.

E. Observables and properties

Benchmarking NAMD methods faces the challenge of identifying a unique, clearly defined, and quantifiable “result”. In contrast, electronic structure benchmarks are based on well-defined numerical values such as electronic energies, or optimized geometries. The outcome of a NAMD simulation involves a time-dependent molecular wavefunction, with the desired results and properties depending on the specific system and phenomenon under study. Nevertheless, we aim to identify key properties and observables that can facilitate both qualitative and quantitative comparisons across different methods for NAMD.

In this section, we use the term *observable* in the physical sense, namely a quantity that is directly determinable from an experiment and is, therefore, independent of the theoretical representation used in the calculations as it corresponds to the expectation value of an operator. By contrast, we refer to a *property* as a quantity that may be used to interpret the simulated dynamics or an experimental measurement, but that cannot be directly measured. Below, we discuss how observables and properties can be selected for benchmarks.

For the purpose of benchmarking, observables and properties need to be selected such that different methods can be compared fairly, following several criteria. First, it is desirable that the considered observables or properties can be computed by every NAMD method under investigation. For instance, the operators involved in the calculation of expectation

values should ideally have a relatively simple form to allow for the computation of high-dimensional integrals required for the quantum dynamics approaches. Similarly, it should be possible to calculate the observables directly as expectation values by reconstructing the nuclear wavefunctions. For trajectory-based methods, the observables and the properties are often calculated as trajectory averages, with all trajectories having equal weight (or different weight depending on method).

Second, it is also necessary to choose a set of observables and properties that describe all aspects of the dynamical processes at play. For NAMD, this normally requires the consideration of both electronic and nuclear degrees of freedom. Different methods are unlikely to reproduce each type of observable or property equally well, so having the most diverse observable set is important for a comprehensive comparison between methods.

Finally, NAMD methods employ different electronic representations. Some electronic properties, such as electronic populations may only be accessible in or dependent on a given representation and shall be used “with care” for comparisons of methods. One way to avoid this issue is to consider representation-independent electronic properties and observables, such as optical spectra.

To make a tangible example of the observables and properties that can be of interest for understanding the processes taking place during a photochemical reaction, let us discuss Figure 3. The *absorption* of light by an organic molecule in its vibrational and electronic ground state, S_0 (violet Gaussian on the left) produces a photoexcited nuclear wavepacket in a singlet excited electronic state, here S_1 (green Gaussian on the left). The photoexcited molecule relaxes non-radiatively via *internal conversion* from S_1 to S_0 , transferring the population to the electronic ground state and accessing the configurations of the various *photoproducts* (violet Gaussians in the center). The remaining contribution to the nuclear wavepacket in S_1 can be transferred non-radiatively to a triplet state (blue Gaussians in the center), here T_n , by *intersystem crossing*. Finally, the S_1 and the T_n wavepackets can ultimately relax radiatively to the ground state (violet Gaussians on the right) via *fluorescence* and *phosphorescence*.

Based on this schematic representation of a photochemical reaction, the following properties could provide a useful way of tracking the important aspects of the dynamics. The relaxation of the photoexcited system to a lower energy electronic state can be followed

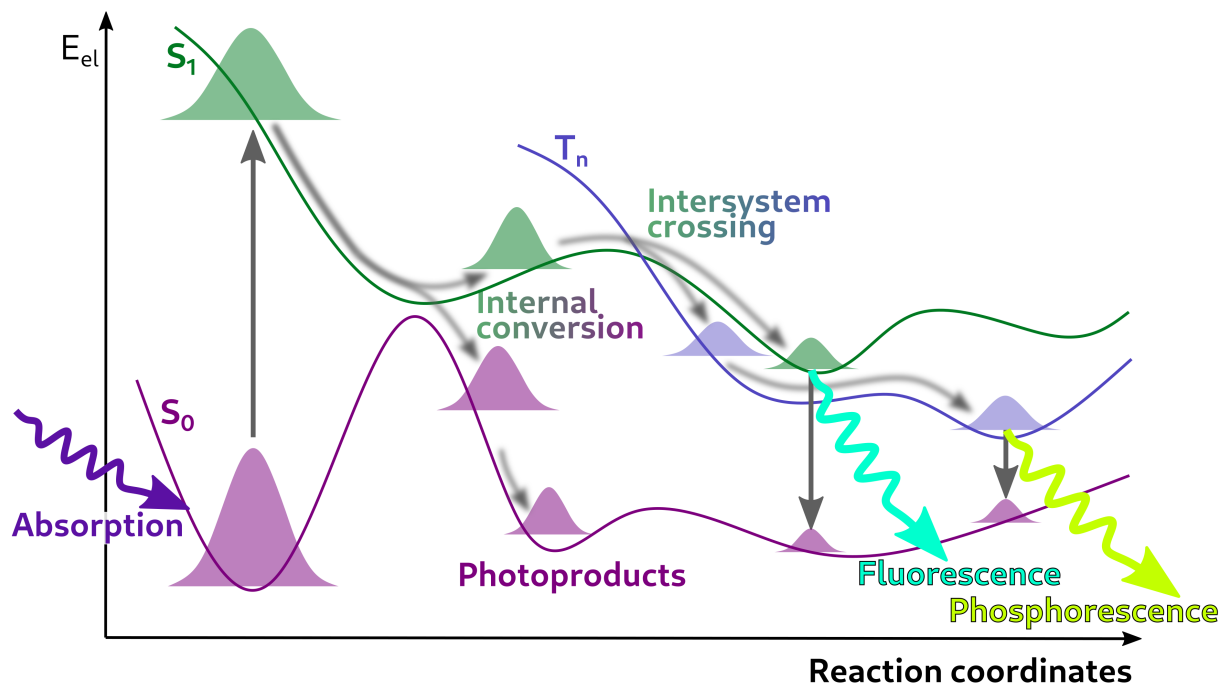


FIG. 3: Processes that can occur upon photoexcitation of a molecular system.

via the electronic (adiabatic and diabatic) populations. While easily accessible, electronic populations are a representation-dependent quantity and therefore, excited state lifetimes in different spin multiplicities should additionally be linked to an observable that is sensitive to them. Calculating the time-dependence of the energy gap distribution between two appropriate electronic PESs, as probed by transient-absorption spectroscopy, would additionally quantify the motion of the nuclear wavepacket away from the conical intersection seams towards a stable minimum energy geometry on the lower-energy surface and give a quantitative picture of the electronic relaxation, in particular for NRR. For molecular systems consisting of donor and acceptor moieties, transient exciton localization can be tracked, enabling the study of intramolecular energy transfer between different chromophoric units.^{434,435} Finally, an important aspect of photochemical processes is the formation of photoproducts. This is particularly important for characterizing ISO, DIS, and ESIPT phenomena, and can be probed via the associated quantum yields, preferably computed for different excitation wavelengths. For ESIPT-related processes, it would be particularly interesting to study the mechanistic details of the proton transfer, i.e., whether it is stepwise or concerted. This can be deduced

from the time-evolved nuclear probability distribution of the transferring proton or the kinetic isotope effect,⁴³⁶ for example.

To properly compare with experiments, it is essential to consider various spectroscopic observables that can be used to interrogate photochemical and photophysical phenomena.^{432,437–442} Optical transient absorption,^{443–446} time-resolved X-ray absorption,⁴⁴⁷ 2D electronic spectroscopy^{442,448} and time-resolved photoelectron spectroscopy^{449,450} are several complementary techniques that directly probe the dynamical changes in electronic structure associated with a particular process. All of these techniques can, in principle, distinguish between states of different spin multiplicity,^{451–453} and the method of choice may depend on whether the associated valence or core excitation spectra or the photoionization cross-sections provide the greatest contrast between the molecular species and states of interest. In particular, 2D electronic spectroscopy is an ultrafast optical technique capable of providing critical insights into coherence, which signifies the simultaneous evolution of electronic and vibrational dynamics in complex natural and synthetic systems⁴⁵⁴ Coherence refers to the in-phase evolution of specific degrees of freedom and, in quantum mechanics, is formally described by the off-diagonal elements of the density matrix, encompassing both electronic and vibrational components.⁴⁵⁵ Capturing such coherent phenomena in NAMD simulations^{455,456} remains a significant challenge due to the need for consistent and accurate propagation of both electronic and nuclear degrees of freedom at the surface crossings.

One advantage offered by time-resolved photoelectron spectroscopy is that processes like electronic population transfer involving an optically-dark electronic state can be directly observed.⁴⁴⁹ Recently, attosecond transient absorption spectroscopy⁴⁵⁷ and multiphoton ionization⁴⁵⁸ have been used to measure and distinguish adiabatic and non-adiabatic effects in the evolution of electronic coherences. Finally, time-resolved X-ray diffraction^{459–461} and ultrafast electron diffraction^{462,463} spectroscopies provide a useful way of directly probing the nuclear rearrangements of molecules in real-time and can be highlighted as effective experimental tools for investigating ISO, DIS and ESIPT phenomena. In particular, ultrafast electron diffraction has shown sufficient sensitivity to monitor the motion of light atoms like hydrogen in the context of photodissociation.⁴⁶⁴ In general, scattering experiments are beginning to be employed to detect information beyond structural dynamics, such as electronic

populations⁵³ or indeed the rearrangement of electrons during a reaction.^{465,466} This indicates that such experiments stand to provide comprehensive and complete information about the evolution of the molecular wavepacket.

F. The role of experiments in benchmarking nonadiabatic molecular dynamics

Experimental observables are often regarded as the “ultimate” data for providing a reference for results obtained from quantum chemical methods. Spectroscopic techniques seem especially well-suited for providing this due to their ability to reveal quantum state information on the target system. However, there are a number of challenges when drawing comparisons between experiment and theory that need to be considered, particularly when benchmarking NAMD simulations.

Ultrafast spectroscopies are reasonably young in comparison to their static counterparts, with the earliest time-resolved optical absorption measurements being performed in the 1970s.⁴⁶⁷ Many ultrafast techniques, such as time-resolved X-ray absorption, are even newer,^{468–470} which poses a number of further challenges for using this experimental data as a reference in the benchmark of NAMD. The first of these is simply the quantity of experimental data available. While ultrafast optical techniques have seen significant hardware developments,⁴⁷¹ such that “all-in-one” laser and spectrometer systems are now commercially available, ultrafast optical techniques are nevertheless nowhere near as ubiquitous as standard UV-vis absorption, which is now even being performed with smartphones.^{472,473}

A more serious issue for benchmarking is the reproducibility and reliability of the experimental data, coupled with the quality of the data reporting. Although chemists and physicists are generally among the least concerned about a “reproducibility crisis” in science,⁴⁷⁴ there have been recent reviews highlighting how, for X-ray photoelectron spectroscopy (XPS), there is a non-trivial number of papers reporting experimental data with minor errors in the collection process and a much more significant number with major issues associated with the subsequent peak fitting and data analysis procedures.⁴⁷⁵ Growing concerns about the reproducibility problem in XPS have prompted journals⁴⁷⁶ and the community^{477,478} to produce documents on best practices for data collection, reporting, and analysis in order to try and

ensure consistent standards are maintained.

No such systematic analysis exists for the ultrafast literature, and many techniques are still sufficiently novel and challenging to perform. Hence, the research focus is still far from prioritizing systematic characterization studies. Even a brief survey of the literature, though, will reveal many inconsistencies and inadequacies in what experimental parameters are reported. For example, many papers do not report how time-zero (where the pump and probe pulses are temporally overlapping) is established or whether any wavelength calibrations for detectors have been performed and how. Often, only representative pulse parameters for the pump and probe pulses, such as pulse energies, temporal duration and central wavelengths, are reported, and no spectral information provided. While not all measurements are particularly sensitive to the excitation conditions, without this information, it becomes difficult to simulate the exact experimental conditions in excited-state dynamics simulations, particularly when an explicit pulse is included. While there are often reasons for not reporting all of this information, it is clear that it would be highly beneficial to specifically design experiments for use in theoretical benchmarking studies, where a different approach to data collection is required than for a standard photophysical experiment.⁴⁷⁹

It is also very important to make a clear distinction between what is the true experimental signal of measurement and what are parameters extracted from a fitting or modeling of the experimental data. For example, ultrafast spectroscopies are used to extract “lifetime” information, but the reported lifetimes are normally extracted from some kind of kinetic model with an inherent number of assumptions,⁴⁸⁰ although there are a few notable exceptions.^{481,482} As explored more extensively in a recent review,⁴³⁹ the same change in an experimental observable can arise from different physical mechanisms, and it is important to note that most spectroscopies are not directly sensitive to the population dynamics, but rather to the population dynamics convoluted with a transition probability. Evaluating the trustworthiness of models and fits can be as challenging as assessing the quality of experimental data and a difficult task without direct engagement with experts.

III. OUTLOOK – A ROADMAP FOR MOLECULAR BENCHMARKS IN NAMD

The multifaceted nature of NAMD has, to date, hindered systematic efforts toward designing molecular benchmarks, with only a few notable studies making headway.^{73,74,78} The intention behind this Perspective is to narrow down the multitude of available choices of “benchmarkable phenomena” and encourage collaborative efforts within the NAMD community towards these goals. This Section summarizes key considerations for developing molecular benchmarks and presents an executive outline for their implementation. The steps discussed in this Perspective form the *roadmap* towards a community-driven development of benchmarks for NAMD methods (Figure 4).

First, we briefly overview key insights from the workshop in Paris,⁸⁷ which established foundational ideas for this initiative. One challenge identified by the community of NAMD users and developers is the breadth and complexity of NAMD simulations, demanding careful selection criteria to balance feasibility with scientific relevance. To ensure meaningful assessments, molecular benchmarks are meant to capture realistic nonadiabatic phenomena while minimizing reliance on model potentials with reduced dimensionality. The emphasis on realistic processes – those measurable in experiments – reflects the goal of creating benchmarks that will increase confidence in the predictive power of current theoretical developments. We have identified four relevant, although not exhaustive, groups of molecular phenomena for detailed exploration: ISO, DIS, NRR and ESIPT. They are connected to a range of observables, which will be defined early on but whose calculation represents almost the final step of the roadmap (Figure 4). Prioritizing direct calculations of molecular observables reduces the influence of different PES representations, ensuring that benchmarks maintain scientific relevance by predicting measurable quantities.

As discussed above, this relates to the question about the role of experimental data in benchmarking theoretical methods. While reproducing experimental predictions remains a key objective for the community, the direct prediction of experimental observables should currently be viewed as a goal rather than a strategy for benchmarking. Confidently bridging the gap between experiment and theory requires active collaborations from both sides in order to drive the development of all aspects and ingredients of NAMD, and as such, remains an on-

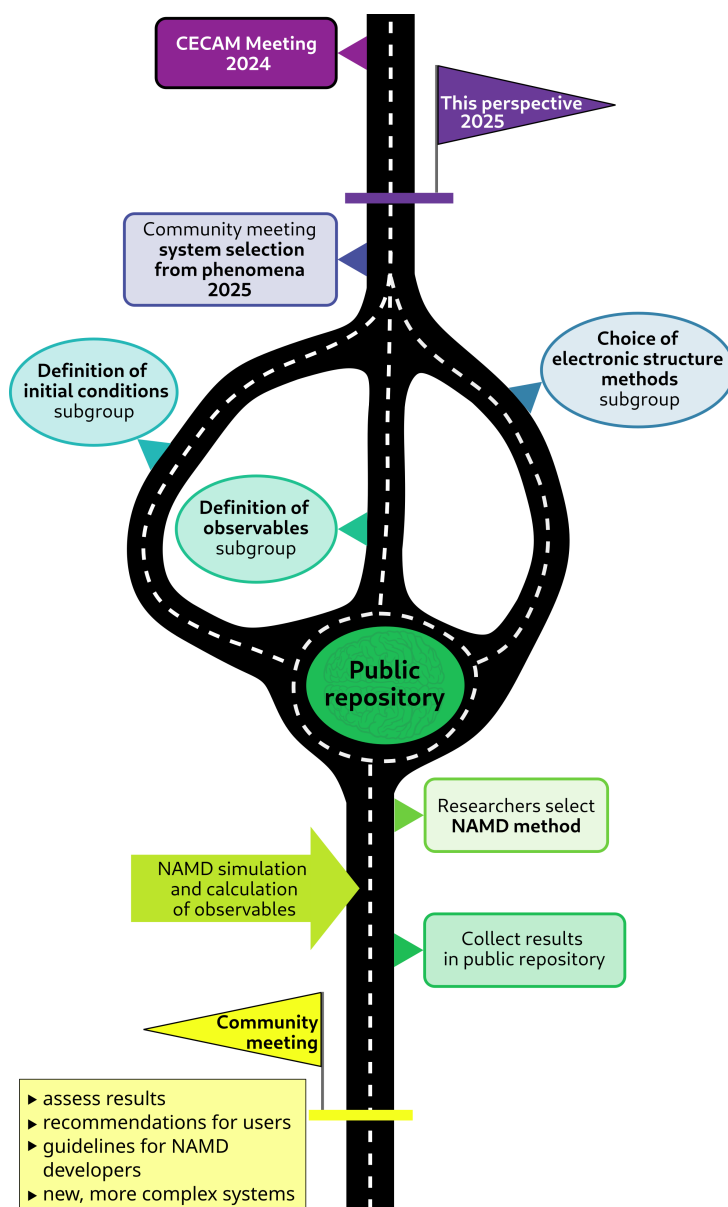


FIG. 4: Schematic representation of the steps discussed in this *roadmap* towards the creation of a benchmark set for NAMD methods and the future steps planned by the community.

going area of research. However, this should not impede the evaluation of NAMD methods in the context of benchmarking. Therefore, we currently do not recommend the systematic assessment of theoretical results by direct comparison with experimental measurements unless the same experimental observable is calculated. Even then, caution is required. In trajectory-based NAMD methods, observables such as photoelectron spectra may be repro-

duced with comparatively few trajectories,^{483,484} while branching ratios require more.¹⁴⁸ As a consequence, it may be misleading to judge convergence and overall accuracy on the basis of a single observable. In addition, in Section II F, we focused our attention on the role of ultrafast spectroscopy in the context of benchmarking NAMD. Alternative and complementary experimental techniques, such as time-resolved mass spectrometry, can provide insights into ultrafast structural dynamics with femtosecond time resolution^{485–489} (thus, having the potential to serve as a high-throughput data source for nonadiabatic simulation benchmarks), but accurate simulations of ultrafast processes in gas-phase ion (as compared to neutral) chemistry remain relatively underexplored.^{490–492}

Molecular benchmarking should rather focus on comparing the theoretical approximations directly with exact or nearly exact solutions from theory, an approach that allows full control over external parameters and ensures a fair comparison. Recognizing that nearly exact solutions may not always be available or feasible to estimate, we refer to the concept of *benchmarking by comparison*. This involves comparing different methods without an absolute reference point. Even in such cases, we can establish a theoretical best estimate (TBE): a prediction from a method that provides the highest level of accuracy in treating nonadiabatic effects in that system. In this context, it is crucial that NAMD calculations are properly converged to the limit of their nuclear basis set or number of trajectories to ensure reliable comparisons. It is worth noting that TBEs have also been used in electronic structure benchmarks and have been updated progressively over time.^{60,61,493}

Using consistent electronic structure methods and equivalent initial conditions for comparing NAMD methods is generally less contentious as an idea, but the practical implementation poses challenges. We have thoroughly discussed these complexities to address all underlying nuances. The systems of interest should avoid prohibitively expensive electronic structure, so as to allow the sufficient convergence of dynamics results, especially for the more computationally demanding approaches. Full dimensional LVC models, which require modest computational resources, may serve as a suitable testing ground for a wide range of methods, particularly in cases like internal conversion and intersystem crossing in NRR, which do not necessarily involve large-amplitude motions (as in ISO) or bond breaking (as in DIS and ESIPT). The exploration of ISO, DIS, and ESIPT phenomena requires more

efforts on the accurate electronic structure evaluation. This would involve selecting electronic structure methods that are affordable, numerically stable, and widely accessible to the community through preferably software packages that are free of charge for the scientific community. Alternatively, one can take advantage of analytical potentials that have been previously obtained and used in NAMD calculations, keeping in mind that it is sometimes not straightforward to transfer a given analytical expressions into the specific form, as for instance a sum-of-products form.

In the generation of initial conditions, using simple approximations like the sudden approximation and the use of a harmonic approximation to describe the ground-state potential could mitigate the complications with initiating different NAMD methods. Nonetheless, translation between the adiabatic and diabatic representations of electronic states requires more meticulous considerations.

Research activities that are currently prioritized involve testing preliminary molecular systems and phenomena selected from a short list with strong potential as effective benchmarks. In this context, “system” refers not only to the molecule itself but also to its electronic structure representation and the possibility of calculating relevant observables. Some of the molecular systems under investigation leverage the advantages of vibronic coupling potentials. At the same time, others already have available pre-constructed PESs that would also be suitable for efficient on-the-fly simulations. Following initial scrutiny, the most promising systems will be selected for benchmarking.

Another ongoing effort involves the creation of a common online repository. Making research data openly available encourages wide participation by researchers from the field, promoting transparency, accessibility, and collaboration. An accessible online repository will allow storage of essential data such as input files, all information relevant for reproducibility and the collection of the results of the benchmarking. Here, the utilization of data science and machine learning techniques, which are rapidly advancing and increasingly permeating chemical and materials sciences, can play a critical role in supporting and maintaining data repositories. These approaches enable efficient data curation, analysis, and debugging, and are especially valuable for integrating data of varying fidelity and origin, thereby enhancing the robustness and usability of complex datasets.⁴⁹⁴

Once the initial set of benchmark systems is finalized and agreed upon by community members, a common set of initial conditions will be established and made available in the repository. Hereby, we recommend entrusting the preparation of initial conditions to a single dedicated research team, making sure that all types of NAMD methods are covered comprehensively. At this stage, establishing standardized input and output data formats is also anticipated to enhance the broader usability of the benchmark set. An appropriate electronic structure method, along with freely available software, will be selected for on-the-fly dynamics. All necessary quantities, input data, and (if required) initial wavefunction files will be incorporated into the repository. For methods that require analytical potentials, these will either be sourced from existing literature or parametrized and shared in the repository. Additionally, a set of relevant observables will be identified for each system, chosen to capture and represent the key aspects of nuclear and electronic dynamics. Comprehensive instructions and materials detailing the calculation of these observables will be provided to ensure consistent evaluation across all NAMD simulations. Additionally, it could be useful to standardize the tools used for post-processing and analysis of NAMD data. Selecting a dedicated Python framework⁴⁹⁵ (or equivalent) would ensure consistency in analyzing observables, trajectory-based statistics, and error quantification, streamlining testing workflows, and promoting transparency across different benchmarking studies. The selection of initial conditions, of the electronic structure method and of the relevant observables will be performed in parallel, as indicated in the roadmap of Figure 4, ultimately converging in the creation of a repository.

Using the system information gathered in the repository, all researchers interested in participating in the benchmarking effort can test their NAMD methodologies and software on the designated test-set. This benchmarking initiative aims to engage researchers with diverse expertise, encompassing the full range of NAMD methods, from trajectory-based approaches to quantum wavepacket-propagation techniques and quantum-computing approaches. This diversity is particularly desired in the realm of *benchmarking by comparison*, as each method should ideally be leveraged to its utmost potential, using the optimal choice of parameters associated with best practices for each NAMD approach. The calculated results, along with the best practice procedures, are expected to be published in conventional research articles

as well as the data shared through the repository – ensuring that benchmarks remain valuable long-term resources. The benchmarking results will be evaluated by the community members during a collective meeting. Based on the data, the goal is to assess the quality of different NAMD approaches for various molecular groups. Additionally, guidelines will be introduced for future NAMD method development, defining standardized tests and expected results to evaluate the performance of new methods.

In the long run, we foresee a continuous refinement of molecular benchmarks aligned with the ongoing advancements in the field that invariably present new challenges. More complex features will be gradually introduced, and likewise, benchmarks will be expanded to include complex systems and phenomena. This covers, for example, molecules in realistic environments (such as solvents, surfaces and materials),^{496–500} an explicit treatment of light-matter interactions,⁴¹⁴ high density of states, and long dynamics. The utilization of machine learning approaches in these efforts has shown great promise in significantly reducing computational cost without compromising numerical accuracy, as clearly demonstrated by early studies in the field.^{402,501,502} Finally, a synergistic approach that integrates theory and experiment (within the context of benchmarking) will inevitably emerge as a key task for the broader NAMD community.

Alongside this *roadmap*, which serves as an initial effort to disseminate our thoughts about benchmarking methods for NAMD, we aim at promoting the broader participation from community members beyond the present core group of contributors, as well as organizing regular meetings and progress reports to ensure the successful accomplishment of the plan.

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REFERENCES

- ¹M. Born and R. Oppenheimer, "Zur Quantentheorie der Molekeln," *Ann. Phys.*, vol. 84, pp. 457–484, 1927.

- ²W. Domcke, D. R. Yarkony, and H. Köppel, *Conical Intersections: Electronic Structure, Dynamics & Spectroscopy*, vol. 15. World Scientific, 2004.
- ³M. Baer, *Beyond Born-Oppenheimer: Electronic Nonadiabatic Coupling Terms and Conical Intersections*. Wiley Interscience, 2006.
- ⁴D. J. Tannor, *Introduction to Quantum Mechanics: A Time-Dependent Perspective*. University Science Books, 2007.
- ⁵F. Gatti, B. Lasorne, H.-D. Meyer, and A. Nauts, *Applications of Quantum Dynamics in Chemistry*. Springer, 2017.
- ⁶L. González and R. Lindh, *Quantum Chemistry and Dynamics of Excited States: Methods and Applications*. Wiley, 2021.
- ⁷H. Nakamura, *Introduction to Nonadiabatic Dynamics*. World Scientific, 2019.
- ⁸H. Nakamura, *Nonadiabatic Transition: Concepts, Basic Theories and Applications*. World Scientific, 2012.
- ⁹J. C. Tully, "Perspective: Nonadiabatic dynamics theory," *J. Chem. Phys.*, vol. 137, p. 22A301, 2012.
- ¹⁰R. Crespo-Otero and M. Barbatti, "Recent Advances and Perspectives on Nonadiabatic Mixed Quantum–Classical Dynamics," *Chem. Rev.*, vol. 118, pp. 7026–7068, 2018.
- ¹¹B. F. E. Curchod and T. J. Martínez, "Ab Initio Nonadiabatic Quantum Molecular Dynamics," *Chem. Rev.*, vol. 118, pp. 3305–3336, 2018.
- ¹²G. A. Worth and L. S. Cederbaum, "Beyond Born-Oppenheimer: Molecular Dynamics Through a Conical Intersection," *Annu. Rev. Phys. Chem.*, vol. 55, pp. 127–158, 2004.
- ¹³S. Mai and L. González, "Molecular Photochemistry: Recent Developments in Theory," *Angew. Chem. Int. Ed.*, vol. 59, pp. 16832–16846, 2020.
- ¹⁴L.-M. Ibele, E. Sangiogo Gil, E. Villaseco Arribas, and F. Agostini, "Simulations of photoinduced processes with the exact factorization: state of the art and perspectives," *Phys. Chem. Chem. Phys.*, vol. 26, pp. 26693–26718, 2024.
- ¹⁵J. E. Subotnik, A. Jain, B. Landry, A. Petit, W. Ouyang, and N. Bellonzi, "Understanding the Surface Hopping View of Electronic Transitions and Decoherence," *Annu. Rev. Phys. Chem.*, vol. 67, pp. 387–417, 2016.
- ¹⁶G. W. Richings, I. Polyak, K. E. Spinlove, G. A. Worth, I. Burghardt, and B. Lasorne,

- "Quantum dynamics simulations using Gaussian wavepackets: the vMCG method," *Int. Rev. Phys. Chem.*, vol. 34, pp. 269–308, 2015.
- ¹⁷O. V. Prezhdo, "Modeling Non-adiabatic Dynamics in Nanoscale and Condensed Matter Systems," *Acc. Chem. Res.*, vol. 54, pp. 4239–4249, 2021.
- ¹⁸B. Lasorne, G. A. Worth, and M. A. Robb, "Excited-state dynamics," *WIREs Comput. Mol. Sci.*, vol. 1, pp. 460–475, 2011.
- ¹⁹T. R. Nelson, A. J. White, J. A. Bjorggaard, A. E. Sifain, Y. Zhang, B. Nebgen, S. Fernandez-Alberti, D. Mozyrsky, A. E. Roitberg, and S. Tretiak, "Non-adiabatic Excited-State Molecular Dynamics: Theory and Applications for Modeling Photophysics in Extended Molecular Materials," *Chem. Rev.*, vol. 120, pp. 2215–2287, 2020.
- ²⁰F. Agostini and B. F. E. Curchod, "Different flavors of nonadiabatic molecular dynamics," *WIREs Comput. Mol. Sci.*, vol. 9, p. e1417, 2019.
- ²¹S. Nanbu, T. Ishida, and H. Nakamura, "Future perspectives of nonadiabatic chemical dynamics," *Chem. Sci.*, vol. 1, pp. 663–674, 2010.
- ²²A. H. Zewail, "Laser Femtochemistry," *Science*, vol. 242, pp. 1645–1653, 1988.
- ²³A. H. Zewail, "Femtochemistry: Atomic-Scale Dynamics of the Chemical Bond," *J. Phys. Chem. A*, vol. 104, pp. 5660–5694, 2000.
- ²⁴A. Stolow, A. E. Bragg, and D. M. Neumark, "Femtosecond Time-Resolved Photoelectron Spectroscopy," *Chem. Rev.*, vol. 104, pp. 1719–1758, 2004.
- ²⁵M. Kowalewski, B. P. Fingerhut, K. E. Dorfman, K. Bennett, and S. Mukamel, "Simulating Coherent Multidimensional Spectroscopy of Nonadiabatic Molecular Processes: From the Infrared to the X-ray Regime," *Chem. Rev.*, vol. 117, pp. 12165–12226, 2017.
- ²⁶M. Nisoli, P. Decleva, F. Calegari, A. Palacios, and F. Martín, "Attosecond Electron Dynamics in Molecules," *Chem. Rev.*, vol. 117, pp. 10760–10825, 2017.
- ²⁷E. T. J. Nibbering, H. Fidder, and E. Pines, "Ultrafast Chemistry: Using Time-Resolved Vibrational Spectroscopy for Interrogation of Structural Dynamics," *Annu. Rev. Phys. Chem.*, vol. 56, pp. 337–367, 2005.
- ²⁸C. Bressler and M. Chergui, "Ultrafast X-ray Absorption Spectroscopy," *Chem. Rev.*, vol. 104, pp. 1781–1812, 2004.
- ²⁹C. Bressler and M. Chergui, "Molecular Structural Dynamics Probed by Ultrafast X-ray

- Absorption Spectroscopy," *Annu. Rev. Phys. Chem.*, vol. 61, pp. 263–282, 2010.
- ³⁰M. Maiuri, M. Garavelli, and G. Cerullo, "Ultrafast Spectroscopy: State of the Art and Open Challenges," *J. Am. Chem. Soc.*, vol. 142, pp. 3–15, 2019.
- ³¹P. M. Kraus, M. Zürch, S. K. Cushing, D. M. Neumark, and S. R. Leone, "The ultrafast X-ray spectroscopic revolution in chemical dynamics," *Nat. Rev. Chem.*, vol. 2, pp. 82–94, 2018.
- ³²G. A. Worth, M. H. Beck, A. Jäckle, and H.-D. Meyer, "The MCTDH Package, Version 8.2, (2000). H.-D. Meyer, Version 8.3 (2002), Version 8.4 (2007). O. Vendrell and H.-D. Meyer, Version 8.5 (2013)." <http://mctdh.uni-hd.de>.
- ³³M. Barbatti, M. Bondanza, R. Crespo-Otero, B. Demoulin, P. O. Dral, G. Granucci, F. Kossoski, H. Lischka, B. Mennucci, Mukherjee, *et al.*, "Newton-X Platform: New Software Developments for Surface Hopping and Nuclear Ensembles," *J. Chem. Theory Comput.*, vol. 18, pp. 6851–6865, 2022.
- ³⁴S. Mai, P. Marquetand, and L. González, "Nonadiabatic dynamics: The SHARC approach," *WIREs Comput. Mol. Sci.*, vol. 8, p. e1370, 2018.
- ³⁵M. Shakiba, B. Smith, W. Li, M. Dutra, A. Jain, X. Sun, S. Garashchuk, and A. Akimov, "Libra: A modular software library for quantum nonadiabatic dynamics," *Softw. Impacts*, vol. 14, p. 100445, 2022.
- ³⁶G. A. Worth, "QUANTICS: A general purpose package for quantum molecular dynamics simulations," *Comput. Phys. Commun.*, vol. 248, p. 107040, 2020.
- ³⁷G. Granucci, M. Persico, D. Accomasso, E. Sangiogo Gil, S. Corni, J. Fregoni, T. Laino, M. Tesi, and A. Toniolo, "MOPAC-PI: a program for excited state dynamics simulations based on nonadiabatic trajectories and semiempirical electronic structure calculations." <https://gitlab.com/granucci/mopacpi.git>, 2024.
- ³⁸W. Thiel, "Semiempirical quantum–chemical methods," *WIREs Comput. Mol. Sci.*, vol. 4, pp. 145–157, 2014.
- ³⁹"CPMD." <http://www.cpmc.org/>, 2024. Copyright IBM Corp 1990-2019, Copyright MPI für Festkörperforschung Stuttgart 1997-2001.
- ⁴⁰A. Pereira, J. Knapik, A. Chen, D. Lauvergnat, and F. Agostini, "Quantum molecular dynamics simulations of the effect of secondary modes on the photoisomerization of a

- retinal chromophore model," *Eur. Phys. J. Spec. Top.*, vol. 232, pp. 1917–1933, 2023.
- ⁴¹I. S. Lee, J. K. Ha, D. Han, T. I. Kim, S. W. Moon, and S. K. Min, "PyUNIxMD: A Python-based excited state molecular dynamics package," *J. Comput. Chem.*, vol. 42, pp. 1755–1766, 2021.
- ⁴²A. V. Akimov and O. V. Prezhdo, "The PYXAID Program for Non-Adiabatic Molecular Dynamics in Condensed Matter Systems," *J. Chem. Theory Comput.*, vol. 9, pp. 4959–4972, 2013.
- ⁴³O. Weingart, A. Nenov, P. Altoè, I. Rivalta, J. Segarra-Martí, I. Dokukina, and M. Garavelli, "COBRAMM 2.0—A software interface for tailoring molecular electronic structure calculations and running nanoscale (QM/MM) simulations," *J. Mol. Model.*, vol. 24, p. 271, 2018.
- ⁴⁴D. A. Fedorov, S. Seritan, B. S. Fales, T. J. Martínez, and B. G. Levine, "PySpawn: Software for Nonadiabatic Quantum Molecular Dynamics," *J. Chem. Theory Comput.*, vol. 16, pp. 5485–5498, 2020.
- ⁴⁵L. Du and Z. Lan, "An On-the-Fly Surface-Hopping Program JADE for Nonadiabatic Molecular Dynamics of Polyatomic Systems: Implementation and Applications," *J. Chem. Theory Comput.*, vol. 11, pp. 1360–1374, 2015.
- ⁴⁶W. Malone, B. Nebgen, A. White, Y. Zhang, H. Song, J. A. Bjorgaard, A. E. Sifain, B. Rodriguez-Hernandez, V. M. Freixas, S. Fernandez-Alberti, *et al.*, "NEXMD Software Package for Nonadiabatic Excited State Molecular Dynamics Simulations," *J. Chem. Theory Comput.*, vol. 16, pp. 5771–5783, 2020.
- ⁴⁷R. Mitrić, J. Petersen, and V. Bonačić-Koutecký, "Laser-field-induced surface-hopping method for the simulation and control of ultrafast photodynamics," *Phys. Rev. A*, vol. 79, p. 053416, 2009.
- ⁴⁸T. J. A. Wolf, D. M. Sanchez, J. Yang, R. M. Parrish, J. P. F. Nunes, M. Centurion, R. Coffee, J. P. Cryan, M. Gühr, K. Hegazy, *et al.*, "The photochemical ring-opening of 1,3-cyclohexadiene imaged by ultrafast electron diffraction," *Nat. Chem.*, vol. 11, pp. 504–509, 2019.
- ⁴⁹S. Karashima, A. Humeniuk, R. Uenishi, T. Horio, M. Kanno, T. Ohta, J. Nishitani, R. Mitrić, and T. Suzuki, "Ultrafast Ring-Opening Reaction of 1,3-Cyclohexadiene: Iden-

- tification of Nonadiabatic Pathway via Doubly Excited State," *J. Am. Chem. Soc.*, vol. 143, pp. 8034–8045, 2021.
- ⁵⁰O. Travnikova, T. Piteša, A. Ponzi, M. Sapunar, R. J. Squibb, R. Richter, P. Finetti, M. Di Fraia, A. De Fanis, N. Mahne, *et al.*, "Photochemical Ring-Opening Reaction of 1,3-Cyclohexadiene: Identifying the True Reactive State," *J. Am. Chem. Soc.*, vol. 144, pp. 21878–21886, 2022.
- ⁵¹S. Pathak, L. M. Ibele, R. Boll, C. Callegari, A. Demidovich, B. Erk, R. Feifel, R. Forbes, M. Di Fraia, L. Giannesi, *et al.*, "Tracking the ultraviolet-induced photochemistry of thiophenone during and after ultrafast ring opening," *Nat. Chem.*, vol. 12, pp. 795–800, 2020.
- ⁵²J. P. F. Nunes, L. M. Ibele, S. Pathak, A. R. Attar, S. Bhattacharyya, R. Boll, K. Borne, M. Centurion, B. Erk, M.-F. Lin, *et al.*, "Monitoring the Evolution of Relative Product Populations at Early Times during a Photochemical Reaction," *J. Am. Chem. Soc.*, vol. 146, pp. 4134–4143, 2024.
- ⁵³J. Yang, X. Zhu, J. P. F. Nunes, J. K. Yu, R. M. Parrish, T. J. A. Wolf, M. Centurion, M. Gühr, R. Li, Y. Liu, *et al.*, "Simultaneous observation of nuclear and electronic dynamics by ultrafast electron diffraction," *Science*, vol. 368, pp. 885–889, 2020.
- ⁵⁴M. Williams, R. Forbes, H. Weir, K. Veyrinas, R. J. MacDonell, A. E. Boguslavskiy, M. S. Schuurman, A. Stolow, and T. J. Martínez, "Unmasking the cis-Stilbene Phantom State via Vacuum Ultraviolet Time-Resolved Photoelectron Spectroscopy and Ab Initio Multiple Spawning," *J. Phys. Chem. Lett.*, vol. 12, pp. 6363–6369, 2021.
- ⁵⁵T. Piteša, M. Sapunar, A. Ponzi, M. F. Gelin, N. Došlić, W. Domcke, and P. Decleva, "Combined Surface-Hopping, Dyson Orbital, and B-Spline Approach for the Computation of Time-Resolved Photoelectron Spectroscopy Signals: The Internal Conversion in Pyrazine," *J. Chem. Theory Comput.*, vol. 17, pp. 5098–5109, 2021.
- ⁵⁶V. Scutelnic, S. Tsuru, M. Pápai, Z. Yang, M. Epshtein, T. Xue, E. Haugen, Y. Kobayashi, A. I. Krylov, K. B. Møller, *et al.*, "X-ray transient absorption reveals the 1A_u ($n\pi^*$) state of pyrazine in electronic relaxation," *Nat. Commun.*, vol. 12, p. 5003, 2021.
- ⁵⁷Y.-P. Chang, T. Balciunas, Z. Yin, M. Sapunar, B. N. C. Tenorio, A. C. Paul, S. Tsuru, H. Koch, J.-P. Wolf, S. Coriani, *et al.*, "Electronic dynamics created at conical intersections

and its dephasing in aqueous solution," *Nat. Phys.*, vol. 21, pp. 137–145, 2024.

⁵⁸"Prediction Challenge: Cyclobutanone Photochemistry." <https://pubs.aip.org/collection/16531/Prediction-Challenge-Cyclobutanone-Photochemistry>.

⁵⁹"Delta project." <https://molmod.ugent.be/deltacodesdft>.

⁶⁰M. Schreiber, M. R. Silva-Junior, S. P. A. Sauer, and W. Thiel, "Benchmarks for electronically excited states: CASPT2, CC2, CCSD, and CC3," *J. Chem. Phys.*, vol. 128, p. 134110, 2008.

⁶¹M. R. Silva-Junior, S. P. A. Sauer, M. Schreiber, and W. Thiel, "Basis set effects on coupled cluster benchmarks of electronically excited states: CC3, CCSDR(3) and CC2," *Mol. Phys.*, vol. 108, pp. 453–465, 2010.

⁶²K. Lejaeghere, G. Bihlmayer, T. Björkman, P. Blaha, S. Blügel, V. Blum, D. Caliste, I. E. Castelli, S. J. Clark, A. Dal Corso, *et al.*, "Reproducibility in density functional theory calculations of solids," *Science*, vol. 351, p. aad3000, 2016.

⁶³C. Adamo and D. Jacquemin, "The calculations of excited-state properties with Time-Dependent Density Functional Theory," *Chem. Soc. Rev.*, vol. 42, pp. 845–856, 2013.

⁶⁴"HyDRA Challenge." <https://qmbench.net/challenges/hydra/hydra>.

⁶⁵"Fe-MAN Challenge." <https://qmbench.net/challenges/feman/feman>.

⁶⁶J. C. Tully, "Molecular dynamics with electronic transitions," *J. Chem. Phys.*, vol. 93, pp. 1061–1071, 1990.

⁶⁷S. Shin and H. Metiu, "Nonadiabatic effects on the charge transfer rate constant: A numerical study of a simple model system," *J. Chem. Phys.*, vol. 102, pp. 9285–9295, 1995.

⁶⁸S. Hahn and G. Stock, "Quantum-Mechanical Modeling of the Femtosecond Isomerization in Rhodopsin," *J. Phys. Chem. B*, vol. 104, pp. 1146–1149, 2000.

⁶⁹V. Engel and H. Metiu, "A quantum mechanical study of predissociation dynamics of NaI excited by a femtosecond laser pulse," *J. Chem. Phys.*, vol. 90, pp. 6116–6128, 1989.

⁷⁰R. Schneider and W. Domcke, " S_1 - S_2 conical intersection and ultrafast $S_1 \rightarrow S_2$ internal conversion in pyrazine," *Chem. Phys. Lett.*, vol. 150, pp. 235–242, 1988.

⁷¹M. D. Hack, A. M. Wensmann, D. G. Truhlar, M. Ben-Nun, and T. J. Martínez, "Com-

- parison of full multiple spawning, trajectory surface hopping, and converged quantum mechanics for electronically nonadiabatic dynamics," *J. Chem. Phys.*, vol. 115, pp. 1172–1186, 2001.
- ⁷²S. Choi and J. Vaníček, "How important are the residual nonadiabatic couplings for an accurate simulation of nonadiabatic quantum dynamics in a quasidiabatic representation?," *J. Chem. Phys.*, vol. 154, p. 124119, 2021.
- ⁷³W. Xie, M. Sapunar, N. Došlić, M. Sala, and W. Domcke, "Assessing the performance of trajectory surface hopping methods: Ultrafast internal conversion in pyrazine," *J. Chem. Phys.*, vol. 150, p. 154119, 2019.
- ⁷⁴J. Coonjobeeharry, K. E. Spinlove, C. Sanz Sanz, M. Sapunar, N. Došlić, and G. A. Worth, "Mixed-quantum-classical or fully-quantized dynamics? A unified code to compare methods," *Philos. Trans. R. Soc. A*, vol. 380, p. 20200386, 2022.
- ⁷⁵F. Plasser, S. Gómez, M. F. S. J. Menger, S. Mai, and L. González, "Highly efficient surface hopping dynamics using a linear vibronic coupling model," *Phys. Chem. Chem. Phys.*, vol. 21, pp. 57–69, 2019.
- ⁷⁶M. Assmann, H. Köppel, and S. Matsika, "Photoelectron Spectrum and Dynamics of the Uracil Cation," *J. Phys. Chem. A*, vol. 119, pp. 866–875, 2015.
- ⁷⁷T. Nelson, A. Naumov, S. Fernandez-Alberti, and S. Tretiak, "Nonadiabatic excited-state molecular dynamics: On-the-fly limiting of essential excited states," *Chem. Phys.*, vol. 481, pp. 84–90, 2016.
- ⁷⁸L. M. Ibele and B. F. E. Curchod, "A molecular perspective on Tully models for nonadiabatic dynamics," *Phys. Chem. Chem. Phys.*, vol. 22, pp. 15183–15196, 2020.
- ⁷⁹S. Gómez, E. Spinlove, and G. Worth, "Benchmarking non-adiabatic quantum dynamics using the molecular Tully models," *Phys. Chem. Chem. Phys.*, vol. 26, pp. 1829–1844, 2024.
- ⁸⁰J. R. Mannouch and A. Kelly, "Quantum Quality with Classical Cost: Ab Initio Nonadiabatic Dynamics Simulations Using the Mapping Approach to Surface Hopping," *J. Phys. Chem. Lett.*, vol. 15, pp. 5814–5823, 2024.
- ⁸¹L. M. Ibele, Y. Lassmann, T. J. Martínez, and B. F. E. Curchod, "Comparing (stochastic-selection) ab initio multiple spawning with trajectory surface hopping for the photody-

- namics of cyclopropanone, fulvene, and dithiane," *J. Chem. Phys.*, vol. 154, p. 104110, 2021.
- ⁸²B. M. Weight, A. Mandal, and P. Huo, "Ab initio symmetric quasi-classical approach to investigate molecular Tully models," *J. Chem. Phys.*, vol. 155, p. 084106, 2021.
- ⁸³B. M. Weight, A. Mandal, D. Hu, and P. Huo, "Ab initio spin-mapping non-adiabatic dynamics simulations of photochemistry," *J. Chem. Phys.*, vol. 162, p. 084105, 2025.
- ⁸⁴D. Avagliano, E. Lorini, and L. González, "Sampling effects in quantum mechanical/molecular mechanics trajectory surface hopping non-adiabatic dynamics," *Philos. Trans. R. Soc. A*, vol. 380, p. 20200381, 2022.
- ⁸⁵P. Vindel-Zandbergen, L. M. Ibele, J.-K. Ha, S. K. Min, B. F. E. Curchod, and N. T. Maitra, "Study of the Decoherence Correction Derived from the Exact Factorization Approach for Nonadiabatic Dynamics," *J. Chem. Theory Comput.*, vol. 17, pp. 3852–3862, 2021.
- ⁸⁶N. Tokić, T. Piteša, A. Prlj, M. Sapunar, and N. Došlić, "Advantages and Limitations of Landau-Zener Surface Hopping Dynamics," *Croat. Chem. Acta*, vol. 97, 2024.
- ⁸⁷"CECAM workshop: Standardizing nonadiabatic dynamics: towards common benchmarks." <https://www.cecam.org/workshop-details/standardizing-nonadiabatic-dynamics-towards-common-benchmarks-1304>, May 2024.
- ⁸⁸J. Michl and V. Bonačić-Koutecký, *Electronic Aspects of Organic Photochemistry*. Wiley, 1990.
- ⁸⁹N. J. Turro, *Modern Molecular Photochemistry*. University Science Books, 1991.
- ⁹⁰M. Persico and G. Granucci, *Photochemistry: A Modern Theoretical Perspective*. Springer, 2018.
- ⁹¹V. May and O. Kühn, *Charge and Energy Transfer Dynamics in Molecular Systems*. John Wiley & Sons, 2011.
- ⁹²A. D. Wade, "The Semantic Scholar Academic Graph (S2AG)," in *WWW '22: Companion Proceedings of the Web Conference 2022*, Association for Computing Machinery, 2022.
- ⁹³G. Wald, "Molecular Basis of Visual Excitation," *Science*, vol. 162, pp. 230–239, 1968.
- ⁹⁴A. Warshel, "Bicycle-pedal model for the first step in the vision process," *Nature*, vol. 260, pp. 679–683, 1976.

- ⁹⁵L. Dong, Y. Feng, L. Wang, and W. Feng, "Azobenzene-based solar thermal fuels: design, properties, and applications," *Chem. Soc. Rev.*, vol. 47, pp. 7339–7368, 2018.
- ⁹⁶Z. Mahimwalla, K. G. Yager, J.-i. Mamiya, A. Shishido, A. Priimagi, and C. J. Barrett, "Azobenzene photomechanics: prospects and potential applications," *Polym. Bull.*, vol. 69, pp. 967–1006, 2012.
- ⁹⁷A. A. Beharry and G. A. Woolley, "Azobenzene photoswitches for biomolecules," *Chem. Soc. Rev.*, vol. 40, pp. 4422–4437, 2011.
- ⁹⁸D. Villarón and S. J. Wezenberg, "Stiff-Stilbene Photoswitches: From Fundamental Studies to Emergent Applications," *Angew. Chem. Int. Ed.*, vol. 59, pp. 13192–13202, 2020.
- ⁹⁹J. K. Rad, Z. Balzade, and A. R. Mahdavian, "Spiropyran-based advanced photoswitchable materials: A fascinating pathway to the future stimuli-responsive devices," *J. Photochem. Photobiol. C: Photochem. Rev.*, vol. 51, p. 100487, 2022.
- ¹⁰⁰L. Kortekaas and W. R. Browne, "The evolution of spiropyran: fundamentals and progress of an extraordinarily versatile photochrome," *Chem. Soc. Rev.*, vol. 48, pp. 3406–3424, 2019.
- ¹⁰¹R. Klajn, "Spiropyran-based dynamic materials," *Chem. Soc. Rev.*, vol. 43, pp. 148–184, 2014.
- ¹⁰²F. Xu and B. L. Feringa, "Photoresponsive Supramolecular Polymers: From Light-Controlled Small Molecules to Smart Materials," *Adv. Mater.*, vol. 35, p. 2204413, 2023.
- ¹⁰³A. B. Grommet, L. M. Lee, and R. Klajn, "Molecular Photoswitching in Confined Spaces," *Acc. Chem. Res.*, vol. 53, pp. 2600–2610, 2020.
- ¹⁰⁴A. Goulet-Hanssens, F. Eisenreic, and S. Hecht, "Enlightening materials with photoswitches," *Adv. Mater.*, vol. 32, p. 1905966, 2020.
- ¹⁰⁵I. Tochitsky, M. A. Kienzler, E. Isacoff, and R. H. Kramer, "Restoring vision to the blind with chemical photoswitches," *Chem. Rev.*, vol. 118, pp. 10748–10773, 2018.
- ¹⁰⁶B. G. Levine and T. J. Martínez, "Isomerization Through Conical Intersections," *Annu. Rev. Phys. Chem.*, vol. 58, pp. 613–634, 2007.
- ¹⁰⁷R. Schinke, *Photodissociation Dynamics: Spectroscopy and Fragmentation of Small Polyatomic Molecules*. Cambridge University Press, 1995.
- ¹⁰⁸N. F. Scherer, J. L. Knee, D. D. Smith, and A. H. Zewail, "Femtosecond Photofragment

- Spectroscopy: The Reaction $\text{ICN} \rightarrow \text{CN} + \text{I}$," *J. Phys. Chem.*, vol. 89, pp. 5141–5143, 1985.
- ¹⁰⁹T. S. Rose, M. J. Rosker, and A. H. Zewail, "Femtosecond real-time observation of wave packet oscillations (resonance) in dissociation reactions," *J. Chem. Phys.*, vol. 88, pp. 6672–6673, 1988.
- ¹¹⁰H. J. Foth, J. C. Polanyi, and H. H. Telle, "Emission from molecules and reaction intermediates in the process of falling apart," *J. Phys. Chem.*, vol. 86, pp. 5027–5041, 1982.
- ¹¹¹V. Engel and H. Metiu, "The study of NaI predissociation with pump-probe femtosecond laser pulses: The use of an ionizing probe pulse to obtain more detailed dynamic information," *Chem. Phys. Lett.*, vol. 155, pp. 77–82, 1989.
- ¹¹²S. O. Williams and D. G. Imre, "Determination of real time dynamics in molecules by femtosecond laser excitation," *J. Phys. Chem.*, vol. 92, pp. 6648–6654, 1988.
- ¹¹³V. Engel, H. Metiu, R. Almeida, R. A. Marcus, and A. H. Zewail, "Molecular state evolution after excitation with an ultra-short laser pulse: A quantum analysis of NaI and NaBr dissociation," *Chem. Phys. Lett.*, vol. 152, pp. 1–7, 1988.
- ¹¹⁴S. E. Choi and J. C. Light, "Use of the discrete variable representation in the quantum dynamics by a wave packet propagation: Predissociation of $\text{NaI}(^1\Sigma_0^+) \rightarrow \text{NaI}(0^+) \rightarrow \text{Na}(^2S) + \text{I}(^2P)$," *J. Chem. Phys.*, vol. 90, pp. 2593–2604, 1989.
- ¹¹⁵S. Chapman and M. S. Child, "A semiclassical study of long time recurrences in the femtosecond predissociation dynamics of NaI ," *J. Phys. Chem.*, vol. 95, pp. 578–584, 1991.
- ¹¹⁶E. M. Liane, M. Simmermacher, and A. Kirrander, "Ultrafast X-ray scattering and electronic coherence at avoided crossings: complete isotropic signals," *J. Phys. B: At. Mol. Opt. Phys.*, vol. 57, p. 145602, 2024.
- ¹¹⁷V. Betz, B. D. Goddard, and U. Manthe, "Wave packet dynamics in the optimal superadiabatic approximation," *J. Chem. Phys.*, vol. 144, p. 224109, 2016.
- ¹¹⁸J. Janoš, P. Slavíček, and B. F. E. Curchod, "Including Photoexcitation Explicitly in Trajectory-Based Nonadiabatic Dynamics at No Cost," *J. Phys. Chem. Lett.*, vol. 15, pp. 10614–10622, 2024.

- ¹¹⁹K. I. Öberg, "Photochemistry and Astrochemistry: Photochemical Pathways to Interstellar Complex Organic Molecules," *Chem. Rev.*, vol. 116, pp. 9631–9663, 2016.
- ¹²⁰D. A. Blank, S. W. North, and Y. T. Lee, "The ultraviolet photodissociation dynamics of pyrrole," *Chem. Phys.*, vol. 187, pp. 35–47, 1994.
- ¹²¹C.-M. Tseng, Y. T. Lee, M.-F. Lin, C.-K. Ni, S.-Y. Liu, Y.-P. Lee, Z. Xu, and M.-C. Lin, "Photodissociation Dynamics of Phenol," *J. Phys. Chem. A*, vol. 111, pp. 9463–9470, 2007.
- ¹²²S. Satyapal, J. Park, R. Bersohn, and B. Katz, "Dissociation of methanol and ethanol activated by a chemical reaction or by light," *J. Chem. Phys.*, vol. 91, pp. 6873–6879, 1989.
- ¹²³K. I. Öberg, R. T. Garrod, E. F. van Dishoeck, and H. Linnartz, "Formation rates of complex organics in UV irradiated CH₃OH-rich ices," *A&A*, vol. 504, pp. 891–913, 2009.
- ¹²⁴A. Loreti, V. M. Freixas, D. Avagliano, F. Segatta, H. Song, S. Tretiak, S. Mukamel, M. Garavelli, N. Govind, and A. Nenov, "WFOT: A Wave Function Overlap Tool between Single-and Multi-Reference Electronic Structure Methods for Spectroscopy Simulation," *J. Chem. Theory Comput.*, vol. 20, pp. 4804–4819, 2024.
- ¹²⁵B. F. E. Curchod, A. Sisto, and T. J. Martínez, "Ab Initio Multiple Spawning Photochemical Dynamics of DMABN Using GPUs," *J. Phys. Chem. A*, vol. 121, pp. 265–276, 2017.
- ¹²⁶S. Matsika and D. R. Yarkony, "Beyond Two-State Conical Intersections. Three-State Conical Intersections in Low Symmetry Molecules: the Allyl Radical," *J. Am. Chem. Soc.*, vol. 125, pp. 10672–10676, 2003.
- ¹²⁷C. D. Rankine, J. P. F. Nunes, M. S. Robinson, P. D. Lane, and D. A. Wann, "A theoretical investigation of internal conversion in 1,2-dithiane using non-adiabatic multiconfigurational molecular dynamics," *Phys. Chem. Chem. Phys.*, vol. 18, pp. 27170–27174, 2016.
- ¹²⁸J. P. Zobel, M. Heindl, F. Plasser, S. Mai, and L. González, "Surface Hopping Dynamics on Vibronic Coupling Models," *Acc. Chem. Res.*, vol. 54, pp. 3760–3771, 2021.
- ¹²⁹M. Richter, P. Marquetand, J. González-Vázquez, I. Sola, and L. González, "Femtosecond Intersystem Crossing in the DNA Nucleobase Cytosine," *J. Phys. Chem. Lett.*, vol. 3, pp. 3090–3095, 2012.

- ¹³⁰S. Mai, M. Richter, P. Marquetand, and L. González, "Excitation of Nucleobases from a Computational Perspective II: Dynamics," in *Photoinduced Phenomena in Nucleic Acids I: Nucleobases in the Gas Phase and in Solvents* (M. Barbatti, A. C. Borin, and S. Ullrich, eds.), pp. 99–153, Springer International Publishing, 2015.
- ¹³¹B. Fu, Y. C. Han, J. M. Bowman, L. Angelucci, N. Balucani, F. Leonori, and P. Casavecchia, "Intersystem crossing and dynamics in $O(^3P) + C_2H_4$ multichannel reaction: experiment validates theory," *Proc. Natl. Acad. Sci. U.S.A.*, vol. 109, pp. 9733–9738, 2012.
- ¹³²T. Schnappinger, P. Kölle, M. Marazzi, A. Monari, L. González, and R. de Vivie-Riedle, "Ab initio molecular dynamics of thiophene: the interplay of internal conversion and intersystem crossing," *Phys. Chem. Chem. Phys.*, vol. 19, pp. 25662–25670, 2017.
- ¹³³T. Schnappinger, M. Marazzi, S. Mai, A. Monari, L. González, and R. de Vivie-Riedle, "Intersystem Crossing as a Key Component of the Nonadiabatic Relaxation Dynamics of Bithiophene and Terthiophene," *J. Chem. Theory Comput.*, vol. 14, pp. 4530–4540, 2018.
- ¹³⁴R. S. Minns, D. S. N. Parker, T. J. Penfold, G. A. Worth, and H. H. Fielding, "Competing ultrafast intersystem crossing and internal conversion in the "channel 3" region of benzene," *Phys. Chem. Chem. Phys.*, vol. 12, pp. 15607–15615, 2010.
- ¹³⁵C. Reichardt, R. A. Vogt, and C. E. Crespo-Hernández, "On the origin of ultrafast non-radiative transitions in nitro-polycyclic aromatic hydrocarbons: Excited-state dynamics in 1-nitronaphthalene," *J. Chem. Phys.*, vol. 131, p. 224518, 2009.
- ¹³⁶S. Mai, M. Pollum, L. Martínez-Fernández, N. Dunn, P. Marquetand, I. Corral, C. E. Crespo-Hernández, and L. González, "The origin of efficient triplet state population in sulfur-substituted nucleobases," *Nat. Commun.*, vol. 7, p. 13077, 2016.
- ¹³⁷D. Valverde, S. Mai, S. Canuto, A. C. Borin, and L. González, "Ultrafast Intersystem Crossing Dynamics of 6-Selenoguanine in Water," *JACS Au*, vol. 2, pp. 1699–1711, 2022.
- ¹³⁸J. P. Zobel and L. González, "Nonadiabatic Dynamics Simulation Predict Intersystem Crossing in Nitroaromatic Molecules on a Picosecond Time Scale," *ChemPhotoChem*, vol. 3, pp. 833–845, 2019.
- ¹³⁹H. J. M. Greene, D. Ghosh, I. V. Sazanovich, R. Phelps, B. F. E. Curchod, and A. J. Orr-Ewing, "Competing Nonadiabatic Relaxation Pathways for Near-UV Excited ortho-Nitrophenol in Aqueous Solution," *J. Phys. Chem. Lett.*, vol. 15, pp. 9153–9159, 2024.

- ¹⁴⁰C. M. Marian, "Spin-orbit coupling and intersystem crossing in molecules," *WIREs Comput. Mol. Sci.*, vol. 2, pp. 187–203, 2012.
- ¹⁴¹J. N. Harvey, "Spin-forbidden reactions: computational insight into mechanisms and kinetics," *WIREs Comput. Mol. Sci.*, vol. 4, pp. 1–14, 2014.
- ¹⁴²J. N. Harvey, "Understanding the kinetics of spin-forbidden chemical reactions," *Phys. Chem. Chem. Phys.*, vol. 9, pp. 331–343, 2007.
- ¹⁴³C. M. Marian, "Understanding and Controlling Intersystem Crossing in Molecules," *Annu. Rev. Phys. Chem.*, vol. 72, pp. 617–640, 2021.
- ¹⁴⁴L. S. Forster, "Intersystem crossing in transition metal complexes," *Coord. Chem. Rev.*, vol. 250, pp. 2023–2033, 2006.
- ¹⁴⁵G. Baryshnikov, B. Minaev, and H. Ågren, "Theory and Calculation of the Phosphorescence Phenomenon," *Chem. Rev.*, vol. 117, pp. 6500–6537, 2017.
- ¹⁴⁶T. J. Penfold, E. Gindensperger, C. Daniel, and C. M. Marian, "Spin-Vibronic Mechanism for Intersystem Crossing," *Chem. Rev.*, vol. 118, pp. 6975–7025, 2018.
- ¹⁴⁷A. D. Smith, E. M. Warne, D. Bellshaw, D. A. Horke, M. Tudorovskya, E. Springate, A. J. H. Jones, C. Cacho, R. T. Chapman, A. Kirrander, and R. S. Minns, "Mapping the complete reaction path of a complex photochemical reaction," *Phys. Rev. Lett.*, vol. 120, p. 183003, 2018.
- ¹⁴⁸D. Bellshaw, R. S. Minns, and A. Kirrander, "Correspondence between electronic structure calculations and simulations: nonadiabatic dynamics in CS₂," *Phys. Chem. Chem. Phys.*, vol. 21, pp. 14226–14237, 2019.
- ¹⁴⁹J. Cao and D.-C. Chen, "Disulfide bond photochemistry: the effects of higher excited states and different molecular geometries on disulfide bond cleavage," *Phys. Chem. Chem. Phys.*, vol. 21, pp. 4176–4183, 2019.
- ¹⁵⁰B. F. E. Curchod, C. Rauer, P. Marquetand, L. González, and T. J. Martínez, "Communication: GAIMS – Generalized Ab Initio Multiple Spawning for both internal conversion and intersystem crossing processes," *J. Chem. Phys.*, vol. 144, p. 101102, 2016.
- ¹⁵¹F. F. de Carvalho and I. Tavernelli, "Nonadiabatic dynamics with intersystem crossings: A time-dependent density functional theory implementation," *J. Chem. Phys.*, vol. 143, p. 224105, 2015.

- ¹⁵²G. Cui and W. Thiel, "Generalized trajectory surface-hopping method for internal conversion and intersystem crossing," *J. Chem. Phys.*, vol. 141, p. 124101, 2014.
- ¹⁵³M. Richter, P. Marquetand, J. González-Vázquez, I. Sola, and L. González, "SHARC: ab Initio Molecular Dynamics with Surface Hopping in the Adiabatic Representation Including Arbitrary Couplings," *J. Chem. Theory Comput.*, vol. 7, pp. 1253–1258, 2011.
- ¹⁵⁴W. Hu, G. Lendvay, B. Maiti, and G. C. Schatz, "Trajectory Surface Hopping Study of the O(³P) + Ethylene Reaction Dynamics," *J. Phys. Chem. A*, vol. 112, pp. 2093–2103, 2008.
- ¹⁵⁵R. Valero and D. G. Truhlar, "A Diabatic Representation Including Both Valence Nonadiabatic Interactions and Spin-Orbit Effects for Reaction Dynamics," *J. Phys. Chem. A*, vol. 111, pp. 8536–8551, 2007.
- ¹⁵⁶P. Marquetand, M. Richter, J. González-Vázquez, I. Sola, and L. González, "Nonadiabatic ab initio molecular dynamics including spin-orbit coupling and laser fields," *Faraday Discuss.*, vol. 153, pp. 261–273, 2011.
- ¹⁵⁷S. Mai, P. Marquetand, and L. González, "A General Method to Describe Intersystem Crossing Dynamics in Trajectory Surface Hopping," *Int. J. Quantum Chem.*, vol. 115, pp. 1215–1231, 2015.
- ¹⁵⁸G. Granucci, M. Persico, and G. Spighi, "Surface hopping trajectory simulations with spin-orbit and dynamical couplings," *J. Chem. Phys.*, vol. 137, p. 22A501, 2012.
- ¹⁵⁹G. Capano, M. Chergui, U. Rothlisberger, I. Tavernelli, and T. J. Penfold, "A Quantum Dynamics Study of the Ultrafast Relaxation in a Prototypical Cu(I)-Phenanthroline," *J. Phys. Chem. A*, vol. 118, pp. 9861–9869, 2014.
- ¹⁶⁰F. Talotta, S. Morisset, N. Rougeau, D. Lauvergnat, and F. Agostini, "Spin-Orbit Interactions in Ultrafast Molecular Processes," *Phys. Rev. Lett.*, vol. 124, p. 033001, 2020.
- ¹⁶¹P. Zhou and K. Han, "Unraveling the Detailed Mechanism of Excited-State Proton Transfer," *Acc. Chem. Res.*, vol. 51, pp. 1681–1690, 2018.
- ¹⁶²C.-L. Chen, Y.-T. Chen, A. P. Demchenko, and P.-T. Chou, "Amino proton donors in excited-state intramolecular proton-transfer reactions," *Nat. Rev. Chem.*, vol. 2, pp. 131–143, 2018.
- ¹⁶³A. P. Demchenko, "Proton transfer reactions: From photochemistry to biochemistry and

- bioenergetics," *BBA Adv.*, vol. 3, p. 100085, 2023.
- ¹⁶⁴E. L. Holt and V. G. Stavros, "Applications of ultrafast spectroscopy to sunscreen development, from first principles to complex mixtures," *Int. Rev. Phys. Chem.*, vol. 38, pp. 243–285, 2019.
- ¹⁶⁵A. C. Sedgwick, L. Wu, H.-H. Han, S. D. Bull, X.-P. He, T. D. James, J. L. Sessler, B. Z. Tang, H. Tian, and J. Yoon, "Excited-state intramolecular proton-transfer (ESIPT) based fluorescence sensors and imaging agents," *Chem. Soc. Rev.*, vol. 47, pp. 8842–8880, 2018.
- ¹⁶⁶C.-H. Wu, L. J. Karas, H. Ottosson, and J. I.-C. Wu, "Excited-state proton transfer relieves antiaromaticity in molecules," *Proc. Natl. Acad. Sci. U.S.A.*, vol. 116, pp. 20303–20308, 2019.
- ¹⁶⁷H. C. Joshi and L. Antonov, "Excited-State Intramolecular Proton Transfer: A Short Introductory Review," *Molecules*, vol. 26, p. 1475, 2021.
- ¹⁶⁸S. Hammes-Schiffer and A. A. Stuchebrukhov, "Theory of Coupled Electron and Proton Transfer Reactions," *Chem. Rev.*, vol. 110, pp. 6939–6960, 2010.
- ¹⁶⁹Q. Yu, S. Roy, and S. Hammes-Schiffer, "Nonadiabatic Dynamics of Hydrogen Tunneling with Nuclear-Electronic Orbital Multistate Density Functional Theory," *J. Chem. Theory Comput.*, vol. 18, pp. 7132–7141, 2022.
- ¹⁷⁰S. Hammes-Schiffer, "Nuclear-electronic orbital methods: Foundations and prospects," *J. Chem. Phys.*, vol. 155, p. 030901, 2021.
- ¹⁷¹J. C. Light, I. P. Hamilton, and J. V. Lill, "Generalized discrete variable approximation in quantum mechanics," *J. Chem. Phys.*, vol. 82, pp. 1400–1409, 1985.
- ¹⁷²J. C. Light and T. Carrington Jr., "Discrete-Variable Representations and their Utilization," *Adv. Chem. Phys.*, vol. 114, pp. 263–310, 2000.
- ¹⁷³G. Avila and T. Carrington Jr., "Nonproduct quadrature grids for solving the vibrational Schrödinger equation," *J. Chem. Phys.*, vol. 131, p. 174103, 2009.
- ¹⁷⁴H.-D. Meyer, U. Manthe, and L. S. Cederbaum, "The multi-configurational time-dependent Hartree approach," *Chem. Phys. Lett.*, vol. 165, pp. 73–78, 1990.
- ¹⁷⁵M. H. Beck, A. Jäckle, G. A. Worth, and H.-D. Meyer, "The multiconfiguration time-dependent Hartree (MCTDH) method: a highly efficient algorithm for propagating wavepackets," *Phys. Rep.*, vol. 324, pp. 1–105, 2000.

- ¹⁷⁶H. Wang and M. Thoss, "Multilayer formulation of the multiconfiguration time-dependent Hartree theory," *J. Chem. Phys.*, vol. 119, pp. 1289–1299, 2003.
- ¹⁷⁷U. Manthe, "A multilayer multiconfigurational time-dependent Hartree approach for quantum dynamics on general potential energy surfaces," *J. Chem. Phys.*, vol. 128, p. 164116, 2008.
- ¹⁷⁸A. U. J. Lode, C. Lévêque, L. B. Madsen, A. I. Streltsov, and O. E. Alon, "Colloquium: Multiconfigurational time-dependent Hartree approaches for indistinguishable particles," *Rev. Mod. Phys.*, vol. 92, p. 011001, 2020.
- ¹⁷⁹A. Raab, I. Burghardt, and H.-D. Meyer, "The multiconfiguration time-dependent Hartree method generalized to the propagation of density operators," *J. Chem. Phys.*, vol. 111, pp. 8759–8772, 1999.
- ¹⁸⁰D. Picconi and I. Burghardt, "Open system dynamics using Gaussian-based multiconfigurational time-dependent Hartree wavefunctions: Application to environment-modulated tunneling," *J. Chem. Phys.*, vol. 150, p. 224106, 2019.
- ¹⁸¹D. Picconi, "Dynamics of high-dimensional quantum systems coupled to a harmonic bath. General theory and implementation via multiconfigurational wave packets and truncated hierarchical equations for the mean-fields," *J. Chem. Phys.*, vol. 161, p. 164108, 2024.
- ¹⁸²A. Van Haefen, C. Ash, and G. Worth, "Propagating multi-dimensional density operators using the multi-layer- ρ multi-configurational time-dependent Hartree method," *J. Chem. Phys.*, vol. 159, p. 194114, 2023.
- ¹⁸³J. Haegeman, C. Lubich, I. Oseledets, B. Vandereycken, and F. Verstraete, "Unifying time evolution and optimization with matrix product states," *Phys. Rev. B*, vol. 94, p. 165116, 2016.
- ¹⁸⁴S. Paeckel, T. Köhler, A. Swoboda, S. R. Manmana, U. Schollwöck, and C. Hubig, "Time-evolution methods for matrix-product states," *Ann. Phys.*, vol. 411, p. 167998, 2019.
- ¹⁸⁵H. R. Larsson, "A tensor network view of multilayer multiconfiguration time-dependent Hartree methods," *Mol. Phys.*, vol. 122, p. e2306881, 2024.
- ¹⁸⁶J. Ren, W. Li, T. Jiang, Y. Wang, and Z. Shuai, "Time-dependent density matrix renormalization group method for quantum dynamics in complex systems," *WIREs Comput. Mol. Sci.*, vol. 12, p. e1614, 2022.

- ¹⁸⁷S. Han, M. Schröder, F. Gatti, H.-D. Meyer, D. Lauvergnat, D. R. Yarkony, and H. Guo, "Representation of Diabatic Potential Energy Matrices for Multiconfiguration Time-Dependent Hartree Treatments of High-Dimensional Nonadiabatic Photodissociation Dynamics," *J. Chem. Theory Comput.*, vol. 18, pp. 4627–4638, 2022.
- ¹⁸⁸H. R. Larsson and A. Viel, "2500 vibronic eigenstates of the NO₃ radical," *Phys. Chem. Chem. Phys.*, vol. 26, pp. 24506–24523, 2024.
- ¹⁸⁹A. Viel, W. Eisfeld, S. Neumann, W. Domcke, and U. Manthe, "Photoionization-induced dynamics of ammonia: Ab initio potential energy surfaces and time-dependent wave packet calculations for the ammonia cation," *J. Chem. Phys.*, vol. 124, p. 214306, 2006.
- ¹⁹⁰R. Ellerbrock, H. Hoppe, and U. Manthe, "A non-hierarchical multi-layer multi-configurational time-dependent hartree approach for quantum dynamics on general potential energy surfaces," *J. Chem. Phys.*, vol. 160, p. 224108, 2024.
- ¹⁹¹T. J. Martínez, M. Ben-Nun, and R. D. Levine, "Multi-Electronic-State Molecular Dynamics: A Wave Function Approach with Applications," *J. Phys. Chem.*, vol. 100, pp. 7884–7895, 1996.
- ¹⁹²M. Ben-Nun, J. Quenneville, and T. J. Martínez, "Ab Initio Multiple Spawning: Photochemistry from First Principles Quantum Molecular Dynamics," *J. Phys. Chem. A*, vol. 104, pp. 5161–5175, 2000.
- ¹⁹³B. Mignolet and B. F. E. Curchod, "Excited-State Molecular Dynamics Triggered by Light Pulses—Ab Initio Multiple Spawning vs Trajectory Surface Hopping," *J. Phys. Chem. A*, vol. 123, pp. 3582–3591, 2019.
- ¹⁹⁴B. F. E. Curchod, W. J. Glover, and T. J. Martínez, "SSAIMS—Stochastic-Selection Ab Initio Multiple Spawning for Efficient Nonadiabatic Molecular Dynamics," *J. Phys. Chem. A*, vol. 124, pp. 6133–6143, 2020.
- ¹⁹⁵Y. Lassmann and B. F. E. Curchod, "AIMSWISS—Ab initio multiple spawning with informed stochastic selections," *J. Chem. Phys.*, vol. 154, p. 211106, 2021.
- ¹⁹⁶D. V. Shalashilin and M. S. Child, "Multidimensional quantum propagation with the help of coupled coherent states," *J. Chem. Phys.*, vol. 115, pp. 5367–5375, 2001.
- ¹⁹⁷D. V. Shalashilin, "Quantum mechanics with the basis set guided by Ehrenfest trajectories: Theory and application to spin-boson model," *J. Chem. Phys.*, vol. 130, p. 244101, 2009.

- ¹⁹⁸D. V. Makhov, W. J. Glover, T. J. Martínez, and D. V. Shalashilin, "Ab initio multiple cloning algorithm for quantum nonadiabatic molecular dynamics," *J. Chem. Phys.*, vol. 141, p. 054110, 2014.
- ¹⁹⁹I. Burghardt, H.-D. Meyer, and L. S. Cederbaum, "Approaches to the approximate treatment of complex molecular systems by the multiconfiguration time-dependent Hartree method," *J. Chem. Phys.*, vol. 111, pp. 2927–2939, 1999.
- ²⁰⁰G. A. Worth and I. Burghardt, "Full quantum mechanical molecular dynamics using Gaussian wavepackets," *Chem. Phys. Lett.*, vol. 368, pp. 502–508, 2003.
- ²⁰¹I. Burghardt, K. Giri, and G. A. Worth, "Multimode quantum dynamics using Gaussian wavepackets: The Gaussian-based multiconfiguration time-dependent Hartree (GMCTDH) method applied to the absorption spectrum of pyrazine," *J. Chem. Phys.*, vol. 129, p. 174104, 2008.
- ²⁰²G. W. Richings and G. A. Worth, "Multi-state non-adiabatic direct-dynamics on propagated diabatic potential energy surfaces," *Chem. Phys. Lett.*, vol. 683, pp. 606–612, 2017.
- ²⁰³J. C. Tully and R. K. Preston, "Trajectory Surface Hopping Approach to Nonadiabatic Molecular Collisions: The Reaction of H^+ with D_2 ," *J. Chem. Phys.*, vol. 55, pp. 562–572, 1971.
- ²⁰⁴S. Hammes-Schiffer and J. C. Tully, "Proton transfer in solution: Molecular dynamics with quantum transitions," *J. Chem. Phys.*, vol. 101, pp. 4657–4667, 1994.
- ²⁰⁵C. Zhu, K. Nobusada, and H. Nakamura, "New implementation of the trajectory surface hopping method with use of the Zhu–Nakamura theory," *J. Chem. Phys.*, vol. 115, pp. 3031–3044, 2001.
- ²⁰⁶D. F. Coker and L. Xiao, "Methods for molecular dynamics with nonadiabatic transitions," *J. Chem. Phys.*, vol. 102, pp. 496–510, 1995.
- ²⁰⁷S. Nielsen, R. Kapral, and G. Ciccotti, "Mixed quantum-classical surface hopping dynamics," *J. Chem. Phys.*, vol. 112, pp. 6543–6553, 2000.
- ²⁰⁸A. Kelly and T. E. Markland, "Efficient and accurate surface hopping for long time nonadiabatic quantum dynamics," *J. Chem. Phys.*, vol. 139, p. 014104, 2013.
- ²⁰⁹R. Kapral, "Surface hopping from the perspective of quantum–classical Liouville dynamics," *Chem. Phys.*, vol. 481, pp. 77–83, 2016.

- ²¹⁰A. K. Belyaev, W. Domcke, C. Lasser, and G. Trigila, "Nonadiabatic nuclear dynamics of the ammonia cation studied by surface hopping classical trajectory calculations," *J. Chem. Phys.*, vol. 142, 2015.
- ²¹¹L. Araujo, C. Lasser, and B. Schmidt, "FSSH-2: fewest switches surface hopping with robust switching probability," *J. Chem. Theory Comput.*, vol. 20, pp. 3413–3419, 2024.
- ²¹²A. K. Belyaev, C. Lasser, and G. Trigila, "Landau–Zener type surface hopping algorithms," *J. Chem. Phys.*, vol. 140, p. 224108, 2014.
- ²¹³I.-Y. Hsiao, Y. Teranishi, and H. Nakamura, "Classically forbidden nonadiabatic transitions in multidimensional chemical dynamics," *Phys. Chem. Chem. Phys.*, vol. 26, pp. 3795–3799, 2024.
- ²¹⁴T. Ishida, S. Nanbu, and H. Nakamura, "Clarification of nonadiabatic chemical dynamics by the Zhu-Nakamura theory of nonadiabatic transition: from tri-atomic systems to reactions in solutions," *Int. Rev. Phys. Chem.*, vol. 36, pp. 229–285, 2017.
- ²¹⁵E. R. Bittner and P. J. Rossky, "Quantum decoherence in mixed quantum-classical systems: Nonadiabatic processes," *J. Chem. Phys.*, vol. 103, pp. 8130–8143, 1995.
- ²¹⁶G. Granucci and M. Persico, "Critical appraisal of the fewest switches algorithm for surface hopping," *J. Chem. Phys.*, vol. 126, p. 134114, 2007.
- ²¹⁷G. Granucci, M. Persico, and A. Zocante, "Including quantum decoherence in surface hopping," *J. Chem. Phys.*, vol. 133, p. 134111, 2010.
- ²¹⁸M. Persico, G. Granucci, and D. Accomasso, "The Quantum Decoherence Problem in Nonadiabatic Trajectory Methods," in *Comprehensive Computational Chemistry, Volume 4* (M. Yáñez and R. J. Boyd, eds.), pp. 273–292, Oxford: Elsevier, first ed., 2024.
- ²¹⁹J. E. Subotnik and N. Shenvi, "A new approach to decoherence and momentum rescaling in the surface hopping algorithm," *J. Chem. Phys.*, vol. 134, p. 024105, 2011.
- ²²⁰A. Jain, E. Alguire, and J. E. Subotnik, "An Efficient, Augmented Surface Hopping Algorithm That Includes Decoherence for Use in Large-Scale Simulations," *J. Chem. Theory Comput.*, vol. 12, pp. 5256–5268, 2016.
- ²²¹H. M. Jaeger, S. Fischer, and O. V. Prezhdo, "Decoherence-induced surface hopping," *J. Chem. Phys.*, vol. 137, p. 22A545, 2012.
- ²²²J. Suchan, J. Janoš, and P. Slavíček, "Pragmatic Approach to Photodynamics: Mixed

- Landau–Zener Surface Hopping with Intersystem Crossing,” *J. Chem. Theory Comput.*, vol. 16, pp. 5809–5820, 2020.
- ²²³C. Pieroni and F. Agostini, “Nonadiabatic Dynamics with Coupled Trajectories,” *J. Chem. Theory Comput.*, vol. 17, pp. 5969–5991, 2021.
- ²²⁴G. Granucci, M. Persico, and A. Toniolo, “Direct semiclassical simulation of photochemical processes with semiempirical wave functions,” *J. Chem. Phys.*, vol. 114, pp. 10608–10615, 2001.
- ²²⁵L. Wang, A. Akimov, and O. V. Prezhdo, “Recent Progress in Surface Hopping: 2011–2015,” *J. Phys. Chem. Lett.*, vol. 7, pp. 2100–2112, 2016.
- ²²⁶J. M. Toldo, R. S. Mattos, M. Pinheiro Jr., S. Mukherjee, and M. Barbatti, “Recommendations for Velocity Adjustment in Surface Hopping,” *J. Chem. Theory Comput.*, vol. 20, pp. 614–624, 2024.
- ²²⁷F. Plasser, S. Mai, M. Fumanal, E. Gindensperger, C. Daniel, and L. González, “Strong influence of decoherence corrections and momentum rescaling in surface hopping dynamics of transition metal complexes,” *J. Chem. Theory Comput.*, vol. 15, pp. 5031–5045, 2019.
- ²²⁸T. Nelson, S. Fernandez-Alberti, A. E. Roitberg, and S. Tretiak, “Artifacts due to trivial unavoided crossings in the modeling of photoinduced energy transfer dynamics in extended conjugated molecules,” *Chem. Phys. Lett.*, vol. 590, pp. 208–213, 2013.
- ²²⁹L. Wang and O. V. Prezhdo, “A Simple Solution to the Trivial Crossing Problem in Surface Hopping,” *J. Phys. Chem. Lett.*, vol. 5, pp. 713–719, 2014.
- ²³⁰A. Abedi, N. T. Maitra, and E. K. U. Gross, “Exact Factorization of the Time-Dependent Electron-Nuclear Wave Function,” *Phys. Rev. Lett.*, vol. 105, p. 123002, 2010.
- ²³¹L. M. Ibele, C. Pieroni, F. Talotta, B. F. E. Curchod, D. Lauvergnat, and F. Agostini, “Exact Factorization of the Electron-Nuclear Wavefunction: Fundamentals and Algorithms,” in *Comprehensive Computational Chemistry, Volume 4* (M. Yáñez and R. J. Boyd, eds.), pp. 188–211, Oxford: Elsevier, first ed., 2024.
- ²³²C. Pieroni, E. Sangiogo Gil, L. M. Ibele, M. Persico, G. Granucci, and F. Agostini, “Investigating the Photodynamics of trans-Azobenzene with Coupled Trajectories,” *J. Chem. Theory Comput.*, vol. 20, pp. 580–596, 2024.
- ²³³R. Xie, Z. Shi, and L. Wang, “Coupled Trajectory Surface Hopping with Sign Consistency,”

2024. doi: 10.26434/chemrxiv-2024-9dzv5.
- ²³⁴L. M. Ibele, E. Sangiogo Gil, P. Schürger, and F. Agostini, "A coupled-trajectory approach for decoherence, frustrated hops and internal consistency in surface hopping," 2024. doi: 10.48550/arXiv.2412.04958.
- ²³⁵J.-K. Ha, I. S. Lee, and S. K. Min, "Surface Hopping Dynamics beyond Nonadiabatic Couplings for Quantum Coherence," *J. Phys. Chem. Lett.*, vol. 9, pp. 1097–1104, 2018.
- ²³⁶J.-K. Ha and S. K. Min, "Independent trajectory mixed quantum-classical approaches based on the exact factorization," *J. Chem. Phys.*, vol. 156, p. 174109, 2022.
- ²³⁷D. Han and A. V. Akimov, "Nonadiabatic Dynamics with Exact Factorization: Implementation and Assessment," *J. Chem. Theory Comput.*, vol. 20, pp. 5022–5042, 2024.
- ²³⁸L. Dupuy, A. Rikus, and N. T. Maitra, "Exact-Factorization-Based Surface Hopping without Velocity Adjustment," *J. Phys. Chem. Lett.*, vol. 15, pp. 2643–2649, 2024.
- ²³⁹C. F. Craig, W. R. Duncan, and O. V. Prezhdo, "Trajectory Surface Hopping in the Time-Dependent Kohn-Sham Approach for Electron-Nuclear Dynamics," *Phys. Rev. Lett.*, vol. 95, p. 163001, 2005.
- ²⁴⁰R. Tempelaar and D. R. Reichman, "Generalization of fewest-switches surface hopping for coherences," *J. Chem. Phys.*, vol. 148, p. 102309, 2018.
- ²⁴¹C. C. Martens, "Surface Hopping without Momentum Jumps: A Quantum-Trajectory-Based Approach to Nonadiabatic Dynamics," *J. Phys. Chem. A*, vol. 123, pp. 1110–1128, 2019.
- ²⁴²C. C. Martens, "Surface Hopping by Consensus," *J. Phys. Chem. Lett.*, vol. 7, pp. 2610–2615, 2016.
- ²⁴³J. Spencer, F. Gajdos, and J. Blumberger, "FOB-SH: Fragment orbital-based surface hopping for charge carrier transport in organic and biological molecules and materials," *J. Chem. Phys.*, vol. 145, p. 064102, 2016.
- ²⁴⁴F. Kossoski and M. Barbatti, "Nonadiabatic dynamics in multidimensional complex potential energy surfaces," *Chem. Sci.*, vol. 11, pp. 9827–9835, 2020.
- ²⁴⁵Z. Tao, Q. Yu, S. Roy, and S. Hammes-Schiffer, "Direct Dynamics with Nuclear–Electronic Orbital Density Functional Theory," *Acc. Chem. Res.*, vol. 54, pp. 4131–4141, 2021.
- ²⁴⁶J. R. Mannouch and J. O. Richardson, "A mapping approach to surface hopping," *J. Chem.*

- Phys.*, vol. 158, p. 104111, 2023.
- ²⁴⁷J. E. Runeson and D. E. Manolopoulos, "A multi-state mapping approach to surface hopping," *J. Chem. Phys.*, vol. 159, p. 094115, 2023.
- ²⁴⁸J. E. Lawrence, J. R. Mannouch, and J. O. Richardson, "A size-consistent multi-state mapping approach to surface hopping," *J. Chem. Phys.*, vol. 160, p. 244112, 2024.
- ²⁴⁹A. D. McLachlan, "A variational solution of the time-dependent schrodinger equation," *Mol. Phys.*, vol. 8, pp. 39–44, 1964.
- ²⁵⁰A. J. Jenkins, K. E. Spinlove, M. Vacher, G. A. Worth, and M. A. Robb, "The Ehrenfest method with fully quantum nuclear motion (Qu-Eh): Application to charge migration in radical cations," *J. Chem. Phys.*, vol. 149, p. 094108, 2018.
- ²⁵¹V. M. Freixas, S. Fernandez-Alberti, D. V. Makhov, S. Tretiak, and D. Shalashilin, "An ab initio multiple cloning approach for the simulation of photoinduced dynamics in conjugated molecules," *Phys. Chem. Chem. Phys.*, vol. 20, pp. 17762–17772, 2018.
- ²⁵²S. C. Cheng, C. Zhu, K. K. Liang, S. H. Lin, and D. G. Truhlar, "Algorithmic decoherence time for decay-of-mixing non-Born-Oppenheimer dynamics," *J. Chem. Phys.*, vol. 129, p. 024112, 2008.
- ²⁵³C. Zhu, S. Nangia, A. W. Jasper, and D. G. Truhlar, "Coherent switching with decay of mixing: an improved treatment of electronic coherence for non-Born-Oppenheimer trajectories," *J. Chem. Phys.*, vol. 121, pp. 7658–7670, 2004.
- ²⁵⁴C. Zhu, A. W. Jasper, and D. G. Truhlar, "Non-Born-Oppenheimer Liouville-von Neumann Dynamics. Evolution of a Subsystem Controlled by Linear and Population-Driven Decay of Mixing with Decoherent and Coherent Switching," *J. Chem. Theory Comput.*, vol. 1, pp. 527–540, 2005.
- ²⁵⁵W. H. Miller, "The Semiclassical Initial Value Representation: A Potentially Practical Way for Adding Quantum Effects to Classical Molecular Dynamics Simulations," *J. Phys. Chem. A*, vol. 105, pp. 2942–2955, 2001.
- ²⁵⁶X. Sun and W. H. Miller, "Semiclassical initial value representation for electronically nonadiabatic molecular dynamics," *J. Chem. Phys.*, vol. 106, pp. 6346–6353, 1997.
- ²⁵⁷X. Sun, H. Wang, and W. H. Miller, "Semiclassical theory of electronically nonadiabatic dynamics: Results of a linearized approximation to the initial value representation," *J.*

- Chem. Phys.*, vol. 109, pp. 7064–7074, 1998.
- ²⁵⁸S. J. Cotton and W. H. Miller, “Symmetrical windowing for quantum states in quasi-classical trajectory simulations: Application to electronically non-adiabatic processes,” *J. Chem. Phys.*, vol. 139, p. 234112, 2013.
- ²⁵⁹S. J. Cotton and W. H. Miller, “Symmetrical windowing for quantum states in quasi-classical trajectory simulations,” *J. Phys. Chem. A*, vol. 117, pp. 7190–7194, 2013.
- ²⁶⁰R. Kapral and G. Ciccotti, “Mixed quantum-classical dynamics,” *J. Chem. Phys.*, vol. 110, pp. 8919–8929, 1999.
- ²⁶¹R. Kapral, “Progress in the Theory of Mixed Quantum-Classical Dynamics,” *Annu. Rev. Phys. Chem.*, vol. 57, pp. 129–157, 2006.
- ²⁶²R. Grunwald, A. Kelly, and R. Kapral, “Quantum Dynamics in Almost Classical Environments,” in *Energy Transfer Dynamics in Biomaterial Systems* (I. Burghardt, V. May, D. A. Micha, and E. R. Bittner, eds.), pp. 383–413, Springer, 2009.
- ²⁶³H. Kim, A. Nassimi, and R. Kapral, “Quantum-classical Liouville dynamics in the mapping basis,” *J. Chem. Phys.*, vol. 129, p. 084102, 2008.
- ²⁶⁴A. Kelly, R. Van Zon, J. Schofield, and R. Kapral, “Mapping quantum-classical Liouville equation: Projectors and trajectories,” *J. Chem. Phys.*, vol. 136, p. 084101, 2012.
- ²⁶⁵C.-Y. Hsieh and R. Kapral, “Nonadiabatic dynamics in open quantum-classical systems: Forward-backward trajectory solution,” *J. Chem. Phys.*, vol. 137, p. 22A507, 2012.
- ²⁶⁶A. Kelly, A. Montoya-Castillo, L. Wang, and T. E. Markland, “Generalized quantum master equations in and out of equilibrium: When can one win?,” *J. Chem. Phys.*, vol. 144, p. 184105, 2016.
- ²⁶⁷E. R. Dunkel, S. Bonella, and D. F. Coker, “Iterative linearized approach to nonadiabatic dynamics,” *J. Chem. Phys.*, vol. 129, p. 114106, 2008.
- ²⁶⁸S. Bonella and D. F. Coker, “LAND-map, a linearized approach to nonadiabatic dynamics using the mapping formalism,” *J. Chem. Phys.*, vol. 122, p. 194102, 2005.
- ²⁶⁹P. Huo and D. F. Coker, “Communication: Partial linearized density matrix dynamics for dissipative, non-adiabatic quantum evolution,” *J. Chem. Phys.*, vol. 135, p. 201101, 2011.
- ²⁷⁰J. E. Runeson and J. O. Richardson, “Spin-mapping approach for nonadiabatic molecular dynamics,” *J. Chem. Phys.*, vol. 151, p. 044119, 2019.

- ²⁷¹J. E. Runeson and J. O. Richardson, "Generalized spin mapping for quantum-classical dynamics," *J. Chem. Phys.*, vol. 152, p. 084110, 2020.
- ²⁷²M. A. C. Saller, A. Kelly, and J. O. Richardson, "On the identity of the identity operator in nonadiabatic linearized semiclassical dynamics," *J. Chem. Phys.*, vol. 150, p. 071101, 2019.
- ²⁷³M. A. C. Saller, A. Kelly, and J. O. Richardson, "Improved population operators for multi-state nonadiabatic dynamics with the mixed quantum-classical mapping approach," *Faraday Discuss.*, vol. 221, pp. 150–167, 2020.
- ²⁷⁴G. Amati, M. A. C. Saller, A. Kelly, and J. O. Richardson, "Quasiclassical approaches to the generalized quantum master equation," *J. Chem. Phys.*, vol. 157, p. 234103, 2022.
- ²⁷⁵J. R. Mannouch and J. O. Richardson, "A partially linearized spin-mapping approach for nonadiabatic dynamics. I. Derivation of the theory," *J. Chem. Phys.*, vol. 153, p. 194109, 2020.
- ²⁷⁶J. R. Mannouch and J. O. Richardson, "A partially linearized spin-mapping approach for nonadiabatic dynamics. II. Analysis and comparison with related approaches," *J. Chem. Phys.*, vol. 153, p. 194110, 2020.
- ²⁷⁷D. Hu, Y. Xie, J. Peng, and Z. Lan, "On-the-Fly Symmetrical Quasi-Classical Dynamics with Meyer–Miller Mapping Hamiltonian for the Treatment of Nonadiabatic Dynamics at Conical Intersections," *J. Chem. Theory Comput.*, vol. 17, pp. 3267–3279, 2021.
- ²⁷⁸H. Meyer and W. H. Miller, "A classical analog for electronic degrees of freedom in nonadiabatic collision processes," *J. Chem. Phys.*, vol. 70, pp. 3214–3223, 1979.
- ²⁷⁹G. Stock and M. Thoss, "Classical description of nonadiabatic quantum dynamics," *Adv. Chem. Phys.*, vol. 131, pp. 243–375, 2005.
- ²⁸⁰J. Liu, X. He, and B. Wu, "Unified formulation of phase space mapping approaches for nonadiabatic quantum dynamics," *Acc. Chem. Res.*, vol. 23, pp. 4215–4228, 2021.
- ²⁸¹Y. Xie, J. Zheng, and Z. Lan, "Performance evaluation of the symmetrical quasi-classical dynamics method based on Meyer–Miller mapping Hamiltonian in the treatment of site-exciton models," *J. Chem. Phys.*, vol. 149, p. 174105, 2018.
- ²⁸²X. Gao, M. A. C. Saller, Y. Liu, A. Kelly, J. O. Richardson, and E. Geva, "Benchmarking Quasiclassical Mapping Hamiltonian Methods for Simulating Electronically Nonadiabatic

- Molecular Dynamics," *J. Chem. Theory Comput.*, vol. 16, pp. 2883–2895, 2020.
- ²⁸³W. Zhou, A. Mandal, and P. Huo, "Quasi-diabatic scheme for nonadiabatic on-the-fly simulations," *J. Phys. Chem. Lett.*, vol. 10, pp. 7062–7070, 2019.
- ²⁸⁴D. Tang, W.-H. Fang, L. Shen, and G. Cui, "Combining Meyer-Miller Hamiltonian with electronic structure methods for on-the-fly nonadiabatic dynamics simulations: Implementation and application," *Phys. Chem. Chem. Phys.*, vol. 21, pp. 17109–17117, 2019.
- ²⁸⁵W. H. Miller, "Electronically Nonadiabatic Dynamics via Semiclassical Initial Value Methods," *J. Phys. Chem. A*, vol. 113, pp. 1405–1415, 2009.
- ²⁸⁶P. F. Huo and D. F. Coker, "Consistent schemes for non-adiabatic dynamics derived from partial linearized density matrix propagation," *J. Chem. Phys.*, vol. 137, p. 22a535, 2012.
- ²⁸⁷S. K. Min, F. Agostini, and E. K. U. Gross, "Coupled-Trajectory Quantum-Classical Approach to Electronic Decoherence in Nonadiabatic Processes," *Phys. Rev. Lett.*, vol. 115, p. 073001, 2015.
- ²⁸⁸E. Villaseco Arribas and N. T. Maitra, "Energy-conserving coupled trajectory mixed quantum-classical dynamics," *J. Chem. Phys.*, vol. 158, p. 161105, 2023.
- ²⁸⁹A. Dines, M. Ellis, and J. Blumberger, "Stabilized coupled trajectory mixed quantum-classical algorithm with improved energy conservation: CTMQC-EDI," *J. Chem. Phys.*, vol. 159, p. 234118, 2023.
- ²⁹⁰E. Villaseco Arribas, L. M. Ibele, D. Lauvergnat, N. T. Maitra, and F. Agostini, "Significance of Energy Conservation in Coupled-Trajectory Approaches to Nonadiabatic Dynamics," *J. Chem. Theory Comput.*, vol. 19, pp. 7787–7800, 2023.
- ²⁹¹F. P. Bonafé, B. Aradi, B. Hourahine, C. R. Medrano, F. J. Hernández, T. Frauenheim, and C. G. Sánchez, "A Real-Time Time-Dependent Density Functional Tight-Binding Implementation for Semiclassical Excited State Electron–Nuclear Dynamics and Pump–Probe Spectroscopy Simulations," *J. Chem. Theory Comput.*, vol. 16, pp. 4454–4469, 2020.
- ²⁹²F. J. Hernández, F. P. Bonafé, B. Aradi, T. Frauenheim, and C. G. Sánchez, "Simulation of Impulsive Vibrational Spectroscopy," *J. Phys. Chem. A*, vol. 123, pp. 2065–2072, 2019.
- ²⁹³N. Makri and D. E. Makarov, "Tensor propagator for iterative quantum time evolution of reduced density matrices. I. Theory," *J. Chem. Phys.*, vol. 102, pp. 4600–4610, 1995.
- ²⁹⁴N. Makri and K. Thompson, "Semiclassical influence functionals for quantum systems in

- anharmonic environments," *Chem. Phys. Lett.*, vol. 291, pp. 101–109, 1998.
- ²⁹⁵R. Lambert and N. Makri, "Quantum-classical path integral. I. Classical memory and weak quantum nonlocality," *J. Chem. Phys.*, vol. 137, p. 22A552, 2012.
- ²⁹⁶N. Makri, "Small Matrix Path Integral with Extended Memory," *J. Chem. Theory Comput.*, vol. 17, pp. 1–6, 2021.
- ²⁹⁷L. V. Keldysh, "Diagram technique for nonequilibrium processes," in *Selected Papers of Leonid V Keldysh* (M. V. Sadovskii, ed.), pp. 47–55, World Scientific, 2024.
- ²⁹⁸L. P. Kadanoff and G. Baym, *Quantum Statistical Mechanics: Green's Function Methods in Equilibrium and Nonequilibrium Problems*. CRC Press, 2018.
- ²⁹⁹G. Cohen and M. Galperin, "Green's function methods for single molecule junctions," *J. Chem. Phys.*, vol. 152, p. 090901, 2020.
- ³⁰⁰L. Nanni, "Dynamics of proton tunneling in Hydrogen-Bonded systems through Green's function formalism," *J. Nat. Sci. & Math. Res.*, vol. 10, pp. 22–34, 2024.
- ³⁰¹J. Xu, R. Zhou, V. Blum, T. E. Li, S. Hammes-Schiffer, and Y. Kanai, "First-Principles Approach for Coupled Quantum Dynamics of Electrons and Protons in Heterogeneous Systems," *Phys. Rev. Lett.*, vol. 131, p. 238002, 2023.
- ³⁰²J. Xu, R. Zhou, T. E. Li, S. Hammes-Schiffer, and Y. Kanai, "Lagrangian formulation of nuclear–electronic orbital Ehrenfest dynamics with real-time TDDFT for extended periodic systems," *J. Chem. Phys.*, vol. 161, p. 194109, 2024.
- ³⁰³Y. Tanimura and R. Kubo, "Time Evolution of a Quantum System in Contact with a Nearly Gaussian-Markoffian Noise Bath," *J. Phys. Soc. Jpn.*, vol. 58, pp. 101–114, 1989.
- ³⁰⁴Y. Tanimura, "Numerically "exact" approach to open quantum dynamics: The hierarchical equations of motion (HEOM)," *J. Chem. Phys.*, vol. 153, p. 020901, 2020.
- ³⁰⁵Y. Ke, "Tree tensor network state approach for solving hierarchical equations of motion," *J. Chem. Phys.*, vol. 158, p. 211102, 2023.
- ³⁰⁶E. Mangaud, A. Jaouadi, A. Chin, and M. Desouter-Lecomte, "Survey of the hierarchical equations of motion in tensor-train format for non-Markovian quantum dynamics," *Eur. Phys. J.: Spec. Top.*, vol. 232, pp. 1847–1869, 2023.
- ³⁰⁷J. Prior, A. W. Chin, S. F. Huelga, and M. B. Plenio, "Efficient Simulation of Strong System-Environment Interactions," *Phys. Rev. Lett.*, vol. 105, p. 050404, 2010.

- ³⁰⁸D. Tamascelli, A. Smirne, J. Lim, S. F. Huelga, and M. B. Plenio, "Efficient Simulation of Finite-Temperature Open Quantum Systems," *Phys. Rev. Lett.*, vol. 123, p. 090402, 2019.
- ³⁰⁹S. Mukherjee and M. Barbatti, "A Hessian-Free Method to Prevent Zero-Point Energy Leakage in Classical Trajectories," *J. Chem. Theory Comput.*, vol. 18, pp. 4109–4116, 2022.
- ³¹⁰Y. Shu and D. G. Truhlar, "Improved Local-Mode Zero-Point-Energy Conservation Scheme for Quasiclassical Trajectories," *J. Phys. Chem. A*, vol. 128, pp. 3625–3634, 2024.
- ³¹¹R. J. MacDonell, C. E. Dickerson, C. J. T. Birch, A. Kumar, C. L. Edmunds, M. J. Biercuk, C. Hempel, and I. Kassal, "Analog quantum simulation of chemical dynamics," *Chem. Sci.*, vol. 12, pp. 9794–9805, 2021.
- ³¹²C. H. Valahu, V. C. Olaya-Agudelo, R. J. MacDonell, T. Navickas, A. D. Rao, M. J. Millican, J. B. Pérez-Sánchez, J. Yuen-Zhou, M. J. Biercuk, C. Hempel, *et al.*, "Direct observation of geometric-phase interference in dynamics around a conical intersection," *Nat. Chem.*, vol. 15, pp. 1503–1508, 2023.
- ³¹³K. Sun, M. Kang, H. Nuomin, G. Schwartz, D. N. Beratan, K. R. Brown, and J. Kim, "Quantum simulation of spin-boson models with structured bath," 2024. doi: 10.48550/arXiv.2405.14624.
- ³¹⁴T. Navickas, R. J. MacDonell, C. H. Valahu, V. C. Olaya-Agudelo, F. Scuccimarra, M. J. Millican, V. G. Matsos, H. L. Nourse, A. D. Rao, *et al.*, "Experimental Quantum Simulation of Chemical Dynamics," 2024. doi: 10.48550/arXiv.2409.04044.
- ³¹⁵I. Kassal, S. P. Jordan, P. J. Love, M. Mohseni, and A. Aspuru-Guzik, "Polynomial-time quantum algorithm for the simulation of chemical dynamics," *Proc. Natl. Acad. Sci. U.S.A.*, vol. 105, pp. 18681–18686, 2008.
- ³¹⁶A. M. Childs, J. Leng, T. Li, J.-P. Liu, and C. Zhang, "Quantum simulation of real-space dynamics," *Quantum*, vol. 6, p. 860, 2022.
- ³¹⁷N. C. Rubin, D. W. Berry, A. Kononov, F. D. Malone, T. Khattar, A. White, J. Lee, H. Neven, R. Babbush, and A. D. Baczewski, "Quantum computation of stopping power for inertial fusion target design," *Proc. Natl. Acad. Sci. U.S.A.*, vol. 121, p. e2317772121, 2024.

- ³¹⁸D. Motlagh, R. A. Lang, J. A. Campos-Gonzalez-Angulo, T. Zeng, A. Aspuru-Guzik, and J. M. Arrazola, "Quantum Algorithm for Vibronic Dynamics: Case Study on Singlet Fission Solar Cell Design," 2024. doi: 10.48550/arXiv.2411.13669.
- ³¹⁹A. Kovyrshin, M. Skogh, L. Tornberg, A. Broo, S. Mensa, E. Sahin, B. C. B. Symons, J. Crain, and I. Tavernelli, "Nonadiabatic Nuclear–Electron Dynamics: A Quantum Computing Approach," *J. Phys. Chem. Lett.*, vol. 14, pp. 7065–7072, 2023.
- ³²⁰P. J. Ollitrault, G. Mazzola, and I. Tavernelli, "Nonadiabatic molecular quantum dynamics with quantum computers," *Phys. Rev. Lett.*, vol. 125, p. 260511, 2020.
- ³²¹A. Gandon, A. Baiardi, P. Ollitrault, and I. Tavernelli, "Nonadiabatic Molecular Dynamics with Fermionic Subspace-Expansion Algorithms on Quantum Computers," *J. Chem. Theory Comput.*, vol. 20, pp. 5951–5963, 2024.
- ³²²D. Tuna, D. Lefrancois, Ł. Wolański, S. Gozem, I. Schapiro, T. Andruniów, A. Dreuw, and M. Olivucci, "Assessment of Approximate Coupled-Cluster and Algebraic-Diagrammatic Construction Methods for Ground- and Excited-State Reaction Paths and the Conical Intersection Seam of a Retinal-Chromophore Model," *J. Chem. Theory Comput.*, vol. 11, pp. 5758–5781, 2015.
- ³²³T. V. Papineau, D. Jacquemin, and M. Vacher, "Which Electronic Structure Method to Choose in Trajectory Surface Hopping Dynamics Simulations? Azomethane as a Case Study," *J. Phys. Chem. Lett.*, vol. 15, pp. 636–643, 2024.
- ³²⁴L. Ibele, A. Memhood, B. G. Levine, and D. Avagliano, "Ab Initio Multiple Spawning Nonadiabatic Dynamics with Different CASPT2 Flavors: A Fully Open-Source PySpawn/OpenMolcas Interface," *J. Chem. Theory Comput.*, vol. 20, pp. 8140–8151, 2024.
- ³²⁵J. Janoš and P. Slaviček, "What Controls the Quality of Photodynamical Simulations? Electronic Structure Versus Nonadiabatic Algorithm," *J. Chem. Theory Comput.*, vol. 19, pp. 8273–8284, 2023.
- ³²⁶S. Mukherjee, R. S. Mattos, J. M. Toldo, H. Lischka, and M. Barbatti, "Prediction challenge: Simulating Rydberg photoexcited cyclobutanone with surface hopping dynamics based on different electronic structure methods," *J. Chem. Phys.*, vol. 160, p. 154306, 2024.
- ³²⁷J. P. Zobel, A. Kruse, O. Baig, S. Lochbrunner, S. I. Bokarev, O. Kühn, L. González, and

- O. S. Bokareva, "Can range-separated functionals be optimally tuned to predict spectra and excited state dynamics in photoactive iron complexes?," *Chem. Sci.*, vol. 14, pp. 1491–1502, 2023.
- ³²⁸S. Gozem, F. Melaccio, A. Valentini, M. Filatov, M. Huix-Rotllant, N. Ferré, L. M. Frutos, C. Angeli, A. I. Krylov, A. A. Granovsky, *et al.*, "Shape of Multireference, Equation-of-Motion Coupled-Cluster, and Density Functional Theory Potential Energy Surfaces at a Conical Intersection," *J. Chem. Theory Comput.*, vol. 10, pp. 3074–3084, 2014.
- ³²⁹J. C. Cooper, C. Y. Z. Brown, J. Kára, and A. Kirrander, "Photoexcited dynamics of the valence states of norbornadiene," *J. Chem. Phys.*, vol. 162, p. 094102, 2025.
- ³³⁰J. C. Cooper and A. Kirrander, "Electronic structure of norbornadiene and quadricyclane," *Phys. Chem. Chem. Phys.*, vol. 27, pp. 3089–3101, 2025.
- ³³¹R. P. Brady, C. Drury, S. N. Yurchenko, and J. Tennyson, "Numerical Equivalence of Diabatic and Adiabatic Representations in Diatomic Molecules," *J. Chem. Theory Comput.*, vol. 20, pp. 2127–2139, 2024.
- ³³²S. Matsika, "Electronic Structure Methods for the Description of Nonadiabatic Effects and Conical Intersections," *Chem. Rev.*, vol. 121, pp. 9407–9449, 2021.
- ³³³P. G. Szalay, T. Müller, G. Gidofalvi, H. Lischka, and R. Shepard, "Multiconfiguration Self-Consistent Field and Multireference Configuration Interaction Methods and Applications," *Chem. Rev.*, vol. 112, pp. 108–181, 2012.
- ³³⁴L. González, D. Escudero, and L. Serrano-Andrés, "Progress and Challenges in the Calculation of Electronic Excited States," *ChemPhysChem*, vol. 13, pp. 28–51, 2012.
- ³³⁵J. W. Park, R. Al-Saadon, M. K. MacLeod, T. Shiozaki, and B. Vlaisavljevich, "Multireference Electron Correlation Methods: Journeys along Potential Energy Surfaces," *Chem. Rev.*, vol. 120, pp. 5878–5909, 2020.
- ³³⁶J. W. Snyder Jr., R. M. Parrish, and T. J. Martínez, " α -CASSCF: An Efficient, Empirical Correction for SA-CASSCF To Closely Approximate MS-CASPT2 Potential Energy Surfaces," *J. Phys. Chem. Lett.*, vol. 8, pp. 2432–2437, 2017.
- ³³⁷L. M. Frutos, T. Andruniów, F. Santoro, N. Ferré, and M. Olivucci, "Tracking the excited-state time evolution of the visual pigment with multiconfigurational quantum chemistry," *Proc. Natl. Acad. Sci. U.S.A.*, vol. 104, pp. 7764–7769, 2007.

- ³³⁸N. H. List, C. M. Jones, and T. J. Martínez, "Internal conversion of the anionic GFP chromophore: in and out of the I-twisted S_1/S_0 conical intersection seam," *Chem. Sci.*, vol. 13, pp. 373–385, 2022.
- ³³⁹P. Slaviček and T. J. Martínez, "Ab initio floating occupation molecular orbital-complete active space configuration interaction: An efficient approximation to CASSCF," *J. Chem. Phys.*, vol. 132, p. 234102, 2010.
- ³⁴⁰D. Hollas, L. Šišťík, E. G. Hohenstein, T. J. Martínez, and P. Slaviček, "Nonadiabatic Ab Initio Molecular Dynamics with the Floating Occupation Molecular Orbital-Complete Active Space Configuration Interaction Method," *J. Chem. Theory Comput.*, vol. 14, pp. 339–350, 2018.
- ³⁴¹C. A. Ullrich, *Time-Dependent Density-Functional Theory: Concepts and Applications*. Oxford University Press, 2011.
- ³⁴²D. J. Tozer and N. C. Handy, "On the determination of excitation energies using density functional theory," *Phys. Chem. Chem. Phys.*, vol. 2, pp. 2117–2121, 2000.
- ³⁴³B. G. Levine, C. Ko, J. Quenneville, and T. J. Martínez, "Conical intersections and double excitations in time-dependent density functional theory," *Mol. Phys.*, vol. 104, pp. 1039–1051, 2006.
- ³⁴⁴N. T. Maitra, F. Zhang, R. J. Cave, and K. Burke, "Double excitations within time-dependent density functional theory linear response," *J. Chem. Phys.*, vol. 120, pp. 5932–5937, 2004.
- ³⁴⁵A. Dreuw and M. Head-Gordon, "Failure of Time-Dependent Density Functional Theory for Long-Range Charge-Transfer Excited States: The Zinbacteriochlorin-Bacteriochlorin and Bacteriochlorophyll-Spheroidene Complexes," *J. Am. Chem. Soc.*, vol. 126, pp. 4007–4016, 2004.
- ³⁴⁶M. Hellgren and E. K. U. Gross, "Discontinuities of the exchange-correlation kernel and charge-transfer excitations in time-dependent density-functional theory," *Phys. Rev. A*, vol. 85, p. 022514, 2012.
- ³⁴⁷M. Thiele and S. Kümmel, "Frequency Dependence of the Exact Exchange-Correlation Kernel of Time-Dependent Density-Functional Theory," *Phys. Rev. Lett.*, vol. 112, p. 083001, 2014.

- ³⁴⁸R. J. Cave, F. Zhang, N. T. Maitra, and K. Burke, "A dressed TDDFT treatment of the 2^1A_g states of butadiene and hexatriene," *Chem. Phys. Lett.*, vol. 389, pp. 39–42, 2004.
- ³⁴⁹P. Elliott, S. Goldson, C. Canahui, and N. T. Maitra, "Perspectives on double-excitations in TDDFT," *Chem. Phys.*, vol. 391, pp. 110–119, 2011.
- ³⁵⁰J. T. Taylor, D. J. Tozer, and B. F. E. Curchod, "On the description of conical intersections between excited electronic states with LR-TDDFT and ADC(2)," *J. Chem. Phys.*, vol. 159, p. 214115, 2023.
- ³⁵¹J. T. Taylor, D. J. Tozer, and B. F. E. Curchod, "On the Topological Phase around Conical Intersections with Tamm–Dancoff Linear-Response Time-Dependent Density Functional Theory," *J. Phys. Chem. A*, vol. 128, pp. 5314–5320, 2024.
- ³⁵²N. T. Maitra, "Perspective: Fundamental aspects of time-dependent density functional theory," *J. Chem. Phys.*, vol. 144, p. 220901, 2016.
- ³⁵³P. Wiggins, J. A. G. Williams, and D. J. Tozer, "Excited state surfaces in density functional theory: a new twist on an old problem," *J. Chem. Phys.*, vol. 131, p. 091101, 2009.
- ³⁵⁴O. Ferchichi, N. Derbel, T. Cours, and A. Alijah, "Dichlorine peroxide (ClOOCI), chloryl chloride (ClCl(O)O) and chlorine chlorite (ClOClO): very accurate ab initio structures and actinic degradation," *Phys. Chem. Chem. Phys.*, vol. 22, pp. 4059–4071, 2020.
- ³⁵⁵W. Chebbi, N. Derbel, A. Alijah, and T. Cours, "UV-spectrum and photodecomposition of peroxyxynitrous acid in the troposphere," *Phys. Chem. Chem. Phys.*, vol. 26, pp. 123–129, 2024.
- ³⁵⁶D. Lefrancois, D. Tuna, T. J. Martínez, and A. Dreuw, "The Spin-Flip Variant of the Algebraic-Diagrammatic Construction Yields the Correct Topology of S_1/S_0 Conical Intersections," *J. Chem. Theory Comput.*, vol. 13, pp. 4436–4441, 2017.
- ³⁵⁷Y. Shao, M. Head-Gordon, and A. I. Krylov, "The spin–flip approach within time-dependent density functional theory: Theory and applications to diradicals," *J. Chem. Phys.*, vol. 118, pp. 4807–4818, 2003.
- ³⁵⁸X. Zhang and J. M. Herbert, "Spin-flip, tensor equation-of-motion configuration interaction with a density-functional correction: a spin-complete method for exploring excited-state potential energy surfaces," *J. Chem. Phys.*, vol. 143, p. 234107, 2015.
- ³⁵⁹Z. Li and W. Liu, "Spin-adapted open-shell random phase approximation and time-

- dependent density functional theory. I. Theory," *J. Chem. Phys.*, vol. 133, p. 064106, 2010.
- ³⁶⁰Z. Li, W. Liu, Y. Zhang, and B. Suo, "Spin-adapted open-shell time-dependent density functional theory. II. Theory and pilot application," *J. Chem. Phys.*, vol. 134, p. 134101, 2011.
- ³⁶¹Z. Li and W. Liu, "Spin-adapted open-shell time-dependent density functional theory. III. An even better and simpler formulation," *J. Chem. Phys.*, vol. 135, p. 194106, 2011.
- ³⁶²M. Filatov, "Spin-restricted ensemble-referenced Kohn–Sham method: basic principles and application to strongly correlated ground and excited states of molecules," *WIREs Comput. Mol. Sci.*, vol. 5, pp. 146–167, 2015.
- ³⁶³S. Lee, E. E. Kim, H. Nakata, S. Lee, and C. H. Choi, "Efficient implementations of analytic energy gradient for mixed-reference spin-flip time-dependent density functional theory (MRSF-TDDFT)," *J. Chem. Phys.*, vol. 150, p. 184111, 2019.
- ³⁶⁴S. Lee, S. Shostak, M. Filatov, and C. H. Choi, "Conical Intersections in Organic Molecules: Benchmarking Mixed-Reference Spin–Flip Time-Dependent DFT (MRSF-TD-DFT) vs Spin–Flip TD-DFT," *J. Phys. Chem. A*, vol. 123, pp. 6455–6462, 2019.
- ³⁶⁵Y. Horbatenko, S. Lee, M. Filatov, and C. H. Choi, "How Beneficial Is the Explicit Account of Doubly-Excited Configurations in Linear Response Theory?," *J. Chem. Theory Comput.*, vol. 17, pp. 975–984, 2021.
- ³⁶⁶C. Bannwarth, J. K. Yu, E. G. Hohenstein, and T. J. Martínez, "Hole–hole Tamm–Dancoff-approximated density functional theory: A highly efficient electronic structure method incorporating dynamic and static correlation," *J. Chem. Phys.*, vol. 153, p. 024110, 2020.
- ³⁶⁷J. K. Yu, C. Bannwarth, E. G. Hohenstein, and T. J. Martínez, "Ab Initio Nonadiabatic Molecular Dynamics with Hole–Hole Tamm–Dancoff Approximated Density Functional Theory," *J. Chem. Theory Comput.*, vol. 16, pp. 5499–5511, 2020.
- ³⁶⁸J. Yu, J. Li, T. Zhu, and W. Yang, "Accurate and efficient prediction of double excitation energies using the particle–particle random phase approximation," *J. Chem. Phys.*, vol. 162, p. 094101, 2025.
- ³⁶⁹D. B. Dar and N. T. Maitra, "Oscillator strengths and excited-state couplings for double excitations in time-dependent density functional theory," *J. Chem. Phys.*, vol. 159,

p. 211104, 2023.

- ³⁷⁰D. B. Dar and N. T. Maitra, "Capturing the Elusive Curve-Crossing in Low-Lying States of Butadiene with Dressed TDDFT," *J. Phys. Chem. Lett.*, vol. 16, pp. 703–709, 2025.
- ³⁷¹X. Li, N. Govind, C. Isborn, A. E. DePrince III, and K. Lopata, "Real-Time Time-Dependent Electronic Structure Theory," *Chem. Rev.*, vol. 120, pp. 9951–9993, 2020.
- ³⁷²M. R. Provorse and C. M. Isborn, "Electron dynamics with real-time time-dependent density functional theory," *Int. J. Quantum Chem.*, vol. 116, pp. 739–749, 2016.
- ³⁷³A. Dreuw and M. Wormit, "The algebraic diagrammatic construction scheme for the polarization propagator for the calculation of excited states," *WIREs Comput. Mol. Sci.*, vol. 5, pp. 82–95, 2015.
- ³⁷⁴F. Plasser, R. Crespo-Otero, M. Pederzoli, J. Pittner, H. Lischka, and M. Barbatti, "Surface Hopping Dynamics with Correlated Single-Reference Methods: 9H-Adenine as a Case Study," *J. Chem. Theory Comput.*, vol. 10, pp. 1395–1405, 2014.
- ³⁷⁵E. Marsili, A. Prlj, and B. F. E. Curchod, "Caveat when using ADC(2) for studying the photochemistry of carbonyl-containing molecules," *Phys. Chem. Chem. Phys.*, vol. 23, pp. 12945–12949, 2021.
- ³⁷⁶C. Hättig, "Structure Optimizations for Excited States with Correlated Second-Order Methods: CC2 and ADC(2)," *Adv. Quantum Chem.*, vol. 50, pp. 37–60, 2005.
- ³⁷⁷S. M. Parker, S. Roy, and F. Furche, "Unphysical divergences in response theory," *J. Chem. Phys.*, vol. 145, p. 134105, 2016.
- ³⁷⁸E. F. Kjønsstad, O. J. Fajen, A. C. Paul, S. Angelico, D. Mayer, M. Gühr, T. J. A. Wolf, T. J. Martínez, and H. Koch, "Photoinduced hydrogen dissociation in thymine predicted by coupled cluster theory," *Nat. Commun.*, vol. 15, p. 10128, 2024.
- ³⁷⁹D. Hait, D. Lahana, O. J. Fajen, A. S. Paz, P. A. Unzueta, B. Rana, L. Lu, Y. Wang, E. F. Kjønsstad, H. Koch, and T. J. Martínez, "Prediction of photodynamics of 200 nm excited cyclobutanone with linear response electronic structure and ab initio multiple spawning," *J. Chem. Phys.*, vol. 160, p. 244101, 2024.
- ³⁸⁰T. Cusati, G. Granucci, and M. Persico, "Photodynamics and Time-Resolved Fluorescence of Azobenzene in Solution: A Mixed Quantum-Classical Simulation," *J. Am. Chem. Soc.*, vol. 133, pp. 5109–5123, 2011.

- ³⁸¹T. Cusati, G. Granucci, E. Martínez-Núñez, F. Martini, M. Persico, and S. Vázquez, "Semiempirical Hamiltonian for Simulation of Azobenzene Photochemistry," *J. Phys. Chem. A*, vol. 116, pp. 98–110, 2012.
- ³⁸²E. Fabiano, T. W. Keal, and W. Thiel, "Implementation of surface hopping molecular dynamics using semiempirical methods," *Chem. Phys.*, vol. 349, pp. 334–347, 2008.
- ³⁸³D. Accomasso, M. Persico, and G. Granucci, "Diabatization by Localization in the Framework of Configuration Interaction Based on Floating Occupation Molecular Orbitals (FOMO-CI)," *ChemPhotoChem*, vol. 3, pp. 933–944, 2019.
- ³⁸⁴D. Accomasso, S. Arslançan, L. Cupellini, G. Granucci, and B. Mennucci, "Ultrafast Excited-State Dynamics of Carotenoids and the Role of the S_x State," *J. Phys. Chem. Lett.*, vol. 13, pp. 6762–6769, 2022.
- ³⁸⁵E. Fabiano and W. Thiel, "Nonradiative Deexcitation Dynamics of 9H-Adenine: An OM2 Surface Hopping Study," *J. Phys. Chem. A*, vol. 112, pp. 6859–6863, 2008.
- ³⁸⁶O. Weingart, Z. Lan, A. Kosłowski, and W. Thiel, "Chiral Pathways and Periodic Decay in cis-Azobenzene Photodynamics," *J. Phys. Chem. Lett.*, vol. 2, pp. 1506–1509, 2011.
- ³⁸⁷G. Li Manni, I. Fdez. Galván, A. Alavi, F. Aleotti, F. Aquilante, J. Autschbach, D. Avagliano, A. Baiardi, J. J. Bao, S. Battaglia, *et al.*, "The OpenMolcas Web: A Community-Driven Approach to Advancing Computational Chemistry," *J. Chem. Theory Comput.*, vol. 19, pp. 6933–6991, 2023.
- ³⁸⁸T. Shiozaki, "BAGEL: Brilliantly Advanced General Electronic-structure Library," *WIREs Comput. Mol. Sci.*, vol. 8, p. e1331, 2018.
- ³⁸⁹F. Neese, "Software update: the ORCA program system, version 4.0," *WIREs Comput. Mol. Sci.*, vol. 8, p. e1327, 2018.
- ³⁹⁰E. Aprà, E. J. Bylaska, W. A. de Jong, N. Govind, K. Kowalski, T. P. Straatsma, M. Valiev, H. J. J. van Dam, Y. Alexeev, J. Anchell, *et al.*, "NWChem: Past, present, and future," *J. Chem. Phys.*, vol. 152, p. 184102, 2020.
- ³⁹¹G. M. J. Barca, C. Bertoni, L. Carrington, D. Datta, N. De Silva, J. E. Deustua, D. G. Fedorov, J. R. Gour, A. O. Gunina, E. Guidez, *et al.*, "Recent developments in the general atomic and molecular electronic structure system," *J. Chem. Phys.*, vol. 152, p. 154102, 2020.

- ³⁹²X. Wu, A. Kosłowski, and W. Thiel, "Semiempirical Quantum Chemical Calculations Accelerated on a Hybrid Multicore CPU–GPU Computing Platform," *J. Chem. Theory Comput.*, vol. 8, pp. 2272–2281, 2012.
- ³⁹³Q. Sun, T. C. Berkelbach, N. S. Blunt, G. H. Booth, S. Guo, Z. Li, J. Liu, J. D. McClain, E. R. Sayfutyarova, S. Sharma, *et al.*, "PySCF: the Python-based simulations of chemistry framework," *WIREs Comput. Mol. Sci.*, vol. 8, p. e1340, 2018.
- ³⁹⁴G. W. Richings and S. Habershon, "MCTDH on-the-fly: Efficient grid-based quantum dynamics without pre-computed potential energy surfaces," *J. Chem. Phys.*, vol. 148, p. 134116, 2018.
- ³⁹⁵G. W. Richings, C. Robertson, and S. Habershon, "Improved on-the-Fly MCTDH Simulations with Many-Body-Potential Tensor Decomposition and Projection Diabatization," *J. Chem. Theory Comput.*, vol. 15, pp. 857–870, 2019.
- ³⁹⁶H. Köppel, W. Domcke, and L. S. Cederbaum, "The multi-mode vibronic-coupling approach," in *Conical Intersections*, pp. 323–367, World Scientific, 2004.
- ³⁹⁷M. Heindl and L. González, "Taming Disulfide Bonds with Laser Fields. Nonadiabatic Surface-Hopping Simulations in a Ruthenium Complex," *J. Phys. Chem. Lett.*, vol. 13, pp. 1894–1900, 2022.
- ³⁹⁸P. Vindel-Zandbergen, S. Matsika, and N. T. Maitra, "Exact-Factorization-Based Surface Hopping for Multistate Dynamics," *J. Phys. Chem. Lett.*, vol. 13, pp. 1785–1790, 2022.
- ³⁹⁹Y. Guan, C. Xie, D. R. Yarkony, and H. Guo, "High-fidelity first principles nonadiabaticity: diabaticization, analytic representation of global diabatic potential energy matrices, and quantum dynamics," *Phys. Chem. Chem. Phys.*, vol. 23, pp. 24962–24983, 2021.
- ⁴⁰⁰J. Westermayr, M. Gastegger, M. F. S. J. Menger, S. Mai, L. González, and P. Marquetand, "Machine learning enables long time scale molecular photodynamics simulations," *Chem. Sci.*, vol. 10, pp. 8100–8107, 2019.
- ⁴⁰¹P. O. Dral and M. Barbatti, "Molecular excited states through a machine learning lens," *Nat. Rev. Chem.*, vol. 5, pp. 388–405, 2021.
- ⁴⁰²J. Westermayr and P. Marquetand, "Machine Learning for Electronically Excited States of Molecules," *Chem. Rev.*, vol. 121, pp. 9873–9926, 2020.
- ⁴⁰³I. Schapiro, M. N. Ryazantsev, L. M. Frutos, N. Ferré, R. Lindh, and M. Olivucci, "The

- Ultrafast Photoisomerizations of Rhodopsin and Bathorhodopsin Are Modulated by Bond Length Alternation and HOOP Driven Electronic Effects," *J. Am. Chem. Soc.*, vol. 133, pp. 3354–3364, 2011.
- ⁴⁰⁴C. Schnedermann, X. Yang, M. Liebel, K. Spillane, J. Lugtenburg, I. Fernández, A. Valentini, I. Schapiro, M. Olivucci, P. Kukura, *et al.*, "Evidence for a vibrational phase-dependent isotope effect on the photochemistry of vision," *Nat. Chem.*, vol. 10, pp. 449–455, 2018.
- ⁴⁰⁵S. Manzhos and T. Carrington, Jr., "Using neural networks to represent potential surfaces as sum of products," *J. Chem. Phys.*, vol. 125, p. 084109, 2006.
- ⁴⁰⁶Q. Song, X. Zhang, D. Peláez, and Q. Meng, "Direct Canonical-Polyadic-Decomposition of the Potential Energy Surface from Discrete Data by Decoupled Gaussian Process Regression," *J. Phys. Chem. Lett.*, vol. 13, pp. 11128–11135, 2022.
- ⁴⁰⁷G. Avila and T. Carrington Jr., "Using multi-dimensional Smolyak interpolation to make a sum-of-products potential," *J. Chem. Phys.*, vol. 143, p. 044106, 2015.
- ⁴⁰⁸R. L. Panadés-Barrueta and D. Peláez, "Low-rank sum-of-products finite-basis-representation (SOP-FBR) of potential energy surfaces," *J. Chem. Phys.*, vol. 153, p. 234110, 2020.
- ⁴⁰⁹N. s. Nadoveza, R. L. Panadés-Barrueta, L. Shi, F. Gatti, and D. Peláez, "Analytical high-dimensional operators in canonical polyadic finite basis representation (CP-FBR)," *J. Chem. Phys.*, vol. 158, p. 114109, 2023.
- ⁴¹⁰Z. Qiu, F. Magoulès, and D. Peláez, "Single-entry computation of analytical hierarchical (binary) tree structures," *Adv. Eng. Softw.*, vol. 203, p. 103873, 2025.
- ⁴¹¹L. Shi, M. Schröder, H.-D. Meyer, D. Peláez, A. M. Wodtke, K. Golibrzuch, A.-M. Schöne-mann, A. Kandratsenka, and F. Gatti, "Quantum and classical molecular dynamics for h atom scattering from graphene," *J. Chem. Phys.*, vol. 159, p. 194102, 2023.
- ⁴¹²M. Persico and G. Granucci, "An overview of nonadiabatic dynamics simulations methods, with focus on the direct approach versus the fitting of potential energy surfaces," *Theor. Chem. Acc.*, vol. 133, p. 1526, 2014.
- ⁴¹³J. Suchan, D. Hollas, B. F. E. Curchod, and P. Slavíček, "On the importance of initial conditions for excited-state dynamics," *Faraday Discuss.*, vol. 212, pp. 307–330, 2018.
- ⁴¹⁴J. Janoš, P. Slavíček, and B. F. E. Curchod, "Selecting Initial Conditions for Trajectory-

- Based Nonadiabatic Simulations," *Acc. Chem. Res.*, vol. 58, pp. 261–270, 2025.
- ⁴¹⁵L. Adamska, I. Nayyar, H. Chen, A. K. Swan, N. Oldani, S. Fernandez-Alberti, M. R. Golder, R. Jasti, S. K. Doorn, and S. Tretiak, "Self-trapping of excitons, violation of condon approximation, and efficient fluorescence in conjugated cycloparaphenylenes," *Nano Lett.*, vol. 14, pp. 6539–6546, 2014.
- ⁴¹⁶M. Ceriotti, G. Bussi, and M. Parrinello, "Nuclear Quantum Effects in Solids Using a Colored-Noise Thermostat," *Phys. Rev. Lett.*, vol. 103, p. 030603, 2009.
- ⁴¹⁷M. Ceriotti, G. Bussi, and M. Parrinello, "Colored-Noise Thermostats à la Carte," *J. Chem. Theory Comput.*, vol. 6, pp. 1170–1180, 2010.
- ⁴¹⁸S. Huppert, T. Plé, S. Bonella, P. Depondt, and F. Finocchi, "Simulation of Nuclear Quantum Effects in Condensed Matter Systems via Quantum Baths," *Appl. Sci.*, vol. 12, p. 4756, 2022.
- ⁴¹⁹M. Barbatti and K. Sen, "Effects of different initial condition samplings on photodynamics and spectrum of pyrrole," *Int. J. Quantum Chem.*, vol. 116, pp. 762–771, 2016.
- ⁴²⁰A. Prlj, D. Hollas, and B. F. E. Curchod, "Deciphering the Influence of Ground-State Distributions on the Calculation of Photolysis Observables," *J. Phys. Chem. A*, vol. 127, pp. 7400–7409, 2023.
- ⁴²¹I. Tavernelli, B. F. E. Curchod, and U. Rothlisberger, "Mixed quantum-classical dynamics with time-dependent external fields: A time-dependent density-functional-theory approach," *Phys. Rev. A*, vol. 81, p. 052508, 2010.
- ⁴²²B. Mignolet, B. F. E. Curchod, and T. J. Martínez, "Communication: XFAIMS—eXternal Field Ab Initio Multiple Spawning for electron-nuclear dynamics triggered by short laser pulses," *J. Chem. Phys.*, vol. 145, p. 191104, 2016.
- ⁴²³T. Penfold, M. Pápai, K. B. Møller, and G. A. Worth, "Excited state dynamics initiated by an electromagnetic field within the Variational Multi-Configurational Gaussian (vMCG) method," *Comput. Theor. Chem.*, vol. 1160, pp. 24–30, 2019.
- ⁴²⁴J. J. Bajo, G. Granucci, and M. Persico, "Interplay of radiative and nonradiative transitions in surface hopping with radiation-molecule interactions," *J. Chem. Phys.*, vol. 140, p. 044113, 2014.
- ⁴²⁵M. Heindl and L. González, "Validating fewest-switches surface hopping in the presence

- of laser fields," *J. Chem. Phys.*, vol. 154, p. 144102, 2021.
- ⁴²⁶T. Fiedlschuster, J. Handt, and R. Schmidt, "Floquet surface hopping: Laser-driven dissociation and ionization dynamics of H_2^+ ," *Phys. Rev. A*, vol. 93, p. 053409, 2016.
- ⁴²⁷T. Fiedlschuster, J. Handt, E. K. U. Gross, and R. Schmidt, "Surface hopping in laser-driven molecular dynamics," *Phys. Rev. A*, vol. 95, p. 063424, 2017.
- ⁴²⁸P. Brumer, "Shedding (Incoherent) Light on Quantum Effects in Light-Induced Biological Processes," *J. Phys. Chem. Lett.*, vol. 9, pp. 2946–2955, 2018.
- ⁴²⁹M. Barbatti, "Simulation of Excitation by Sunlight in Mixed Quantum-Classical Dynamics," *J. Chem. Theory Comput.*, vol. 16, pp. 4849–4856, 2020.
- ⁴³⁰M. Schirò, F. G. Eich, and F. Agostini, "Quantum-classical nonadiabatic dynamics of Floquet driven systems," *J. Chem. Phys.*, vol. 154, p. 114101, 2021.
- ⁴³¹A. Martínez-Mesa and P. Saalfrank, "Semiclassical modelling of finite-pulse effects on non-adiabatic photodynamics via initial condition filtering: The predissociation of NaI as a test case," *J. Chem. Phys.*, vol. 142, p. 194107, 2015.
- ⁴³²M. F. Gelin, X. Huang, W. Xie, L. Chen, N. Došlić, and W. Domcke, "Ab Initio Surface-Hopping Simulation of Femtosecond Transient-Absorption Pump–Probe Signals of Nonadiabatic Excited-State Dynamics Using the Doorway–Window Representation," *J. Chem. Theory Comput.*, vol. 17, pp. 2394–2408, 2021.
- ⁴³³E. Villaseco Arribas, N. T. Maitra, and F. Agostini, "Nonadiabatic dynamics with classical trajectories: The problem of an initial coherent superposition of electronic states," *J. Chem. Phys.*, vol. 160, p. 054102, 2024.
- ⁴³⁴D. Ondarse-Alvarez, N. Oldani, A. Roitberg, V. Kleiman, S. Tretiak, and S. Fernandez-Alberti, "Energy transfer and spatial scrambling of an exciton in a conjugated dendrimer," *Phys. Chem. Chem. Phys.*, vol. 20, pp. 29648–29660, 2018.
- ⁴³⁵L. Alfonso-Hernandez, N. Oldani, S. Athanasopoulos, J. Lupton, S. Tretiak, and S. Fernandez-Alberti, "Photoinduced energy transfer in linear guest–host chromophores: A computational study," *J. Phys. Chem. A*, vol. 125, pp. 5303–5313, 2021.
- ⁴³⁶C. Schrieffer, S. Lochbrunner, A. R. Ofial, and E. Riedle, "The origin of ultrafast proton transfer: Multidimensional wave packet motion vs. tunneling," *Chem. Phys. Lett.*, vol. 503, pp. 61–65, 2011.

- ⁴³⁷V. Barone, S. Alessandrini, M. Biczysko, J. R. Cheeseman, D. C. Clary, A. B. McCoy, R. J. DiRisio, F. Neese, M. Melosso, and C. Puzzarini, "Computational molecular spectroscopy," *Nat. Rev. Methods Primers*, vol. 1, p. 38, 2021.
- ⁴³⁸D. Avagliano, M. Bonfanti, A. Nenov, and M. Garavelli, "Automatized protocol and interface to simulate QM/MM time-resolved transient absorption at TD-DFT level with COBRAMM," *J. Comput. Chem.*, vol. 43, pp. 1641–1655, 2022.
- ⁴³⁹C. Puzzarini, J. Bloino, N. Tasinato, and V. Barone, "Accuracy and Interpretability: The Devil and the Holy Grail. New Routes across Old Boundaries in Computational Spectroscopy," *Chem. Rev.*, vol. 119, pp. 8131–8191, 2019.
- ⁴⁴⁰L. Seidner, G. Stock, and W. Domcke, "Nonperturbative approach to femtosecond spectroscopy: General theory and application to multidimensional nonadiabatic photoisomerization processes," *J. Chem. Phys.*, vol. 103, pp. 3998–4011, 1995.
- ⁴⁴¹W. Domcke and G. Stock, "Theory of ultrafast nonadiabatic excited-state processes and their spectroscopic detection in real time," *Adv. Chem. Phys.*, vol. 100, pp. 1–169, 1997.
- ⁴⁴²X. Huang, W. Xie, N. Došlić, M. F. Gelin, and W. Domcke, "Ab Initio Quasiclassical Simulation of Femtosecond Time-Resolved Two-Dimensional Electronic Spectra of Pyrazine," *J. Phys. Chem. Lett.*, vol. 12, pp. 11736–11744, 2021.
- ⁴⁴³A. L. Whittock, T. T. Abiola, and V. G. Stavros, "A Perspective on Femtosecond Pump–Probe Spectroscopy in the Development of Future Sunscreens," *J. Phys. Chem. A*, vol. 126, pp. 2299–2308, 2022.
- ⁴⁴⁴D. Hu, J. Peng, L. Chen, M. F. Gelin, and Z. Lan, "Spectral Fingerprint of Excited-State Energy Transfer in Dendrimers through Polarization-Sensitive Transient-Absorption Pump–Probe Signals: On-the-Fly Nonadiabatic Dynamics Simulations," *J. Phys. Chem. Lett.*, vol. 12, pp. 9710–9719, 2021.
- ⁴⁴⁵C. Xu, K. Lin, D. Hu, F. L. Gu, M. F. Gelin, and Z. Lan, "Ultrafast Internal Conversion Dynamics through the on-the-Fly Simulation of Transient Absorption Pump–Probe Spectra with Different Electronic Structure Methods," *J. Phys. Chem. Lett.*, vol. 13, pp. 661–668, 2022.
- ⁴⁴⁶R. Perez-Castillo, V. M. Freixas, S. Mukamel, A. Martinez-Mesa, L. Uranga-Piña, S. Tretiak, M. F. Gelin, and S. Fernandez-Alberti, "Transient-absorption spectroscopy

- of dendrimers via nonadiabatic excited-state dynamics simulations," *Chem. Sci.*, vol. 15, pp. 13250–13261, 2024.
- ⁴⁴⁷A. Bhattacharjee and S. R. Leone, "Ultrafast X-ray Transient Absorption Spectroscopy of Gas-Phase Photochemical Reactions: A New Universal Probe of Photoinduced Molecular Dynamics," *Acc. Chem. Res.*, vol. 51, pp. 3203–3211, 2018.
- ⁴⁴⁸J. Zhang, J. Peng, D. Hu, M. F. Gelin, and Z. Lan, "What Two-Dimensional Electronic Spectroscopy Can Tell Us about Energy Transfer in Dendrimers: Ab Initio Simulations," *J. Phys. Chem. Lett.*, vol. 16, pp. 1007–1015, 2025.
- ⁴⁴⁹M. S. Schuurman and V. Blanchet, "Time-resolved photoelectron spectroscopy: the continuing evolution of a mature technique," *Phys. Chem. Chem. Phys.*, vol. 24, pp. 20012–20024, 2022.
- ⁴⁵⁰C. C. Pemberton, Y. Zhang, K. Saita, A. Kirrander, and P. M. Weber, "From the (1B) Spectroscopic State to the Photochemical Product of the Ultrafast Ring-Opening of 1,3-Cyclohexadiene: A Spectral Observation of the Complete Reaction Path," *J. Phys. Chem. A*, vol. 119, pp. 8832–8845, 2015.
- ⁴⁵¹A. Bhattacharjee, C. D. Pemmaraju, K. Schnorr, A. R. Attar, and S. R. Leone, "Ultrafast Intersystem Crossing in Acetylacetone via Femtosecond X-ray Transient Absorption at the Carbon K-Edge," *J. Am. Chem. Soc.*, vol. 139, pp. 16576–16583, 2017.
- ⁴⁵²T. J. A. Wolf, R. M. Parrish, R. H. Myhre, T. J. Martínez, H. Koch, and M. Gühr, "Observation of Ultrafast Intersystem Crossing in Thymine by Extreme Ultraviolet Time-Resolved Photoelectron Spectroscopy," *J. Phys. Chem. A*, vol. 123, pp. 6897–6903, 2019.
- ⁴⁵³T. Palmeira, D. S. Conceição, D. P. Ferreira, C. C. Ferreira, L. F. V. Ferreira, and M. N. Berberan-Santos, "Obtaining triplet-triplet absorption spectra and triplet lifetimes of long-lived molecules with a UV-Visible spectrophotometer," *J. Photochem. Photobiol.*, vol. 20, p. 100226, 2024.
- ⁴⁵⁴S. Biswas, J. W. Kim, X. Zhang, and G. D. Scholes, "Coherent Two-Dimensional and Broadband Electronic Spectroscopies," *Chem. Rev.*, vol. 122, pp. 4257–4321, 2022.
- ⁴⁵⁵J. D. Schultz, J. L. Yuly, E. A. Arsenault, K. Parker, S. N. Chowdhury, R. Dani, S. Kundu, H. Nuomin, Z. Zhang, J. Valdiviezo, *et al.*, "Coherence in Chemistry: Foundations and Frontiers," *Chem. Rev.*, vol. 124, pp. 11641–11766, 2024.

- ⁴⁵⁶T. R. Nelson, D. Ondarse-Alvarez, N. Oldani, B. Rodriguez-Hernandez, L. Alfonso-Hernandez, J. F. Galindo, V. D. Kleiman, S. Fernandez-Alberti, A. E. Roitberg, and S. Tretiak, "Coherent exciton-vibrational dynamics and energy transfer in conjugated organics," *Nat. Commun.*, vol. 9, p. 2316, 2018.
- ⁴⁵⁷B. Kaufman, P. Marquetand, T. Rozgonyi, and T. Weinacht, "Long-lived electronic coherences in molecules," *Phys. Rev. Lett.*, vol. 131, p. 263202, 2022.
- ⁴⁵⁸D. T. Matselyukh, V. Despré, N. V. Golubev, A. I. Kuleff, and H. J. Wörner, "Decoherence and revival in attosecond charge migration driven by non-adiabatic dynamics," *Nat. Phys.*, vol. 18, pp. 1206–1213, 2022.
- ⁴⁵⁹Y. Lee, K. Y. Oang, D. Kim, and H. Ihee, "A comparative review of time-resolved x-ray and electron scattering to probe structural dynamics," *Struct. Dyn.*, vol. 11, p. 031301, 2024.
- ⁴⁶⁰H. Yong, A. Kirrander, and P. M. Weber, "Time-resolved X-ray Scattering of Excited State Structure and Dynamics," in *Structural Dynamics with X-ray and Electron Scattering* (K. Amini, A. Rouzée, and M. J. J. Vrakking, eds.), vol. 25 of *Theoretical and Computational Chemistry Series*, pp. 344–373, United Kingdom: Royal Society of Chemistry, first ed., 2024.
- ⁴⁶¹A. Odate, A. Kirrander, P. M. Weber, and M. P. Minitti, "Brighter, faster, stronger: ultrafast scattering of free molecules," *Adv. Phys.: X*, vol. 8, p. 2126796, 2023.
- ⁴⁶²M. Centurion, T. J. Wolf, and J. Yang, "Ultrafast Imaging of Molecules with Electron Diffraction," *Annu. Rev. Phys. Chem.*, vol. 73, pp. 21–42, 2022.
- ⁴⁶³W. O. Razmus, K. Acheson, P. Bucksbaum, M. Centurion, E. Champenois, I. Gabalski, M. C. Hoffman, A. Howard, M.-F. Lin, Y. Liu, *et al.*, "Multichannel photodissociation dynamics in CS₂ studied by ultrafast electron diffraction," *Phys. Chem. Chem. Phys.*, vol. 24, pp. 15416–15427, 2022.
- ⁴⁶⁴E. G. Champenois, N. H. List, M. Ware, M. Britton, P. H. Bucksbaum, X. Cheng, M. Centurion, J. P. Cryan, R. Forbes, I. Gabalski, *et al.*, "Femtosecond Electronic and Hydrogen Structural Dynamics in Ammonia Imaged with Ultrafast Electron Diffraction," *Phys. Rev. Lett.*, vol. 131, p. 143001, 2023.
- ⁴⁶⁵H. Yong, N. Zotev, J. M. Ruddock, B. Stankus, M. Simmermacher, A. M. Carrascosa,

- W. Du, N. Goff, Y. Chang, D. Bellshaw, *et al.*, "Observation of the molecular response to light upon photoexcitation," *Nat. Commun.*, vol. 11, p. 2157, 2020.
- ⁴⁶⁶H. Yong, X. Xu, J. M. Ruddock, B. Stankus, A. M. Carrascosa, N. Zotev, D. Bellshaw, W. Du, N. Goff, Y. Chang, *et al.*, "Ultrafast X-ray scattering offers a structural view of excited-state charge transfer," *Proc. Nat. Acad. Sci. U.S.A.*, vol. 118, p. e2021714118, 2021.
- ⁴⁶⁷G. E. Busch and P. M. Rentzepis, "Picosecond Chemistry," *Science*, vol. 194, pp. 276–283, 1976.
- ⁴⁶⁸M. Khalil, M. A. Marcus, A. L. Smeigh, J. K. McCusker, H. H. W. Chong, and R. W. Schoenlein, "Picosecond X-ray Absorption Spectroscopy of a Photoinduced Iron(II) Spin Crossover Reaction in Solution," *J. Phys. Chem. A*, vol. 110, pp. 38–44, 2006.
- ⁴⁶⁹W. Gawelda, V.-T. Pham, M. Benfatto, Y. Zaushitsyn, M. Kaiser, D. Grolimund, S. L. Johnson, R. Abela, A. Hauser, C. Bressler, and M. Chergui, "Structure Determination of a Short-Lived Excited Iron(II) Complex by Picosecond X-Ray Absorption Spectroscopy," *Phys. Rev. Lett.*, vol. 98, p. 057401, 2007.
- ⁴⁷⁰D. Mayer, F. Lever, D. Picconi, J. Metje, S. Alisauskas, F. Calegari, S. Düsterer, C. Ehlert, R. Feifel, M. Niebuhr, *et al.*, "Following excited-state chemical shifts in molecular ultrafast x-ray photoelectron spectroscopy," *Nat. Commun.*, vol. 13, p. 198, 2022.
- ⁴⁷¹C. T. Kuhs, B. M. Luther, and A. T. Krummel, "Recent Advances in 2D IR Spectroscopy Driven by Advances in Ultrafast Technology," *IEEE J. Sel. Top. Quantum Electron.*, vol. 25, p. 3100313, 2019.
- ⁴⁷²H. J. S. de Oliveira, P. L. de Almeida Jr., B. A. Sampaio, J. P. A. Fernandes, O. D. Pessoa-Neto, E. A. de Lima, and L. F. de Almeida, "A handheld smartphone-controlled spectrophotometer based on hue to wavelength conversion for molecular absorption and emission measurements," *Sens. Actuators B: Chem.*, vol. 238, pp. 1084–1091, 2017.
- ⁴⁷³E. K. Grasse, M. H. Torcasio, and A. W. Smith, "Teaching UV-Vis Spectroscopy with a 3D-Printable Smartphone Spectrophotometer," *J. Chem. Educ.*, vol. 93, pp. 146–151, 2016.
- ⁴⁷⁴M. Baker, "Is there a reproducibility crisis?," *Nature*, vol. 533, pp. 452–454, 2016.
- ⁴⁷⁵G. H. Major, T. G. Avval, B. Moeini, G. Pinto, D. Shah, V. Jain, V. Carver, W. Skinner,

- T. R. Gengenbach, C. D. Easton, *et al.*, "Assessment of the frequency and nature of erroneous x-ray photoelectron spectroscopy analyses in the scientific literature," *J. Vac. Sci. Technol. A*, vol. 38, p. 061204, 2020.
- ⁴⁷⁶D. R. Baer and I. S. Gilmore, "Responding to the growing issue of research reproducibility," *J. Vac. Sci. Technol. A*, vol. 36, p. 068502, 2018.
- ⁴⁷⁷J. W. Pinder, G. H. Major, D. R. Baer, J. Terry, J. E. Whitten, J. Čechal, J. D. Crossman, A. J. Lizarbe, S. Jafari, C. D. Easton, *et al.*, "Avoiding common errors in X-ray photoelectron spectroscopy data collection and analysis, and properly reporting instrument parameters," *Appl. Surf. Sci. Adv.*, vol. 19, p. 100534, 2024.
- ⁴⁷⁸D. R. Baer, K. Artyushkova, C. R. Brundle, J. E. Castle, M. H. Engelhard, K. J. Gaskell, J. T. Grant, R. T. Haasch, M. R. Linford, C. J. Powell, *et al.*, "Practical guides for x-ray photoelectron spectroscopy: First steps in planning, conducting, and reporting XPS measurements," *J. Vac. Sci. Technol. A*, vol. 37, p. 031401, 2019.
- ⁴⁷⁹R. A. Mata and M. A. Suhm, "Benchmarking Quantum Chemical Methods: Are We Heading in the Right Direction?," *Angew. Chem. Int. Ed*, vol. 56, pp. 11011–11018, 2017.
- ⁴⁸⁰J. S. Beckwith, C. A. Rumble, and E. Vauthey, "Data analysis in transient electronic spectroscopy – an experimentalist's view," *Int. Rev. Phys. Chem.*, vol. 39, pp. 135–216, 2020.
- ⁴⁸¹B. Lang, A. Rosspeintner, G. Angulo, and E. Vauthey, "Model-free decomposition of transient absorption spectra into components with time-dependent shape," *EPJ Web Conf.*, vol. 205, p. 09011, 2019.
- ⁴⁸²B. Lang, A. Rosspeintner, and E. Vauthey, "Model-free Investigation of Ultrafast Bimolecular Chemical Reactions: Bimolecular Photo Induced Electron Transfer," *EPJ Web Conf.*, vol. 41, p. 05041, 2013.
- ⁴⁸³M. Tudorovskaya, R. S. Minns, and A. Kirrander, "Effects of probe energy and competing pathways on time-resolved photoelectron spectroscopy: the ring-opening of 1,3-cyclohexadiene," *Phys. Chem. Chem. Phys.*, vol. 20, pp. 17714–17726, 2018.
- ⁴⁸⁴A. Kirrander, K. Saita, and D. V. Shalashilin, "Ultrafast X-ray Scattering from Molecules," *J. Chem. Theory Comput.*, vol. 12, pp. 957–967, 2016.

- ⁴⁸⁵D. Zhong and A. H. Zewail, "Femtosecond Real-Time Probing of Reactions. 23. Studies of Temporal, Velocity, Angular, and State Dynamics from Transition States to Final Products by Femtosecond-Resolved Mass Spectrometry," *J. Phys. Chem. A*, vol. 102, pp. 4031–4058, 1998.
- ⁴⁸⁶M. Dantus, "Tracking Molecular Fragmentation in Electron–Ionization Mass Spectrometry with Ultrafast Time Resolution," *Acc. Chem. Res.*, vol. 57, pp. 845–854, 2024.
- ⁴⁸⁷S. Roeding and T. Brixner, "Coherent two-dimensional electronic mass spectrometry," *Nat. Commun.*, vol. 9, p. 2519, 2018.
- ⁴⁸⁸M. Hervé, V. Despré, P. Castellanos Nash, V. Lorient, A. Boyer, A. Scognamiglio, G. Karras, R. Brédy, E. Constant, A. G. G. M. Tielens, *et al.*, "Ultrafast dynamics of correlation bands following XUV molecular photoionization," *Nat. Phys.*, vol. 17, pp. 327–331, 2021.
- ⁴⁸⁹A. Marciniak, V. Despré, T. Barillot, A. Rouzée, M. C. E. Galbraith, J. Klei, C.-H. Yang, C. T. L. Smeenk, V. Lorient, S. Nagaprasad Reddy, *et al.*, "XUV excitation followed by ultrafast non-adiabatic relaxation in PAH molecules as a femto-astrochemistry experiment," *Nat. Commun.*, vol. 6, p. 7909, 2015.
- ⁴⁹⁰S. Wang, T. Kind, P. L. Bremer, D. J. Tantillo, and O. Fiehn, "Beyond the Ground State: Predicting Electron Ionization Mass Spectra Using Excited-State Molecular Dynamics," *J. Chem. Inf. Model.*, vol. 62, pp. 4403–4410, 2022.
- ⁴⁹¹C. E. M. Gonçalves, R. D. Levine, and F. Remacle, "Ultrafast geometrical reorganization of a methane cation upon sudden ionization: an isotope effect on electronic non-equilibrium quantum dynamics," *Phys. Chem. Chem. Phys.*, vol. 23.21, pp. 12051–12059, 2021.
- ⁴⁹²J. Koopman and S. Grimme, "Calculation of Mass Spectra with the QCxMS Method for Negatively and Multiply Charged Molecules," *J. Am. Soc. Mass Spectrom.*, vol. 33, pp. 2226–2242, 2022.
- ⁴⁹³M. R. Silva-Junior, M. Schreiber, S. P. A. Sauer, and W. Thiel, "Benchmarks of electronically excited states: Basis set effects on CASPT2 results," *J. Chem. Phys.*, vol. 133, p. 174318, 2010.
- ⁴⁹⁴M. Kulichenko, B. Nebgen, N. Lubbers, J. S. Smith, K. Barros, A. E. A. Allen, A. Habib, E. Shinkle, N. Fedik, Y. W. Li, *et al.*, "Data Generation for Machine Learning Interatomic Potentials and Beyond," *Chem. Rev.*, vol. 24, pp. 13681–13714, 2024.

- ⁴⁹⁵M. Pinheiro, M. de Oliveira Bispo, R. S. Mattos, M. Telles do Casal, B. C. Garain, J. M. Toldo, S. Mukherjee, and M. Barbatti, "ULaMDyn: enhancing excited-state dynamics analysis through streamlined unsupervised learning," *Digit. Discov.*, vol. 4, pp. 666–682, 2025.
- ⁴⁹⁶S. Polonius, O. Zhuravel, B. Bachmair, and S. Mai, "LVC/MM: A Hybrid Linear Vibronic Coupling/Molecular Mechanics Model with Distributed Multipole-Based Electrostatic Embedding for Highly Efficient Surface Hopping Dynamics in Solution," *J. Chem. Theory Comput.*, vol. 19, pp. 7171–7186, 2023.
- ⁴⁹⁷L. L. E. Cigrang, J. A. Green, S. Gómez, J. Cerezo, R. Improta, G. Prampolini, F. Santoro, and G. A. Worth, "Non-adiabatic direct quantum dynamics using force fields: Toward solvation," *J. Chem. Phys.*, vol. 160, p. 174120, 2024.
- ⁴⁹⁸E. Vandaele, M. Mališ, and S. Lubner, "The Δ SCF method for non-adiabatic dynamics of systems in the liquid phase," *J. Chem. Phys.*, vol. 156, p. 130901, 2022.
- ⁴⁹⁹M. Rivera, M. Dommett, and R. Crespo-Otero, "ONIOM(QM:QM') Electrostatic Embedding Schemes for Photochemistry in Molecular Crystals," *J. Chem. Theory Comput.*, vol. 15, pp. 2504–2516, 2019.
- ⁵⁰⁰T. J. Zuehlsdorff and C. M. Isborn, "Modeling absorption spectra of molecules in solution," *Int. J. Quantum Chem.*, vol. 119, p. e25719, 2018.
- ⁵⁰¹P. O. Dral, M. Barbatti, and W. Thiel, "Nonadiabatic Excited-State Dynamics with Machine Learning," *J. Phys. Chem. Lett.*, vol. 19, pp. 5660–5663, 2018.
- ⁵⁰²L. Dupuy and N. T. Maitra, "Exciting DeePMD: Learning excited-state energies, forces, and non-adiabatic couplings," *J. Chem. Phys.*, vol. 161, p. 134103, 2024.